

When a rotation is performed:

→ root of the tree may change

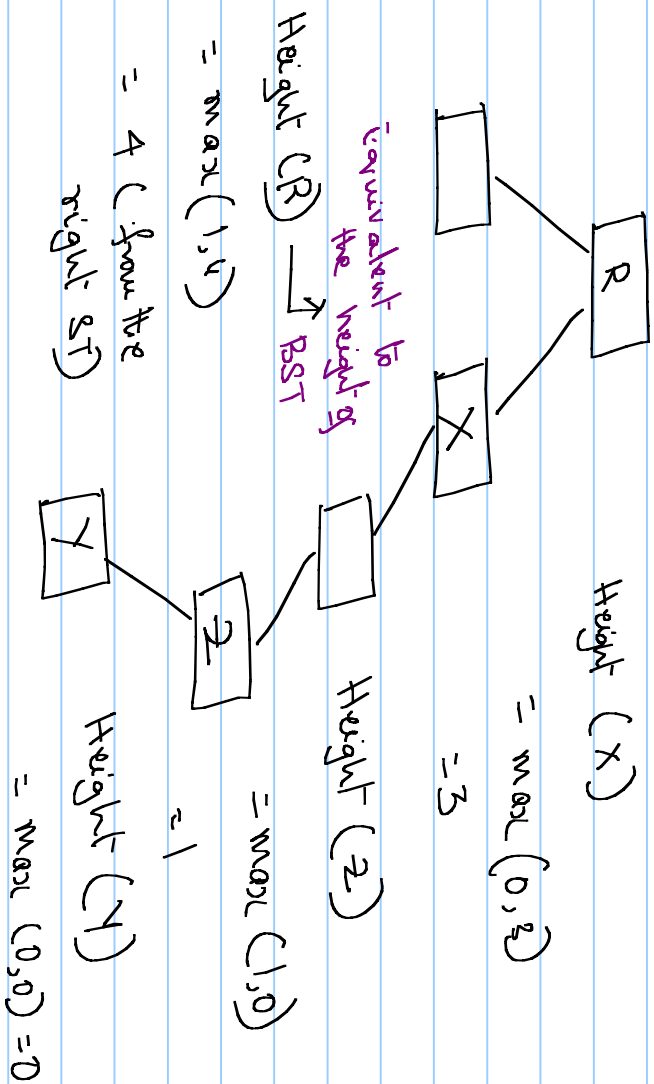
→ child nodes may get new parents

ST2 (260) → parent = Y (280)

ST2 (260) → parent = X (200)

(if parent maintained, adjustment of parent must be done)

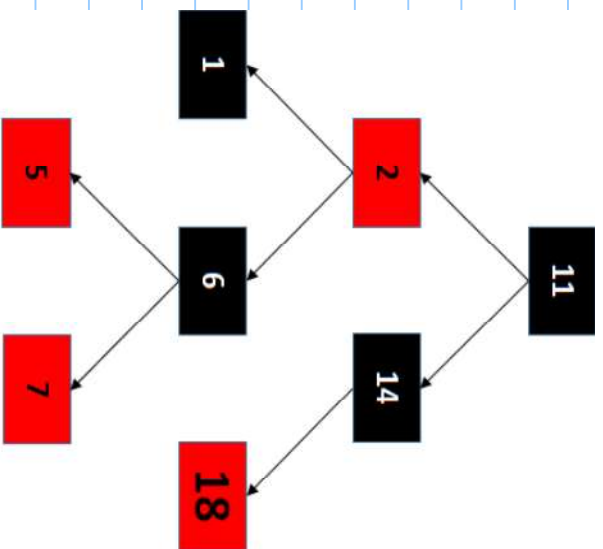
Height of a tree



Algorithm will return 1

$$1 + \max(\text{left subtree}) = 1$$

$$1 + (\max(\text{left subtree}) = \text{NULL}) = 2$$



Red-black tree

↳ the node has an additional property of color of node

typedef struct rbnode {

int key;

struct rbnode * left;

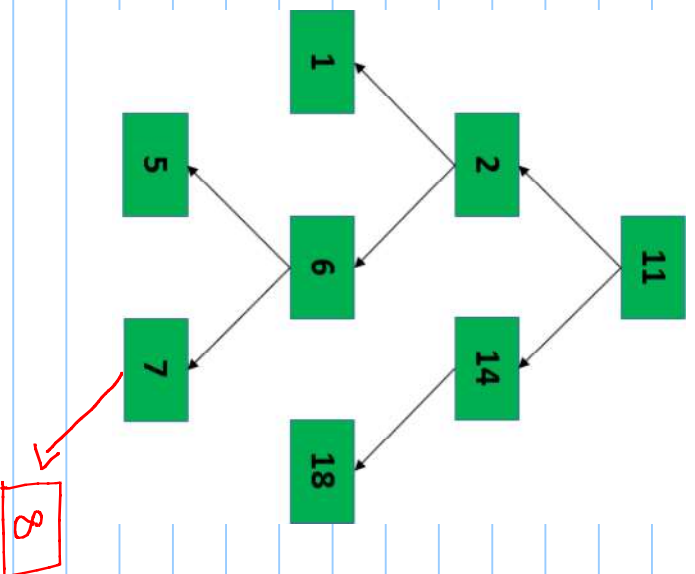
" " * right;

" " * parent;

" " int color; // char color[10];

};

↳ this is important property of red-black tree



Balance factor

$$bf(\text{root}) = bf(11) = \text{height}(14) - \text{height}(2)$$

$$= 1 - 2$$

$$= -1 \checkmark$$

$$bf(6) = \text{height}(5) - \text{height}(7)$$

$$0 - 0$$

$$= 0 \checkmark$$

if balance factor is $> 1 \rightarrow$ left rotation
 if balance factor is $< -1 \rightarrow$ right rotation