

6. To prove that the only prime triple is 3, 5, 7.

Let's assume  $p$  is a prime number.

For a prime triple to exist,

$p, p+2$  &  $p+4$  must all be primes &  $p \in \mathbb{N}$ .

But, we have just seen (Problem 5) that one of  $p, p+2, p+4$  are always divisible by 3. Hence

$p, p+2, p+4$  cannot all be primes unless  $p$  or  $p+2$  are themselves equal to 3 ( $\because p+4 > 3 \forall p \in \mathbb{N}$ ).

But for  $p+2$  to be equal to 3,  $p$  should be 1, which is not a prime by definition.

Therefore  $p$  has to be equal to 3.

$\therefore$  The only prime triple is  
 $3 (= p), 5 (= p+2), 7 (= p+4).$