

Table S1: Total time (in seconds) required to solve the k QUBO models generated with QUBO-Correlation for the Classification task with different QUBO solvers. Missing values for the QPU indicate the problem did not fit on the hardware.

| Dataset | N | QPU | Hybrid | SA | SD | Tabu |
|---------------|------|-------|--------|----------|---------|---------|
| waveform-5000 | 40 | 39.0 | 394.4 | 57.9 | 7.8 | 474.6 |
| SPECTF | 44 | 48.4 | 426.3 | 72.3 | 9.3 | 522.4 |
| coverttype | 54 | 130.1 | 491.5 | 17.0 | 1.9 | 99.1 |
| spambase | 57 | 65.9 | 487.4 | 107.1 | 15.7 | 598.9 |
| nomao | 118 | 100.1 | 507.5 | 323.6 | 54.3 | 620.9 |
| tecator | 124 | 95.6 | 504.3 | 374.2 | 57.7 | 623.5 |
| USPS | 256 | - | 541.1 | 1174.0 | 220.4 | 785.2 |
| isolet | 617 | - | 640.2 | 6280.7 | 1260.4 | 1735.7 |
| Bioresponse | 1776 | - | 1435.1 | 53978.2 | 10814.2 | 10531.4 |
| SVHN_small | 3072 | - | 3575.4 | 124041.7 | 33802.1 | 32440.0 |
| gisette | 5000 | - | 8666.3 | 80062.4 | 18811.6 | 18238.1 |

Table S2: Total time (in seconds) required to solve the k QUBO models generated with QUBO-Boosting for the Classification task with different QUBO solvers. Missing values for the QPU indicate the problem did not fit on the hardware.

| Dataset | N | QPU | Hybrid | SA | SD | Tabu |
|---------------|------|-------|--------|----------|---------|---------|
| waveform-5000 | 40 | 41.7 | 384.2 | 62.3 | 6.6 | 473.1 |
| SPECTF | 44 | 44.3 | 422.9 | 80.1 | 9.5 | 524.3 |
| coverttype | 54 | 129.0 | 491.2 | 18.6 | 1.9 | 99.1 |
| spambase | 57 | 61.9 | 486.6 | 125.2 | 14.2 | 597.0 |
| nomao | 118 | 110.2 | 498.7 | 386.3 | 50.1 | 614.5 |
| tecator | 124 | 91.6 | 512.5 | 388.8 | 58.6 | 622.9 |
| USPS | 256 | - | 545.3 | 1324.5 | 215.0 | 775.9 |
| isolet | 617 | - | 709.5 | 7141.0 | 1224.1 | 1715.3 |
| Bioresponse | 1776 | - | 1446.0 | 71102.2 | 10639.2 | 10502.3 |
| SVHN_small | 3072 | - | 3593.6 | 183687.1 | 23886.7 | 23301.3 |
| gisette | 5000 | - | 8671.6 | 74620.9 | 14418.6 | 14820.1 |

Table S3: Total time (in seconds) required to solve the k QUBO models generated with MIQUBO for the Classification task with different QUBO solvers. Missing values for the QPU indicate the problem did not fit on the hardware.

| Dataset | N | QPU | Hybrid | SA | SD | Tabu |
|---------------|------|-------|--------|---------|---------|---------|
| waveform-5000 | 40 | 39.2 | 385.9 | 7.5 | 1.0 | 78.6 |
| SPECTF | 44 | 45.1 | 421.7 | 9.5 | 1.2 | 86.7 |
| coverttype | 54 | 127.3 | 809.9 | 17.0 | 1.9 | 99.0 |
| spambase | 57 | 51.5 | 486.4 | 17.6 | 2.0 | 99.1 |
| nomao | 118 | 98.1 | 512.5 | 46.6 | 7.9 | 101.9 |
| tecator | 124 | 90.2 | 515.1 | 62.3 | 8.8 | 102.3 |
| USPS | 256 | - | 542.6 | 138.0 | 34.6 | 124.3 |
| isolet | 617 | - | 642.4 | 838.1 | 201.6 | 263.8 |
| Bioresponse | 1776 | - | 1423.4 | 11031.8 | 1727.8 | 1632.8 |
| SVHN_small | 3072 | - | 3591.1 | 23332.5 | 5455.9 | 5146.8 |
| gisette | 5000 | - | 8606.4 | 78635.7 | 14210.1 | 14610.5 |

Table S4: Total time (in seconds) required to solve the k QUBO models generated with QUBO-Correlation for the Ranking task with different QUBO solvers.

| Dataset | F | QPU | Hybrid | SA | SD | Tabu |
|---------|----|-------|--------|------|-----|------|
| OHSUMED | 45 | 154.1 | 436.8 | 13.5 | 1.7 | 89.4 |
| MQ2007 | 46 | 472.5 | 444.5 | 15.6 | 1.9 | 91.5 |
| MQ2008 | 46 | 122.7 | 436.7 | 15.0 | 1.6 | 91.7 |

Table S5: Total time (in seconds) required to solve the k QUBO models generated with QUBO-Boosting for the Ranking task with different QUBO solvers.

| Dataset | F | QPU | Hybrid | SA | SD | Tabu |
|---------|----|-------|--------|------|-----|------|
| OHSUMED | 45 | 382.7 | 441.5 | 15.4 | 1.6 | 89.5 |
| MQ2007 | 46 | 407.9 | 441.1 | 16.6 | 1.5 | 91.4 |
| MQ2008 | 46 | 57.2 | 442.2 | 17.4 | 1.6 | 91.7 |

Table S6: Total time (in seconds) required to solve the k QUBO models generated with MIQUBO for the Ranking task with different QUBO solvers.

| Dataset | F | QPU | Hybrid | SA | SD | Tabu |
|---------|----|-------|--------|------|-----|------|
| OHSUMED | 45 | 497.9 | 435.1 | 13.9 | 1.5 | 89.2 |
| MQ2007 | 46 | 74.0 | 445.0 | 12.8 | 1.5 | 91.2 |
| MQ2008 | 46 | 96.4 | 443.1 | 13.0 | 1.5 | 91.3 |

Table S7: Drill down of the time (in seconds) required to solve the QUBO models generated with QUBO-Correlation for the Classification task. The Embedding column refers to the time required to embed the problem on the QPU. The columns under QPU show the time-to-solution as observed by the local client (Total), splitted between the actual physical annealing process (Sampling) and the latency due to the data transfer as well as further waiting time after the task is queued (Latency). Note that the Latency time is more than one order of magnitude higher than the Sampling time.

| Dataset | F | Embedding | QPU | | |
|---------------|-----|-----------|-------|----------|---------|
| | | | Total | Sampling | Latency |
| waveform-5000 | 40 | 2.9 | 39.0 | 0.9 | 38.1 |
| SPECTF | 44 | 3.5 | 48.4 | 1.1 | 47.3 |
| coverttype | 54 | 7.1 | 130.1 | 1.1 | 129.0 |
| spambase | 57 | 17.7 | 65.9 | 1.2 | 64.8 |
| nomao | 118 | 54.3 | 100.1 | 1.6 | 98.5 |
| tecator | 124 | 125.2 | 95.6 | 1.5 | 94.2 |

Table S8: Drill down of the time (in seconds) required to solve the QUBO models generated with QUBO-Boosting for the Classification task. The Embedding column refers to the time required to embed the problem on the QPU. The columns under QPU show the time-to-solution as observed by the local client (Total), splitted between the actual physical annealing process (Sampling) and the latency due to the data transfer as well as further waiting time after the task is queued (Latency). Note that the Latency time is more than one order of magnitude higher than the Sampling time.

| Dataset | F | Embedding | QPU | | |
|---------------|-----|-----------|-------|----------|---------|
| | | | Total | Sampling | Latency |
| waveform-5000 | 40 | 4.4 | 41.7 | 0.8 | 40.9 |
| SPECTF | 44 | 7.0 | 44.3 | 0.9 | 43.4 |
| covertime | 54 | 18.6 | 129.0 | 1.4 | 127.6 |
| spambase | 57 | 31.2 | 61.9 | 1.4 | 60.6 |
| nomao | 118 | 138.1 | 110.2 | 1.6 | 108.6 |
| tecator | 124 | 287.1 | 91.6 | 1.6 | 90.0 |

Table S9: Drill down of the time (in seconds) required to solve the QUBO models generated with MIQUBO for the Classification task. The Embedding column refers to the time required to embed the problem on the QPU. The columns under QPU show the time-to-solution as observed by the local client (Total), splitted between the actual physical annealing process (Sampling) and the latency due to the data transfer as well as further waiting time after the task is queued (Latency). Note that the Latency time is more than one order of magnitude higher than the Sampling time.

| Dataset | F | Embedding | QPU | | |
|---------------|-----|-----------|-------|----------|---------|
| | | | Total | Sampling | Latency |
| waveform-5000 | 40 | 7.0 | 39.2 | 0.9 | 38.3 |
| SPECTF | 44 | 5.3 | 45.1 | 1.1 | 44.0 |
| covertime | 54 | 7.9 | 127.3 | 1.2 | 126.1 |
| spambase | 57 | 14.2 | 51.5 | 1.0 | 50.5 |
| nomao | 118 | 209.9 | 98.1 | 1.6 | 96.5 |
| tecator | 124 | 164.6 | 90.2 | 1.5 | 88.7 |

Table S10: Drill down of the time (in seconds) required to solve the QUBO models generated with QUBO-Correlation for the Ranking task. The Embedding column refers to the time required to embed the problem on the QPU. The columns under QPU show the time-to-solution as observed by the local client (Total), splitted between the actual physical annealing process (Sampling) and the latency due to the data transfer as well as further waiting time after the task is queued (Latency). Note that the Latency time is more than one order of magnitude higher than the Sampling time.

| Dataset | F | Embedding | QPU | | |
|---------|----|-----------|-------|----------|---------|
| | | | Total | Sampling | Latency |
| OHSUMED | 45 | 10.5 | 154.1 | 1.1 | 153.0 |
| MQ2007 | 46 | 11.7 | 472.5 | 1.0 | 471.5 |
| MQ2008 | 46 | 7.9 | 122.7 | 1.2 | 121.6 |

Table S11: Drill down of the time (in seconds) required to solve the QUBO models generated with QUBO-Boosting for the Ranking task. The Embedding column refers to the time required to embed the problem on the QPU. The columns under QPU show the time-to-solution as observed by the local client (Total), splitted between the actual physical annealing process (Sampling) and the latency due to the data transfer as well as further waiting time after the task is queued (Latency). Note that the Latency time is more than one order of magnitude higher than the Sampling time.

| Dataset | F | Embedding | QPU | | |
|---------|----|-----------|-------|----------|---------|
| | | | Total | Sampling | Latency |
| OHSUMED | 45 | 8.8 | 382.7 | 1.2 | 381.5 |
| MQ2007 | 46 | 17.5 | 407.9 | 1.0 | 406.9 |
| MQ2008 | 46 | 9.7 | 57.2 | 1.0 | 56.2 |

Table S12: Drill down of the time (in seconds) required to solve the QUBO models generated with MIQUBO for the Ranking task. The Embedding column refers to the time required to embed the problem on the QPU. The columns under QPU show the time-to-solution as observed by the local client (Total), splitted between the actual physical annealing process (Sampling) and the latency due to the data transfer as well as further waiting time after the task is queued (Latency). Note that the Latency time is more than one order of magnitude higher than the Sampling time.

| Dataset | F | Embedding | QPU | | |
|---------|----|-----------|-------|----------|---------|
| | | | Total | Sampling | Latency |
| OHSUMED | 45 | 7.2 | 497.9 | 1.0 | 496.9 |
| MQ2007 | 46 | 17.0 | 74.0 | 1.0 | 72.9 |
| MQ2008 | 46 | 10.3 | 96.4 | 1.2 | 95.3 |