

## MATRIX : CONIC ASSIGNMENT

### 0.1 Problem:

Find the area between the curves  $y = x$  and  $y = x^2$ .

### 0.2 Solution:

#### Input Parameters :

Curve Equation :  $y = x^2$ .

Line Equation :  $y = x$ .

#### To Find :

1. Comparing the given curve equation with the standard equation of the conics and finding its parameters.
2. Finding the required parameters for the line equation.
3. Finding the Point of Intersection of the to the curve.
4. Finding the area between the curve.

#### Step - 1 :

Curve Equation :  $y = x^2$ .

The standard equation of the conics is given as :

$$\mathbf{x}^T \mathbf{V} \mathbf{x} + 2\mathbf{u}^T \mathbf{x} + f = 0 \quad (1)$$

The given curve can be expressed as conics with parameters

$$\mathbf{V} = \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix}, \mathbf{u} = \begin{pmatrix} 0 \\ -\frac{1}{2} \end{pmatrix}, f = 0 \quad (2)$$

#### Step - 2 :

Line Equation :  $y = x$ .

From the above line equation below vectors are taken

$$\mathbf{q} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \mathbf{m} = \begin{pmatrix} 1 \\ 1 \end{pmatrix} \quad (3)$$

#### Step - 3 :

The points of intersection of the line,

$$L : \mathbf{x} = \mathbf{q} + \mu \mathbf{m} \quad \mu \in \mathbb{R} \quad (4)$$

with the conic section,

$$\mathbf{x}^T \mathbf{V} \mathbf{x} + 2\mathbf{u}^T \mathbf{x} + f = 0 \quad (5)$$

are given by

$$\mathbf{x}_i = \mathbf{q} + \mu_i \mathbf{m} \quad (6)$$

where,

$$\mu_i = \frac{1}{\mathbf{m}^T \mathbf{V} \mathbf{m}} \left( -\mathbf{m}^T (\mathbf{V} \mathbf{q} + \mathbf{u}) \pm \sqrt{[\mathbf{m}^T (\mathbf{V} \mathbf{q} + \mathbf{u})]^2 - (\mathbf{q}^T \mathbf{V} \mathbf{q} + 2\mathbf{u}^T \mathbf{q} + f) (\mathbf{m}^T \mathbf{V} \mathbf{m})} \right) \quad (7)$$

On substituting  $\mathbf{V}, \mathbf{q}, \mathbf{m}$  in the above equation, we get the values of  $\mu$ . By substituting the values of  $\mu$  in eq(6), we get the points of intersection of line with the given curve.

*i.e.,*  $\mathbf{x}_1, \mathbf{x}_2$

$$\therefore \mathbf{x}_1 = \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \mathbf{x}_2 = \begin{pmatrix} 1 \\ 1 \end{pmatrix} \quad (8)$$

#### Step - 4 :

The area bounded by the curve  $y = x^2$  and line  $y = x$  is given by

$$\Rightarrow A = \int_0^1 [x] dx \quad (9)$$

$$\Rightarrow A = \frac{x^2}{2} \quad (10)$$

By solving we get the required area  
 $\therefore A = \frac{1}{6}$

### 0.3 Termux Commands :

bash rncm.sh ..... Using Shell commands.

### 0.4 Plot :

