

•True random numbers generators

Several sources of randomness – natural sources of randomness

- decay times of radioactive materials
- electrical noise from a resistor or semiconductor
- radio channel or audible noise
- keyboard timings
- disk electrical activity
- mouse movements
- Physical unclonable function (PUF)
- Some are better than others

Combining sources of randomness

•Suppose r_1, r_2, \dots, r_k are random numbers from different sources. E.g.,

r_1 = electrical noise from a resistor or semiconductor

r_2 = sample of hip-hop music on radio

r_3 = clock on computer

$b = r_1 \oplus r_2 \oplus \dots \oplus r_k$

If any one of r_1, r_2, \dots, r_k is truly random, then so is b

Many poor sources + 1 good source = good entropy

Pseudorandom Number Generators (PRNGs)

- True randomness is expensive
- **Pseudorandom number generator (PRNGs)**: An algorithm that uses a little bit of true randomness to generate a lot of random-looking output
- Also called **deterministic random bit generators (DRBGs)**
- PRNGs are deterministic: Output is generated according to a set algorithm
- However, for an attacker who can't see the internal state, the output is *computationally indistinguishable* from true randomness

PRNG: Definition

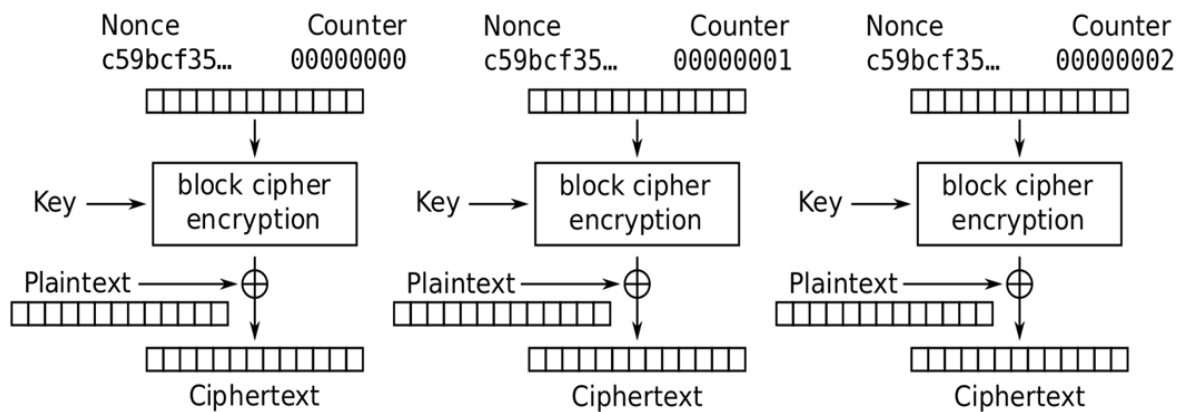
- A PRNG has two functions:
 - PRNG.Seed(randomness): Initializes the internal state using the entropy
Input: Some truly random bits
 - PRNG.Generate(n): Generate n pseudorandom bits
Input: A number n
Output: n pseudorandom bits
Updates the internal state as needed

Properties

- **Correctness**: Deterministic
- **Efficiency**: Efficient to generate pseudorandom bits
- **Security**: Indistinguishability from random
- **Rollback resistance**: cannot deduce anything about any previously-generated bit

Example construction of PRNG

- Using block cipher in Counter (CTR) mode:
- If you want m random bits, and a block cipher with E_k has n bits, apply the block cipher m/n times and concatenate the result:
- $\text{PRNG.Seed}(K \parallel IV) = E_k(IV, 1) \parallel E_k(IV, 2) \parallel E_k(IV, 3) \dots E_k(IV, \text{ceil}(m/n))$,
- \parallel is concatenation
- Initialization vector (IV) / Nonce – typically is random or pseudorandom
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Counter (CTR) mode encryption

PRNG: Security

- Can we design a PRNG that is truly random?
- A PRNG cannot be truly random
- The output is deterministic given the initial seed
- A secure PRNG is computationally indistinguishable from random to an attacker
- Game: Present an attacker with a truly random sequence and a sequence outputted from a secure PRNG
- An attacker should be able to determine which is which with probability ≈ 0
- Equivalence: An attacker cannot predict future output of the PRNG
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Create pseudorandom numbers

- Truly random numbers are impossible with any program!
- However, we can generate seemingly random numbers, called pseudorandom numbers
- The function `rand()` returns a non-negative number between 0 and `RAND_MAX`
- For C, it is defined in `stdlib.h`

PRNGs: Summary

- True randomness requires sampling a physical process
- PRNG: An algorithm that uses a little bit of true randomness to generate a lot of random-looking output
- Seed(entropy): Initialize internal state
- Generate(n): Generate n bits of pseudorandom output
- Security: computationally indistinguishable from truly random bits
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