

# PROBABILITY

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**13.1.11** <sup>1</sup> A fair die is rolled. Consider events  $E=1,3,5$   $F=2,3$  and  $G=2,3,4,5$ . Find

- (a)  $\Pr(E | F)$  and  $\Pr(F | E)$
- (b)  $\Pr(E | G)$  and  $\Pr(G | E)$
- (c)  $\Pr(E \cup F | G)$  and  $\Pr(E \cap F | G)$

**Solution:**

Event	Probability
$\Pr(E)$	$\frac{1}{2}$
$\Pr(F)$	$\frac{1}{3}$
$\Pr(G)$	$\frac{2}{3}$
$\Pr(EF)$	$\frac{1}{6}$
$\Pr(EG)$	$\frac{1}{3}$
$\Pr(FG)$	$\frac{1}{3}$
$\Pr(EFG)$	$\frac{1}{6}$

Table 13.1.3.2: Probability of Events.

- (a)  $\Pr(E | F)$  and  $\Pr(F | E)$

$$\Pr(E | F) = \frac{\Pr(EF)}{\Pr(F)} \quad (13.1.1.1)$$

$$= \frac{\frac{1}{6}}{\frac{1}{3}} \quad (13.1.1.2)$$

$$= \frac{1}{2} \quad (13.1.1.3)$$

$$\Pr(F | E) = \frac{\Pr(FE)}{\Pr(E)} \quad (13.1.1.4)$$

$$= \frac{\frac{1}{6}}{\frac{1}{2}} \quad (13.1.1.5)$$

$$= \frac{1}{3} \quad (13.1.1.6)$$

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<sup>1</sup>Read question numbers as (CHAPTER NUMBER).(EXERCISE NUMBER).(QUESTION NUMBER)

(b)  $\Pr(E \mid G)$  and  $\Pr(G \mid E)$

$$\Pr(E \mid G) = \frac{\Pr(EG)}{\Pr(G)} \quad (13.1.2.7)$$

$$= \frac{\frac{1}{3}}{\frac{2}{3}} \quad (13.1.2.8)$$

$$= \frac{1}{2} \quad (13.1.2.9)$$

$$\Pr(G \mid E) = \frac{\Pr(GE)}{\Pr(E)} \quad (13.1.2.10)$$

$$= \frac{\frac{1}{3}}{\frac{1}{2}} \quad (13.1.2.11)$$

$$= \frac{2}{3} \quad (13.1.2.12)$$

(c)  $\Pr(E \cup F \mid G)$  and  $\Pr(E \cap F \mid G)$

$$\Pr(E + F \mid G) = \frac{\Pr((E + F)G)}{\Pr(G)} \quad (13.1.3.13)$$

$$= \frac{\Pr(EG + FG)}{\Pr(G)} \quad (13.1.3.14)$$

$$= \frac{\Pr(EG) + \Pr(FG) - \Pr(EFG)}{\Pr(G)} \quad (13.1.3.15)$$

$$= \frac{3}{4} \quad (13.1.3.16)$$

$$\Pr(EF \mid G) = \frac{\Pr(EFG)}{\Pr(G)} \quad (13.1.3.17)$$

$$= \frac{1}{4} \quad (13.1.3.18)$$