

An example with 5x5 matrices which are pair-wise unitarily similar but not S.U.S

It runs for 2 iterations showing that the collection is not S.U.S

Printing salient results of each iteration

The given input collection of  $p=2$ , 2-tuples  $(A_l, B_l)$

Displaying 2 decimal places

$A_1$

$0.26 + 0.98j$	$0.20 + 0.89j$	$0.28 + 0.65j$	$0.08 + 0.03j$	$0.73 + 0.71j$
$0.32 + 0.38j$	$0.53 + 0.78j$	$0.18 + 0.05j$	$0.11 + 0.69j$	$0.33 + 0.81j$
$0.48 + 0.38j$	$0.51 + 0.79j$	$0.66 + 0.88j$	$0.67 + 0.69j$	$0.26 + 1.00j$
$0.73 + 0.97j$	$0.23 + 0.05j$	$0.99 + 0.08j$	$0.20 + 0.31j$	$0.66 + 0.27j$
$0.48 + 0.37j$	$0.32 + 0.36j$	$0.95 + 0.76j$	$0.80 + 0.66j$	$0.61 + 0.04j$

$B_1$

$0.57 + 0.82j$	$0.40 + 0.72j$	$-0.83 + 0.43j$	$1.02 + 0.87j$	$-1.10 + 0.05j$
$0.88 + -0.03j$	$-0.08 + 0.64j$	$-0.21 + -0.22j$	$0.63 + -0.27j$	$-0.27 + 0.59j$
$0.39 + 0.00j$	$-0.06 + 0.47j$	$0.30 + 0.39j$	$0.11 + -0.04j$	$0.17 + 0.59j$
$0.06 + 1.63j$	$0.17 + 0.86j$	$-0.26 + 0.06j$	$1.07 + 0.63j$	$-0.45 + -0.17j$
$0.21 + -0.77j$	$0.34 + -1.14j$	$0.09 + -0.09j$	$-0.07 + -0.68j$	$0.41 + 0.50j$

$A_2$

$0.20 + 0.89j$	$0.14 + 0.35j$	$0.27 + 0.05j$	$0.62 + 0.31j$	$0.18 + 0.12j$
$0.70 + 0.88j$	$0.34 + 0.54j$	$0.25 + 0.96j$	$0.82 + 0.68j$	$0.90 + 0.42j$
$0.36 + 0.18j$	$0.14 + 0.29j$	$0.77 + 0.46j$	$0.70 + 0.43j$	$0.52 + 0.30j$
$0.90 + 0.97j$	$0.21 + 0.48j$	$0.64 + 0.19j$	$0.54 + 0.49j$	$0.13 + 0.45j$

$0.55 + 0.92j$   $0.97 + 0.16j$   $0.79 + 0.51j$   $0.02 + 0.23j$   $0.17 + 0.27j$

B\_2

$0.77 + 0.71j$   $-0.52 + -0.63j$   $0.21 + 0.02j$   $0.26 + -0.46j$   $-0.45 + -0.08j$   
 $-1.15 + -1.21j$   $0.68 + 0.90j$   $-0.30 + 0.09j$   $0.05 + 0.14j$   $0.56 + -0.89j$   
 $-0.44 + 0.03j$   $-0.11 + 0.18j$   $-0.37 + 0.19j$   $-0.04 + -0.51j$   $-0.37 + -0.31j$   
 $0.66 + 0.16j$   $0.05 + -0.18j$   $-0.30 + 0.16j$   $-0.06 + -0.04j$   $-0.24 + 0.34j$   
 $0.50 + -1.19j$   $-0.67 + 1.04j$   $-0.47 + 0.56j$   $0.03 + -0.29j$   $1.00 + 0.90j$

Iteration: 1

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U-Induced Partition: [5]

Not in Pre-Solution form

Please refer Definition 3

Reason:  $A_{ii}^{\wedge}/B_{ii}^{\wedge}$ , the  $i,j$  of  $A_{ij}^{\wedge}$  which fail's the criterion as follows:

$i = 1, i = 1, j = 1$

$i$ th partitioned matrix of collection from where sub-matrices (S,R) are picked for Diagonalization

A\_1

$0.26+0.98j$   $0.20+0.89j$   $0.28+0.65j$   $0.08+0.03j$   $0.73+0.71j$   
 $0.32+0.38j$   $0.53+0.78j$   $0.18+0.05j$   $0.11+0.69j$   $0.33+0.81j$   
 $0.48+0.38j$   $0.51+0.79j$   $0.66+0.88j$   $0.67+0.69j$   $0.26+1.00j$   
 $0.73+0.97j$   $0.23+0.05j$   $0.99+0.08j$   $0.20+0.31j$   $0.66+0.27j$   
 $0.48+0.37j$   $0.32+0.36j$   $0.95+0.76j$   $0.80+0.66j$   $0.61+0.04j$

B\_1

0.57+0.82j 0.40+0.72j -0.83+0.43j 1.02+0.87j -1.10+0.05j  
0.88+-0.03j -0.08+0.64j -0.21+-0.22j 0.63+-0.27j -0.27+0.59j  
0.39+0.00j -0.06+0.47j 0.30+0.39j 0.11+-0.04j 0.17+0.59j  
0.06+1.63j 0.17+0.86j -0.26+0.06j 1.07+0.63j -0.45+-0.17j  
0.21+-0.77j 0.34+-1.14j 0.09+-0.09j -0.07+-0.68j 0.41+0.50j

S

0.26 + 0.98j 0.20 + 0.89j 0.28 + 0.65j 0.08 + 0.03j 0.73 + 0.71j  
0.32 + 0.38j 0.53 + 0.78j 0.18 + 0.05j 0.11 + 0.69j 0.33 + 0.81j  
0.48 + 0.38j 0.51 + 0.79j 0.66 + 0.88j 0.67 + 0.69j 0.26 + 1.00j  
0.73 + 0.97j 0.23 + 0.05j 0.99 + 0.08j 0.20 + 0.31j 0.66 + 0.27j  
0.48 + 0.37j 0.32 + 0.36j 0.95 + 0.76j 0.80 + 0.66j 0.61 + 0.04j

R

0.57 + 0.82j 0.40 + 0.72j -0.83 + 0.43j 1.02 + 0.87j -1.10 + 0.05j  
0.88 + -0.03j -0.08 + 0.64j -0.21 + -0.22j 0.63 + -0.27j -0.27 + 0.59j  
0.39 + 0.00j -0.06 + 0.47j 0.30 + 0.39j 0.11 + -0.04j 0.17 + 0.59j  
0.06 + 1.63j 0.17 + 0.86j -0.26 + 0.06j 1.07 + 0.63j -0.45 + -0.17j  
0.21 + -0.77j 0.34 + -1.14j 0.09 + -0.09j -0.07 + -0.68j 0.41 + 0.50j

Setting up an Equivalent Problem

U `blocks further', New partition

Refer Theorem 2, Proof item number/s: 1

[1, 1, 1, 1, 1]

Iteration: 2

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U-Induced Partition: [1, 1, 1, 1, 1]

Not in Pre-Solution form

Please refer Definition 3

Reason:  $A_{ii}/B_{ii}$  , the  $i,j$  of  $A_{ij}$  which fail's the criterion as follows:

$l = 2 , i = 1 , j = 1$

$l$ th partitioned matrix of collection from where sub-matrices (S,R) are picked for Diagonalization

A\_2

-0.06+0.20j | 0.13+0.03j | 0.62+-0.20j | -0.15+0.32j | 0.44+0.41j

-----+-----+-----+-----+-----

-0.28+0.53j | 0.04+0.08j | 0.17+-0.22j | -0.28+-0.48j | 0.93+0.10j

-----+-----+-----+-----+-----

0.27+-0.17j | 0.17+0.55j | 0.13+0.35j | -0.19+0.04j | 0.20+0.12j

-----+-----+-----+-----+-----

0.30+-0.29j | 0.42+0.33j | -0.06+-0.34j | -0.29+-0.02j | 0.55+-0.05j

-----+-----+-----+-----+-----

-0.07+-0.38j | 0.45+0.71j | -0.03+0.64j | -0.38+-0.43j | 2.21+2.05j

B\_2

1.61+1.71j | 0.37+-1.50j | -0.35+-0.61j | 0.69+0.09j | 0.48+0.93j

-----+-----+-----+-----+-----

-0.16+0.45j | 0.31+0.27j | -0.53+0.26j | -0.48+-0.02j | -0.26+0.17j

-----+-----+-----+-----+-----

-0.08+-0.41j | -0.10+0.02j | 0.04+0.28j | 0.19+-0.10j | 0.16+-0.39j

-----+-----+-----+-----+-----

0.01+1.05j | -0.27+0.07j | 0.38+-0.12j | -0.41+0.31j | -0.35+0.07j

-----+-----+-----+-----+-----

0.93+0.06j | -0.41+0.09j | -0.22+0.10j | 0.49+0.16j | 0.47+0.08j

S

-0.06 + 0.20j

R

1.61 + 1.71j

Setting up an Equivalent Problem

vals\_A

[0.196993025]

vals\_B

[1.709486354]

mults\_A

[1]

mults\_B

[1]

NOT S.U.S

Reason: The eigen-values of (S,R) used for setting up equivalent problem do not match

Refer Theorem 2, Proof item number/s: 1