Output tables for the test of Multiple comparisons.

June 12, 2017

1 Average rankings of Friedman test

Average ranks obtained by applying the Friedman procedure

| Ranking | 4.7812 | 9 | 4.3438 | 4.5625 | 4.5938 | 4.7188 | 3.9688 | 3.0312 |
|-----------|--------|--------|--------|--------|--------|----------|-----------|--------|
| Algorithm | Base | ADASYN | SMOTE | Bord | NCL | SMOTE+TL | SMOTE+ENN | CCR |
| | | | | | | | | |

Table 1: Average Rankings of the algorithms

Friedman statistic considering reduction performance (distributed according to chi-square with 7 degrees of freedom: 25.885417.

2 Post hoc comparisons

Results achieved on post hoc comparisons for $\alpha=0.05,\,\alpha=0.10$ and adjusted p-values.

2.1 P-values for $\alpha = 0.05$

| i | algorithms | $z = (R_0 - R_i)/SE$ | d | Shaffer |
|--------------|------------------------|----------------------|----------|----------|
| 28 | ADASYN vs. CCR | 4.847948 | 0.000001 | 0.001786 |
| 27 | ADASYN vs. SMOTE+ENN | 3.317017 | 0.00091 | 0.002381 |
| 56 | Base vs. CCR | 2.857738 | 0.004267 | 0.002381 |
| 25 | SMOTE+TL vs. CCR | 2.755676 | 0.005857 | 0.002381 |
| 24 | ADASYN vs. SMOTE | 2.704645 | 0.006838 | 0.002381 |
| 23 | NCL vs. CCR | 2.551552 | 0.010724 | 0.002381 |
| 22 | Bord vs. CCR | 2.500521 | 0.012401 | 0.002381 |
| 21 | ADASYN vs. Bord | 2.347428 | 0.018904 | 0.002381 |
| 20 | ADASYN vs. NCL | 2.296397 | 0.021653 | 0.0025 |
| 19 | SMOTE vs. CCR | 2.143304 | 0.032089 | 0.002632 |
| 18 | ADASYN vs. SMOTE+TL | 2.092272 | 0.036414 | 0.002778 |
| 17 | Base vs. ADASYN | 1.99021 | 0.046568 | 0.002941 |
| 16 | SMOTE+ENN vs. CCR | 1.530931 | 0.125786 | 0.003125 |
| 15 | Base vs. SMOTE+ENN | 1.326807 | 0.184573 | 0.003333 |
| 14 | SMOTE+TL vs. SMOTE+ENN | 1.224745 | 0.220671 | 0.003571 |
| 13 | NCL vs. SMOTE+ENN | 1.020621 | 0.307434 | 0.003846 |
| 12 | Bord vs. SMOTE+ENN | 0.96959 | 0.332251 | 0.004167 |
| 11 | Base vs. SMOTE | 0.714435 | 0.474959 | 0.004545 |
| 10 | SMOTE vs. SMOTE+TL | 0.612372 | 0.540291 | 0.005 |
| 6 | SMOTE vs. SMOTE+ENN | 0.612372 | 0.540291 | 0.005556 |
| _∞ | SMOTE vs. NCL | 0.408248 | 0.683091 | 0.00625 |
| _ | Base vs. Bord | 0.357217 | 0.720929 | 0.007143 |
| 9 | SMOTE vs. Bord | 0.357217 | 0.720929 | 0.008333 |
| 2 | Base vs. NCL | 0.306186 | 0.759463 | 0.01 |
| 4 | Bord vs. SMOTE+TL | 0.255155 | 0.798603 | 0.0125 |
| 3 | NCL vs. SMOTE+TL | 0.204124 | 0.838256 | 0.016667 |
| 2 | Base vs. SMOTE+TL | 0.102062 | 0.918707 | 0.025 |
| П | Bord vs. NCL | 0.051031 | 0.959301 | 0.05 |

Table 2: P-values Table for $\alpha = 0.05$

| i | algorithms | $z = (R_0 - R_i)/SE$ | d | Shaffer |
|----|------------------------|----------------------|----------|-----------|
| 28 | ADASYN vs. CCR | 4.847948 | 0.000001 | 0.003571 |
| 27 | ADASYN vs. SMOTE+ENN | 3.317017 | 0.00091 | 0.004762 |
| 26 | Base vs. CCR | 2.857738 | 0.004267 | 0.004762 |
| 25 | SMOTE+TL vs. CCR | 2.755676 | 0.005857 | 0.004762 |
| 24 | ADASYN vs. SMOTE | 2.704645 | 0.006838 | 0.004762 |
| 23 | NCL vs. CCR | 2.551552 | 0.010724 | 0.004762 |
| 22 | Bord vs. CCR | 2.500521 | 0.012401 | 0.004762 |
| 21 | ADASYN vs. Bord | 2.347428 | 0.018904 | 0.004762 |
| 20 | ADASYN vs. NCL | 2.296397 | 0.021653 | 0.005 |
| 19 | SMOTE vs. CCR | 2.143304 | 0.032089 | 0.005263 |
| 18 | ADASYN vs. SMOTE+TL | 2.092272 | 0.036414 | 0.005556 |
| 17 | Base vs. ADASYN | 1.99021 | 0.046568 | 0.005882 |
| 16 | SMOTE+ENN vs. CCR | 1.530931 | 0.125786 | 0.00625 |
| 15 | Base vs. SMOTE+ENN | 1.326807 | 0.184573 | 0.006667 |
| 14 | SMOTE+TL vs. SMOTE+ENN | 1.224745 | 0.220671 | 0.007143 |
| 13 | NCL vs. SMOTE+ENN | 1.020621 | 0.307434 | 0.007692 |
| 12 | Bord vs. SMOTE+ENN | 0.96959 | 0.332251 | 0.008333 |
| 11 | Base vs. SMOTE | 0.714435 | 0.474959 | 0.009091 |
| 10 | SMOTE vs. SMOTE+TL | 0.612372 | 0.540291 | 0.01 |
| 6 | SMOTE vs. SMOTE+ENN | 0.612372 | 0.540291 | 0.0111111 |
| œ | SMOTE vs. NCL | 0.408248 | 0.683091 | 0.0125 |
| 7 | Base vs. Bord | 0.357217 | 0.720929 | 0.014286 |
| 9 | SMOTE vs. Bord | 0.357217 | 0.720929 | 0.016667 |
| v | Base vs. NCL | 0.306186 | 0.759463 | 0.02 |
| 4 | Bord vs. SMOTE+TL | 0.255155 | 0.798603 | 0.025 |
| က | NCL vs. SMOTE+TL | 0.204124 | 0.838256 | 0.033333 |
| 2 | Base vs. SMOTE+TL | 0.102062 | 0.918707 | 0.05 |
| 1 | Bord vs. NCL | 0.051031 | 0.959301 | 0.1 |
| | | | | |

Table 3: P-values Table for $\alpha = 0.10$

Shaffer's procedure rejects those hypotheses that have an unadjusted p-value ≤ 0.003571 .

| | hypothesis | unadjusted p | p_{Shaf} |
|----|------------------------|----------------|------------|
| П | ADASYN vs. CCR | 0.000001 | 0.000035 |
| 2 | ADASYN vs .SMOTE+ENN | 0.00091 | 0.019107 |
| က | Base vs .CCR | 0.004267 | 0.089601 |
| 4 | SMOTE+TL vs .CCR | 0.005857 | 0.122999 |
| v | ADASYN vs. SMOTE | 0.006838 | 0.143593 |
| 9 | NCL vs.CCR | 0.010724 | 0.225213 |
| 7 | Bord vs .CCR | 0.012401 | 0.260423 |
| œ | ADASYN vs. Bord | 0.018904 | 0.396974 |
| 6 | ADASYN vs. NCL | 0.021653 | 0.396974 |
| 10 | SMOTE vs.CCR | 0.032089 | 0.51342 |
| 11 | ADASYN vs.SMOTE+TL | 0.036414 | 0.582626 |
| 12 | Base vs .ADASYN | 0.046568 | 0.745084 |
| 13 | SMOTE+ENN vs .CCR | 0.125786 | 2.012583 |
| 14 | Base vs.SMOTE+ENN | 0.184573 | 2.768588 |
| 15 | SMOTE+TL vs .SMOTE+ENN | 0.220671 | 2.868728 |
| 16 | NCL vs .SMOTE+ENN | 0.307434 | 3.996644 |
| 17 | Bord vs .SMOTE+ENN | 0.332251 | 3.996644 |
| 18 | Base vs .SMOTE | 0.474959 | 5.224544 |
| 19 | SMOTE vs. SMOTE+TL | 0.540291 | 5.402914 |
| 20 | SMOTE vs .SMOTE+ENN | 0.540291 | 5.402914 |
| 21 | SMOTE vs.NCL | 0.683091 | 5.464731 |
| 22 | Base vs .Bord | 0.720929 | 5.464731 |
| 23 | SMOTE vs .Bord | 0.720929 | 5.464731 |
| 24 | Base vs .NCL | 0.759463 | 5.464731 |
| 25 | Bord vs .SMOTE+TL | 0.798603 | 5.464731 |
| 26 | NCL vs .SMOTE+TL | 0.838256 | 5.464731 |
| 27 | Base vs .SMOTE+TL | 0.918707 | 5.464731 |
| 28 | Bord vs .NCL | 0.959301 | 5.464731 |
| | | | |

Table 4: Adjusted p-values