

Output tables for the test of Multiple comparisons.

June 12, 2017

1 Average rankings of Friedman test

Average ranks obtained by applying the Friedman procedure

| Algorithm | Ranking |
|-----------|---------|
| Base | 6.875 |
| ADASYN | 3.4062 |
| SMOTE | 4.8125 |
| Bord | 5.0938 |
| NCL | 3.8125 |
| SMOTE+TL | 4.5 |
| SMOTE+ENN | 5.3125 |
| CCR | 2.1875 |

Table 1: Average Rankings of the algorithms

Friedman statistic considering reduction performance (distributed according to chi-square with 7 degrees of freedom: 73.427083.

P-value computed by Friedman Test: 5.868816543852517E-11.

2 Post hoc comparisons

Results achieved on post hoc comparisons for $\alpha = 0.05$, $\alpha = 0.10$ and adjusted p-values.

2.1 P-values for $\alpha = 0.05$

| i | algorithms | $z = (R_0 - R_i)/SE$ | p | Shaffer |
|-----|------------------------|----------------------|----------|----------|
| 28 | Base vs. CCR | 7.654655 | 0 | 0.001786 |
| 27 | Base vs. ADASYN | 5.664445 | 0 | 0.002381 |
| 26 | SMOTE+ENN vs. CCR | 5.103104 | 0 | 0.002381 |
| 25 | Base vs. NCL | 5.001042 | 0.000001 | 0.002381 |
| 24 | Bord vs. CCR | 4.745886 | 0.000002 | 0.002381 |
| 23 | SMOTE vs. CCR | 4.286607 | 0.000018 | 0.002381 |
| 22 | Base vs. SMOTE+TL | 3.878359 | 0.000105 | 0.002381 |
| 21 | SMOTE+TL vs. CCR | 3.776297 | 0.000159 | 0.002381 |
| 20 | Base vs. SMOTE | 3.368048 | 0.000757 | 0.003125 |
| 19 | ADASYN vs. SMOTE+ENN | 3.112893 | 0.001853 | 0.003125 |
| 18 | Base vs. Bord | 2.908769 | 0.003629 | 0.003125 |
| 17 | ADASYN vs. Bord | 2.755676 | 0.005857 | 0.003125 |
| 16 | NCL vs. CCR | 2.653614 | 0.007963 | 0.003125 |
| 15 | Base vs. SMOTE+ENN | 2.551552 | 0.010724 | 0.003333 |
| 14 | NCL vs. SMOTE+ENN | 2.44949 | 0.014306 | 0.003571 |
| 13 | ADASYN vs. SMOTE | 2.296397 | 0.021653 | 0.003846 |
| 12 | Bord vs. NCL | 2.092272 | 0.036414 | 0.004167 |
| 11 | ADASYN vs. CCR | 1.99021 | 0.046568 | 0.004545 |
| 10 | ADASYN vs. SMOTE+TL | 1.786086 | 0.074085 | 0.005 |
| 9 | SMOTE vs. NCL | 1.632993 | 0.10247 | 0.005556 |
| 8 | SMOTE+TL vs. SMOTE+ENN | 1.326807 | 0.184573 | 0.00625 |
| 7 | NCL vs. SMOTE+TL | 1.122683 | 0.261572 | 0.007143 |
| 6 | Bord vs. SMOTE+TL | 0.96959 | 0.332251 | 0.008333 |
| 5 | SMOTE vs. SMOTE+ENN | 0.816497 | 0.414216 | 0.01 |
| 4 | ADASYN vs. NCL | 0.663403 | 0.507072 | 0.0125 |
| 3 | SMOTE vs. SMOTE+TL | 0.51031 | 0.609834 | 0.016667 |
| 2 | SMOTE vs. Bord | 0.459279 | 0.646034 | 0.025 |
| 1 | Bord vs. SMOTE+ENN | 0.357217 | 0.720929 | 0.05 |

Table 2: P-values Table for $\alpha = 0.05$

Shaffer's procedure rejects those hypotheses that have an unadjusted p-value ≤ 0.001786 .

2.2 P-values for $\alpha = 0.10$

| i | algorithms | $z = (R_0 - R_i)/SE$ | p | Shaffer |
|-----|------------------------|----------------------|----------|----------|
| 28 | Base vs. CCR | 7.654635 | 0 | 0.003571 |
| 27 | Base vs. ADASYN | 5.664445 | 0 | 0.004762 |
| 26 | SMOTE+ENN vs. CCR | 5.103104 | 0 | 0.004762 |
| 25 | Base vs. NCL | 5.001042 | 0.000001 | 0.004762 |
| 24 | Bord vs. CCR | 4.745886 | 0.000002 | 0.004762 |
| 23 | SMOTE vs. CCR | 4.286607 | 0.000018 | 0.004762 |
| 22 | Base vs. SMOTE+TL | 3.878359 | 0.000105 | 0.004762 |
| 21 | SMOTE+TL vs. CCR | 3.776297 | 0.000159 | 0.004762 |
| 20 | Base vs. SMOTE | 3.368048 | 0.000757 | 0.00625 |
| 19 | ADASYN vs. SMOTE+ENN | 3.112893 | 0.001853 | 0.00625 |
| 18 | Base vs. Bord | 2.908769 | 0.003629 | 0.00625 |
| 17 | ADASYN vs. Bord | 2.755676 | 0.005857 | 0.00625 |
| 16 | NCL vs. CCR | 2.653614 | 0.007963 | 0.00625 |
| 15 | Base vs. SMOTE+ENN | 2.551552 | 0.010724 | 0.006667 |
| 14 | NCL vs. SMOTE+ENN | 2.44949 | 0.014306 | 0.007143 |
| 13 | ADASYN vs. SMOTE | 2.296397 | 0.021653 | 0.007692 |
| 12 | Bord vs. NCL | 2.092272 | 0.036414 | 0.008333 |
| 11 | ADASYN vs. CCR | 1.99021 | 0.046568 | 0.009091 |
| 10 | ADASYN vs. SMOTE+TL | 1.786086 | 0.074085 | 0.01 |
| 9 | SMOTE vs. NCL | 1.632993 | 0.10247 | 0.01111 |
| 8 | SMOTE+TL vs. SMOTE+ENN | 1.326807 | 0.184573 | 0.0125 |
| 7 | NCL vs. SMOTE+TL | 1.122683 | 0.261572 | 0.014286 |
| 6 | Bord vs. SMOTE+TL | 0.96959 | 0.332251 | 0.016667 |
| 5 | SMOTE vs. SMOTE+ENN | 0.816497 | 0.414216 | 0.02 |
| 4 | ADASYN vs. NCL | 0.663403 | 0.507072 | 0.025 |
| 3 | SMOTE vs. SMOTE+TL | 0.51031 | 0.609834 | 0.033333 |
| 2 | SMOTE vs. Bord | 0.459279 | 0.646034 | 0.05 |
| 1 | Bord vs. SMOTE+ENN | 0.357217 | 0.720929 | 0.1 |

Table 3: P-values Table for $\alpha = 0.10$

Shaffer's procedure rejects those hypotheses that have an unadjusted p-value ≤ 0.003571 .

2.3 Adjusted p-values

| i | hypothesis | unadjusted p | p_{Shelf} |
|----|------------------------|----------------|-------------|
| 1 | Base vs .CCR | 0 | 0 |
| 2 | Base vs .ADASYN | 0 | 0 |
| 3 | SMOTE+ENN vs .CCR | 0 | 0.000007 |
| 4 | Base vs .NCL | 0.000001 | 0.000012 |
| 5 | Bord vs .CCR | 0.000002 | 0.000044 |
| 6 | SMOTE vs .CCR | 0.000018 | 0.000381 |
| 7 | Base vs .SMOTE+TL | 0.000105 | 0.002208 |
| 8 | SMOTE+TL vs .CCR | 0.000159 | 0.003343 |
| 9 | Base vs .SMOTE | 0.000757 | 0.012112 |
| 10 | ADASYN vs .SMOTE+ENN | 0.001853 | 0.029642 |
| 11 | Base vs .Bord | 0.003629 | 0.058057 |
| 12 | ADASYN vs .Bord | 0.005857 | 0.093714 |
| 13 | NCL vs .CCR | 0.007963 | 0.127416 |
| 14 | Base vs .SMOTE+ENN | 0.010724 | 0.160867 |
| 15 | NCL vs .SMOTE+ENN | 0.014306 | 0.185976 |
| 16 | ADASYN vs .SMOTE | 0.021653 | 0.281492 |
| 17 | Bord vs .NCL | 0.036414 | 0.43697 |
| 18 | ADASYN vs .CCR | 0.046568 | 0.512245 |
| 19 | ADASYN vs .SMOTE+TL | 0.074085 | 0.740853 |
| 20 | SMOTE vs .NCL | 0.10247 | 0.922234 |
| 21 | SMOTE+TL vs .SMOTE+ENN | 0.184573 | 1.47658 |
| 22 | NCL vs .SMOTE+TL | 0.261572 | 1.831006 |
| 23 | Bord vs .SMOTE+TL | 0.332251 | 1.993506 |
| 24 | SMOTE vs .SMOTE+ENN | 0.414216 | 2.071081 |
| 25 | ADASYN vs .NCL | 0.507072 | 2.071081 |
| 26 | SMOTE vs .SMOTE+TL | 0.609834 | 2.071081 |
| 27 | SMOTE vs .Bord | 0.646034 | 2.071081 |
| 28 | Bord vs .SMOTE+ENN | 0.720929 | 2.071081 |

Table 4: Adjusted p -values