

An example with 5x5 matrices which are pair-wise unitarily similar but not S.U.S

It runs for 2 iterations showing that the collection is not S.U.S

Printing salient results of each iteration

The given input collection of p=2, 2-tuples (A\_I,B\_I)

Displaying 2 decimal places

A\_1

0.26 + 0.98j 0.20 + 0.89j 0.28 + 0.65j 0.08 + 0.03j 0.73 + 0.71j  
0.32 + 0.38j 0.53 + 0.78j 0.18 + 0.05j 0.11 + 0.69j 0.33 + 0.81j  
0.48 + 0.38j 0.51 + 0.79j 0.66 + 0.88j 0.67 + 0.69j 0.26 + 1.00j  
0.73 + 0.97j 0.23 + 0.05j 0.99 + 0.08j 0.20 + 0.31j 0.66 + 0.27j  
0.48 + 0.37j 0.32 + 0.36j 0.95 + 0.76j 0.80 + 0.66j 0.61 + 0.04j

B\_1

0.57 + 0.82j 0.40 + 0.72j -0.83 + 0.43j 1.02 + 0.87j -1.10 + 0.05j  
0.88 + -0.03j -0.08 + 0.64j -0.21 + -0.22j 0.63 + -0.27j -0.27 + 0.59j  
0.39 + 0.00j -0.06 + 0.47j 0.30 + 0.39j 0.11 + -0.04j 0.17 + 0.59j  
0.06 + 1.63j 0.17 + 0.86j -0.26 + 0.06j 1.07 + 0.63j -0.45 + -0.17j  
0.21 + -0.77j 0.34 + -1.14j 0.09 + -0.09j -0.07 + -0.68j 0.41 + 0.50j

A\_2

0.20 + 0.89j 0.14 + 0.35j 0.27 + 0.05j 0.62 + 0.31j 0.18 + 0.12j  
0.70 + 0.88j 0.34 + 0.54j 0.25 + 0.96j 0.82 + 0.68j 0.90 + 0.42j  
0.36 + 0.18j 0.14 + 0.29j 0.77 + 0.46j 0.70 + 0.43j 0.52 + 0.30j  
0.90 + 0.97j 0.21 + 0.48j 0.64 + 0.19j 0.54 + 0.49j 0.13 + 0.45j

0.55 + 0.92j 0.97 + 0.16j 0.79 + 0.51j 0.02 + 0.23j 0.17 + 0.27j

B\_2

0.77 + 0.71j -0.52 + -0.63j 0.21 + 0.02j 0.26 + -0.46j -0.45 + -0.08j  
-1.15 + -1.21j 0.68 + 0.90j -0.30 + 0.09j 0.05 + 0.14j 0.56 + -0.89j  
-0.44 + 0.03j -0.11 + 0.18j -0.37 + 0.19j -0.04 + -0.51j -0.37 + -0.31j  
0.66 + 0.16j 0.05 + -0.18j -0.30 + 0.16j -0.06 + -0.04j -0.24 + 0.34j  
0.50 + -1.19j -0.67 + 1.04j -0.47 + 0.56j 0.03 + -0.29j 1.00 + 0.90j

Iteration: 1

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U-Induced Partition: [5]

Not in Pre-Solution form

Please refer Definition 3

Reason:  $A^l_{ii}/B^l_{ii}$ , the l,i,j of  $A^l_{ij}$  which fail's the criterion as follows:

$l = 1, i = 1, j = 1$

$l^{th}$  partitioned matrix of collection from where sub-matrices (S,R) are picked for Diagonalization

A\_1

0.26+0.98j 0.20+0.89j 0.28+0.65j 0.08+0.03j 0.73+0.71j  
0.32+0.38j 0.53+0.78j 0.18+0.05j 0.11+0.69j 0.33+0.81j  
0.48+0.38j 0.51+0.79j 0.66+0.88j 0.67+0.69j 0.26+1.00j  
0.73+0.97j 0.23+0.05j 0.99+0.08j 0.20+0.31j 0.66+0.27j  
0.48+0.37j 0.32+0.36j 0.95+0.76j 0.80+0.66j 0.61+0.04j

B\_1

0.57+0.82j 0.40+0.72j -0.83+0.43j 1.02+0.87j -1.10+0.05j  
0.88+-0.03j -0.08+0.64j -0.21+-0.22j 0.63+-0.27j -0.27+0.59j  
0.39+0.00j -0.06+0.47j 0.30+0.39j 0.11+-0.04j 0.17+0.59j  
0.06+1.63j 0.17+0.86j -0.26+0.06j 1.07+0.63j -0.45+-0.17j  
0.21+-0.77j 0.34+-1.14j 0.09+-0.09j -0.07+-0.68j 0.41+0.50j

S

0.26 + 0.98j 0.20 + 0.89j 0.28 + 0.65j 0.08 + 0.03j 0.73 + 0.71j  
0.32 + 0.38j 0.53 + 0.78j 0.18 + 0.05j 0.11 + 0.69j 0.33 + 0.81j  
0.48 + 0.38j 0.51 + 0.79j 0.66 + 0.88j 0.67 + 0.69j 0.26 + 1.00j  
0.73 + 0.97j 0.23 + 0.05j 0.99 + 0.08j 0.20 + 0.31j 0.66 + 0.27j  
0.48 + 0.37j 0.32 + 0.36j 0.95 + 0.76j 0.80 + 0.66j 0.61 + 0.04j

R

0.57 + 0.82j 0.40 + 0.72j -0.83 + 0.43j 1.02 + 0.87j -1.10 + 0.05j  
0.88 + -0.03j -0.08 + 0.64j -0.21 + -0.22j 0.63 + -0.27j -0.27 + 0.59j  
0.39 + 0.00j -0.06 + 0.47j 0.30 + 0.39j 0.11 + -0.04j 0.17 + 0.59j  
0.06 + 1.63j 0.17 + 0.86j -0.26 + 0.06j 1.07 + 0.63j -0.45 + -0.17j  
0.21 + -0.77j 0.34 + -1.14j 0.09 + -0.09j -0.07 + -0.68j 0.41 + 0.50j

Setting up an Equivalent Problem

U `blocks further', New partition

Refer Theorem 2, Proof item number/s: 1

[1, 1, 1, 1, 1]

Iteration: 2

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U-Induced Partition: [1, 1, 1, 1, 1]

Not in Pre-Solution form

Please refer Definition 3

Reason:  $A^l_{ii}/B^l_{ii}$ , the  $l,i,j$  of  $A^l_{ij}$  which fail's the criterion as follows:

$l = 2, i = 1, j = 1$

$l^{th}$  partitioned matrix of collection from where sub-matrices (S,R) are picked for Diagonalization

A\_2

$$-0.06+0.20j \mid 0.13+0.03j \mid 0.62+-0.20j \mid -0.15+0.32j \mid 0.44+0.41j$$

-----+-----+-----+-----

$$-0.28+0.53j \mid 0.04+0.08j \mid 0.17+-0.22j \mid -0.28+-0.48j \mid 0.93+0.10j$$

-----+-----+-----+-----

$$0.27+-0.17j \mid 0.17+0.55j \mid 0.13+0.35j \mid -0.19+0.04j \mid 0.20+0.12j$$

-----+-----+-----+-----

$$0.30+-0.29j \mid 0.42+0.33j \mid -0.06+-0.34j \mid -0.29+-0.02j \mid 0.55+-0.05j$$

-----+-----+-----+-----

$$-0.07+-0.38j \mid 0.45+0.71j \mid -0.03+0.64j \mid -0.38+-0.43j \mid 2.21+2.05j$$

B\_2

$$1.61+1.71j \mid 0.37+-1.50j \mid -0.35+-0.61j \mid 0.69+0.09j \mid 0.48+0.93j$$

-----+-----+-----+-----

$$-0.16+0.45j \mid 0.31+0.27j \mid -0.53+0.26j \mid -0.48+-0.02j \mid -0.26+0.17j$$

-----+-----+-----+-----

$$-0.08+-0.41j \mid -0.10+0.02j \mid 0.04+0.28j \mid 0.19+-0.10j \mid 0.16+-0.39j$$

-----+-----+-----+-----  
0.01+1.05j | -0.27+0.07j | 0.38+-0.12j | -0.41+0.31j | -0.35+0.07j

-----+-----+-----+-----  
0.93+0.06j | -0.41+0.09j | -0.22+0.10j | 0.49+0.16j | 0.47+0.08j

S

-0.06 + 0.20j

R

1.61 + 1.71j

Setting up an Equivalent Problem

vals\_A

[0.196993025]

vals\_B

[1.709486354]

mults\_A

[1]

mults\_B

[1]

NOT S.U.S

Reason: The eigen-values of (S,R) used for setting up equivalent problem do not match

Refer Theorem 2, Proof item number/s: 1