Fusers in homogenous ensemble of subsampled majority class for highly imbalanced data classification

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Abstract

This is the abstract for this article.

Keywords: classification, classifier ensemble, undersampling, imbalanced data

1. Conclusions

This is a sample article that uses the jmlr class with the wcp class option. Please follow the guidelines in this sample document as it can help to reduce complications when combining the articles into a book. Please avoid using obsolete commands, such as `\rm`, and obsolete packages, such as epsfig.[1]

Please also ensure that your document will compile with PDFLATEX. If you have an error message that's puzzling you, first check for it at the UK TUG FAQ http://www.tex.ac.uk/cgi-bin/texfaq2ht If that doesn't help, create a minimal working example (see http://theoval.cmp.uea.ac.uk/~nlct/latex/min and post to somewhere like TeX on StackExchange (http://tex.stackexchange.com/) or the LaTeX Community Forum (http://www.latex-community.org/forum/).

NOTE:
This is an numbered theorem-like environment that was defined in this document's preamble.

1.1. Sub-sections

Sub-sections are produced using `\subsection`.

1.1.1. SUB-SUB-SECTIONS

Sub-sub-sections are produced using `\subsubsection`.

Sub-sub-sub-sections Sub-sub-sub-sections are produced using `\paragraph`. These are unnumbered with a running head.

Sub-sub-sub-sub-sections Sub-sub-sub-sub-sections are produced using `\subparagraph`. These are unnumbered with a running head.

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1. See http://www.ctan.org/pkg/l2tabu

2. Cross-Referencing

Always use `\label` and `\ref` (or one of the commands described below) when cross-referencing. For example, the next section is Section 3. The jmlr class provides some convenient cross-referencing commands: `\sectionref`, `\equationref`, `\tableref`, `\figureref`, `\algorithmref`, `\theoremref`, `\lemmaref`, `\remarkref`, `\corollaryref`, `\definitionref`, `\conjectureref`, `\axiomref`, `\exampleref` and `\appendixref`. The argument of these commands may either be a single label or a comma-separated list of labels. Examples:

Referencing sections: Section 3 or Sections 1 and 3 or Sections 1, 3, 5.1 and 5.2.

Referencing equations: Equation (1) or Equations (1) and (3) or Equations (1), (2), (3) and (4).

Referencing tables: Table 1 or Tables 1 and 2 or Tables 1, 2 and 3.

Referencing figures: Figure 1 or Figures 1 and 2 or Figures 1, 2 and 3 or Figures 3(a) and 3(b).

Referencing algorithms: Algorithm 1 or Algorithms 1 and 2 or Algorithms 1, 2 and 3.

Referencing theorem-like environments: Theorem 1, Lemma 2, Remark 3, Corollary 4, Definition 5, Conjecture 6, Axiom 7 and Example 1.

Referencing appendices: Appendix A or Appendices A and B.

3. Equations

The jmlr class loads the amsmath package, so you can use any of the commands and environments defined there. (See the amsmath documentation for further details.[2])

Unnumbered single-lined equations should be displayed using `\[` and `\]`. For example:

$$E = mc^2$$

Numbered single-line equations should be displayed using the `equation` environment. For example:

$$\cos^2 \theta + \sin^2 \theta \equiv 1 \tag{1}$$

This can be referenced using `\label` and `\equationref`. For example, Equation (1).

Multi-lined numbered equations should be displayed using the `align` environment.[3] For example:

$$f(x) = x^2 + x \tag{2}$$
$$f'(x) = 2x + 1 \tag{3}$$

Unnumbered multi-lined equations should be displayed using the `align*` environment. For example:

$$f(x) = (x+1)(x-1)$$
$$= x^2 - 1$$

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2. Either `texdoc amsmath` or http://www.ctan.org/pkg/amsmath

3. For reasons why you shouldn't use the obsolete `eqnarray` environment, see Lars Madsen, *Avoid eqnarray!* TUGboat 33(1):21–25, 2012.

If you want to mix numbered with unnumbered lines use the align environment and suppress unwanted line numbers with `\nonumber`. For example:

$$
\begin{aligned}
y &= x^2 + 3x - 2x + 1 \\
&= x^2 + x + 1
\end{aligned}
\tag{4}
$$

An equation that is too long to fit on a single line can be displayed using the `split` environment. Text can be embedded in an equation using `\text` or `\intertext` (as used in Theorem 1). See the `amsmath` documentation for further details.

3.1. Operator Names

Predefined operator names are listed in Table 1. For additional operators, either use `\operatorname`, for example $\mathrm{var}(X)$ or declare it with `\DeclareMathOperator`, for example

`\DeclareMathOperator{\var}{var}`

and then use this new command. If you want limits that go above and below the operator (like `\sum`) use the starred versions (`\operatorname*` or `\DeclareMathOperator*`).

Table 1: Predefined Operator Names (taken from `amsmath` documentation)

`\arccos`	arccos	`\deg`	deg	`\lg`	lg	`\projlim`	proj lim
`\arcsin`	arcsin	`\det`	det	`\lim`	lim	`\sec`	sec
`\arctan`	arctan	`\dim`	dim	`\liminf`	lim inf	`\sin`	sin
`\arg`	arg	`\exp`	exp	`\limsup`	lim sup	`\sinh`	sinh
`\cos`	cos	`\gcd`	gcd	`\ln`	ln	`\sup`	sup
`\cosh`	cosh	`\hom`	hom	`\log`	log	`\tan`	tan
`\cot`	cot	`\inf`	inf	`\max`	max	`\tanh`	tanh
`\coth`	coth	`\injlim`	inj lim	`\min`	min		
`\csc`	csc	`\ker`	ker	`\Pr`	Pr		
		`\varlimsup`	$\overline{\lim}$	`\varinjlim`	$\varinjlim$		
		`\varliminf`	$\underline{\lim}$	`\varprojlim`	$\varprojlim$		

4. Vectors and Sets

Vectors should be typeset using `\vec`. For example $\boldsymbol{x}$. The jmlr class also provides `\set` to typeset a set. For example $\mathcal{S}$.

5. Floats

Floats, such as figures, tables and algorithms, are moving objects and are supposed to float to the nearest convenient location. Please don't force them to go in a particular place. In general it's best to use the `htbp` specifier and don't put the figure or table in the middle of a paragraph (that is make sure there's a paragraph break above and below the float).

Floats are supposed to have a little extra space above and below them to make them stand out from the rest of the text. This extra spacing is put in automatically and shouldn't need modifying.

To ensure consistency, please *don't* try changing the format of the caption by doing something like:

```
\caption{\textit{A Sample Caption.}}
```

or

```
\caption{\em A Sample Caption.}
```

You can, of course, change the font for individual words or phrases, for example:

```
\caption{A Sample Caption With Some \emph{Emphasized Words}.}
```

5.1. Tables

Tables should go in the `table` environment. Within this environment use `\floatconts` (defined by jmlr) to set the caption correctly and center the table contents.

Table 2: An Example Table

Dataset	Result
Data1	0.12345
Data2	0.67890
Data3	0.54321
Data4	0.09876

If you want horizontal rules you can use the booktabs package which provides the commands `\toprule`, `\midrule` and `\bottomrule`. For example, see Table 3.

Table 3: A Table With Horizontal Lines

Dataset	Result
Data1	0.12345
Data2	0.67890
Data3	0.54321
Data4	0.09876

If you want vertical lines as well, you can't use the booktabs commands as there'll be some unwanted gaps. Instead you can use LaTeX's `\hline`, but the rows may appear a bit cramped. You can add extra space above or below a row using `\abovestrut` and `\belowstrut`. For example, see Table 4.

Table 4: A Table With Horizontal and Vertical Lines

Dataset	Result
Data1	0.12345
Data2	0.67890
Data3	0.54321
Data4	0.09876

If you want to align numbers on their decimal point, you can use the siunitx package. For example, see Table 5. For further details see the siunitx documentation[4].

Table 5: A Table With Numbers Aligned on the Decimal Point

Dataset	Result
Data1	0.123 45
Data2	10.6789
Data3	50.543
Data4	200.098 76

If the table is too wide, you can adjust the inter-column spacing by changing the value of \tabcolsep. For example:

```
\setlength{\tabcolsep}{3pt}
```

If the table is very wide but not very long, you can use the sidewaystable environment defined in the rotating package (so use \usepackage{rotating}). If the table is too long to fit on a page, you should use the longtable environment defined in the longtable package (so use \usepackage{longtable}).

5.2. Figures

Figures should go in the figure environment. Within this environment, use \floatconts to correctly position the caption and center the image. Use \includegraphics for external graphics files but omit the file extension. Do not use \epsfig or \psfig. If you want to scale the image, it's better to use a fraction of the line width rather than an explicit length. For example, see Figure 1.

Figure 1: Example Image

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4. Either `texdoc siunitx` or http://www.ctan.org/pkg/siunitx

If your image is made up of LaTeX code (for example, commands provided by the `pgf` package) you can include it using `\includeteximage` (defined by the `jmlr` class). This can be scaled and rotated in the same way as `\includegraphics`. For example, see Figure 2.

Figure 2: Image Created Using LaTeX Code

If the figure is too wide to fit on the page, you can use the `sidewaysfigure` environment defined in the `rotating` package.

Don't use `\graphicspath`. If the images are contained in a subdirectory, specify this when you include the image, for example `\includegraphics{figures/mypic}`.

5.2.1. Sᴜʙ-Fɪɢᴜʀᴇs

Sub-figures can be created using `\subfigure`, which is defined by the `jmlr` class. The optional argument allows you to provide a subcaption. The label should be placed in the mandatory argument of `\subfigure`. You can reference the entire figure, for example Figure 3, or you can reference part of the figure using `\figureref`, for example Figure $3(a)$. Alternatively you can reference the subfigure using `\subfigref`, for example (a) and (b) in Figure 3.

(a) A
Cir-
cle

(b) A
Square

Figure 3: An Example With Sub-Figures.

By default, the sub-figures are aligned on the baseline. This can be changed using the second optional argument of `\subfigure`. This may be `t` (top), `c` (centered) or `b` (bottom). For example, the subfigures (a) and (b) in Figure 4 both have `[c]` as the second optional argument.

(a) A
Small
Cir-
cle

(b) A
Square

Figure 4: Another Example With Sub-Figures.

Dataset	Without oversampled set — All members					Without oversampled set — Reduced members					With oversampled set — All members					With oversampled set — Reduced members					Full — OS	US	Full
	REG	WEI	CON	NOR	NC	REG	WEI	CON	NOR	NC	REG	WEI	CON	NOR	NC	REG	WEI	CON	NOR	NC	OS	US	Full
ecoli-0-1-3-7-vs-2-6	.198	.198	.198	.192	.192	.198	.198	.198	.192	.191	.197	.196	.196	.182	.182	.198	.198	.198	.191	.191	.173	.190	.183
ecoli4	.124	.089	.123	.094	.094	.138	.116	.118	.072	.074	.100	.099	.097	.090	.087	.097	.099	.101	.073	.078	.122	.035	.115
glass-0-1-6-vs-2	.068	.067	.068	.090	.090	.076	.077	.077	.079	.079	.067	.068	.068	.078	.078	.079	.077	.077	.079	.079	.062	.064	.058

Table 6: Balanced accuracy scores obtained using GNB as a base classifier

	Without oversampled set										With oversampled set										Full			Dataset
	All members					Reduced members					All members					Reduced members					OS	US	Full	
	REG	WEI	CON	NOR	NC	REG	WEI	CON	NOR	NC	REG	WEI	CON	NOR	NC	REG	WEI	CON	NOR	NC				
ecoli-0-1-3-7-vs-2-6	.187	.187	.192	.183	.188	.187	.185	.181	.183	.181	.186	.186	.190	.192	.190	.184	.186	.186	.186	.180	.192	.148	.200	ecoli-0-1-3-7-vs-2-6
ecoli4	.021	.021	.024	.048	.047	.019	.019	.019	.021	.021	.038	.038	.044	.046	.060	.016	.016	.018	.047	.047	.062	.016	.122	ecoli4
glass-0-1-6-vs-2	.047	.047	.051	.047	.043	.043	.043	.049	.041	.043	.053	.075	.047	.073	.111	.073	.069	.087	.062	.064	.077	.063	.068	glass-0-1-6-vs-2

Table 7: Balanced accuracy scores obtained using KNN as a base classifier

| Without oversampled set | | | | | | | | | | With oversampled set | | | | | | | | | | Full | | | Dataset |
| All members | | | | | Reduced members | | | | | All members | | | | | Reduced members | | | | | | | | |
REG	WEI	CON	NOR	NC	REG	WEI	CON	NOR	NC	REG	WEI	CON	NOR	NC	REG	WEI	CON	NOR	NC	Full	US	OS	
.164	.164	.165	.213	.213	.175	.175	.175	.183	.183	.219	.194	.194	.211	.213	.175	.177	.177	.176	.176	.179	.111	.193	*ecoli-0-1-3-7-vs-2-6*
.051	.051	.050	.059	.059	.046	.045	.045	.081	.081	.057	.060	.060	.091	.092	.046	.046	.046	.072	.072	.119	.050	.136	*ecoli4*
.143	.143	.143	.120	.120	.120	.134	.134	.113	.113	.149	.162	.127	.090	.092	.120	.120	.120	.031	.031	.071	.048	.124	*glass-0-1-6-vs-2*

Table 8: Balanced accuracy scores obtained using DTC as a base classifier

5.3. Sub-Tables

There is an analogous command \subtable for sub-tables. It has the same syntax as \subfigure described above. You can reference the table using \tableref, for example Table 9 or you can reference part of the table, for example Table 9(a). Alternatively you can reference the subtable using \subtabref, for example (a) and (b) in Table 9.

Table 9: An Example With Sub-Tables

(a)			(b)	
A	**B**		**C**	**D**
1	2		3	4
			5	6

By default, the sub-tables are aligned on the top. This can be changed using the second optional argument of \subtable. This may be t (top), c (centered) or b (bottom). For example, the sub-tables (a) and (b) in Table 10 both have [c] as the second optional argument.

Table 10: Another Example With Sub-Tables

			(b)	
(a)			**C**	**D**
A	**B**		3	4
1	2		5	6

5.4. Algorithms

Enumerated textual algorithms can be displayed using the algorithm environment. Within this environment, use use an enumerate or nested enumerate environments. For example, see Algorithm 1. Note that algorithms float like figures and tables.

Algorithm 1: The Gauss-Seidel Algorithm
---

1. For $k = 1$ to maximum number of iterations

    (a) For $i = 1$ to n

        i. $x_i^{(k)} = \frac{b_i - \sum_{j=1}^{i-1} a_{ij} x_j^{(k)} - \sum_{j=i+1}^{n} a_{ij} x_j^{(k-1)}}{a_{ii}}$

        ii. If $\|\boldsymbol{x}^{(k)} - \boldsymbol{x}^{(k-1)} < \epsilon\|$, where ϵ is a specified stopping criteria, stop.

You can use \caption and \label without using \floatconts (as in Algorithm 2).

If you'd rather have the same numbering throughout the algorithm but still want the convenient indentation of nested **enumerate** environments, you can use the **enumerate*** environment provided by the jmlr class. For example, see Algorithm 2.

Algorithm 2: Moore's Shortest Path

Given a connected graph G, where the length of each edge is 1:

1. Set the label of vertex s to 0

2. Set $i = 0$

    3. Locate all unlabelled vertices adjacent to a vertex labelled i and label them $i + 1$

    4. If vertex t has been labelled,

        the shortest path can be found by backtracking, and the length is given by the label of t.

    otherwise

        increment i and return to step 3

Pseudo code can be displayed using the **algorithm2e** environment. This is defined by the algorithm2e package (which is automatically loaded) so check the algorithm2e documentation for further details.[5] For an example, see Algorithm 3.

Algorithm 3: Computing Net Activation

Input: $x_1, \ldots, x_n, w_1, \ldots, w_n$
Output: y, the net activation
$y \leftarrow 0$;
for $i \leftarrow 1$ **to** n **do**
   | $y \leftarrow y + w_i * x_i$;
end

---

6. Description Lists

The jmlr class also provides a description-like environment called **altdescription**. This has an argument that should be the widest label in the list. Compare:

add A method that adds two variables.

differentiate A method that differentiates a function.

with

    add   A method that adds two variables.

    differentiate   A method that differentiates a function.

---

5. Either `texdoc algorithm2e` or http://www.ctan.org/pkg/algorithm2e

7. Theorems, Lemmas etc

The following theorem-like environments are predefined by the jmlr class: `theorem`, `example`, `lemma`, `proposition`, `remark`, `corollary`, `definition`, `conjecture` and `axiom`. You can use the `proof` environment to display the proof if need be, as in Theorem 1.

Theorem 1 (Eigenvalue Powers) *If λ is an eigenvalue of $\boldsymbol{B}$ with eigenvector $\boldsymbol{\xi}$, then λ^n is an eigenvalue of $\boldsymbol{B}^n$ with eigenvector $\boldsymbol{\xi}$.*

Proof *Let λ be an eigenvalue of $\boldsymbol{B}$ with eigenvector ξ, then*

$$\boldsymbol{B}\boldsymbol{\xi} = \lambda\boldsymbol{\xi}$$

premultiply by $\boldsymbol{B}$:

$$\boldsymbol{B}\boldsymbol{B}\boldsymbol{\xi} = \boldsymbol{B}\lambda\boldsymbol{\xi}$$
$$\Rightarrow \boldsymbol{B}^2\boldsymbol{\xi} = \lambda\boldsymbol{B}\boldsymbol{\xi}$$
$$= \lambda\lambda\boldsymbol{\xi} \qquad \text{since } \boldsymbol{B}\boldsymbol{\xi} = \lambda\boldsymbol{\xi}$$
$$= \lambda^2\boldsymbol{\xi}$$

Therefore true for $n = 2$. Now assume true for $n = k$:

$$\boldsymbol{B}^k\boldsymbol{\xi} = \lambda^k\boldsymbol{\xi}$$

premultiply by $\boldsymbol{B}$:

$$\boldsymbol{B}\boldsymbol{B}^k\boldsymbol{\xi} = \boldsymbol{B}\lambda^k\boldsymbol{\xi}$$
$$\Rightarrow \boldsymbol{B}^{k+1}\boldsymbol{\xi} = \lambda^k\boldsymbol{B}\boldsymbol{\xi}$$
$$= \lambda^k\lambda\boldsymbol{\xi} \qquad \text{since } \boldsymbol{B}\boldsymbol{\xi} = \lambda\boldsymbol{\xi}$$
$$= \lambda^{k+1}\boldsymbol{\xi}$$

Therefore true for $n = k + 1$. Therefore, by induction, true for all n. ■

Lemma 2 (A Sample Lemma) *This is a lemma.*

Remark 3 (A Sample Remark) *This is a remark.*

Corollary 4 (A Sample Corollary) *This is a corollary.*

Definition 5 (A Sample Definition) *This is a definition.*

Conjecture 6 (A Sample Conjecture) *This is a conjecture.*

Axiom 7 (A Sample Axiom) *This is an axiom.*

Example 1 (An Example) *This is an example.*

8. Color vs Grayscale

It's helpful if authors supply grayscale versions of their images in the event that the article is to be incorporated into a black and white printed book. With external PDF, PNG or JPG graphic files, you just need to supply a grayscale version of the file. For example, if the file is called `myimage.png`, then the gray version should be `myimage-gray.png` or `myimage-gray.pdf` or `myimage-gray.jpg`. You don't need to modify your code. The jmlr class checks for the existence of the grayscale version if it is print mode (provided you have used `\includegraphics` and haven't specified the file extension).

You can use `\ifprint` to determine which mode you are in. For example, in Figure 1, the purple ellipse represents an input and the yellow ellipse represents an output. Another example: important text!

You can use the class option `gray` to see how the document will appear in gray scale mode. Colored text will automatically be converted to gray scale.

The jmlr class loads the xcolor package, so you can also define your own colors. For example: XYZ.

The xcolor class is loaded with the `x11names` option, so you can use any of the x11 predefined colors (listed in the xcolor documentation[6]).

9. Citations and Bibliography

The jmlr class automatically loads natbib. This sample file has the citations defined in the accompanying BibTeX file `jmlr-sample.bib`. For a parenthetical citation use `\citep`. For example (**?**). For a textual citation use `\citet`. For example **?**. Both commands may take a comma-separated list, for example **??**.

These commands have optional arguments and have a starred version. See the natbib documentation for further details.[7]

The bibliography is displayed using `\bibliography`.

Acknowledgments

Acknowledgements go here.

References

Appendix A. First Appendix

This is the first appendix.

Appendix B. Second Appendix

This is the second appendix.

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6. either `texdoc xcolor` or http://www.ctan.org/pkg/xcolor
7. Either `texdoc natbib` or http://www.ctan.org/pkg/natbib