

INSTRUCTIONS: Books, notes, and electronic devices are not permitted. Write (1) **your name**, (2) **1350/EXAM 1**, (3) **lecture number/instructor name** and (4) **FALL 2013** on the front of your blue-book. Also make a **grading table** with room for 4 problems and a total score. **Start each problem on a new page.** Box your answers. A correct answer with incorrect or no supporting work may receive no credit, while an incorrect answer with relevant work may receive partial credit. **SHOW ALL WORK**

1. (3 pts each) **True/False**

- (a) (T/F) If f is undefined at $x = c$, then the limit of $f(x)$ as x approaches c does not exist.
- (b) (T/F) If the limit of $f(x)$ as x approaches c is 0, then there must be a number k such that $f(k) < 0.0001$.
- (c) (T/F) $\lim_{x \rightarrow 0} \sin\left(\frac{|x|}{x}\right) = 0$
- (d) (T/F) If f is an even function and $\lim_{x \rightarrow 2^-} f(x) = 7$ then $\lim_{x \rightarrow -2^-} f(x) = 7$
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2. Evaluate the following: you may not use l'Hospital's Rule, justify your answers (5 points each):

- (a) $\lim_{x \rightarrow 1} \frac{\sin(2x)}{\sin(3x)}$ (b) $\lim_{x \rightarrow 1^+} \frac{\sqrt{2x}(x-1)}{|x-1|}$ (c) $\lim_{x \rightarrow 0} \sqrt{x} \sin\left(\frac{1}{x}\right)$
- (d) $f(b^2 + 1) = ?$ given that $f(x) = \begin{cases} |x| + 1, & \text{if } x < 1 \\ -x + 1, & \text{if } x \geq 1 \end{cases}$
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3. (12 pts) For what value(s) of k is the function $f(x) = \begin{cases} \sin(kx), & \text{if } x \leq 0 \\ 3x, & \text{if } x > 0 \end{cases}$ continuous at $x = 0$.

A complete answer will include the definition of continuity.

4. (10 pts) Show the equation $x + 2\cos(4x) = 0$ has at least one solution. Explain your work.

5. Consider the function $f(x) = \frac{2}{3x+3}$.

- (a) (10 pts) Find the rate of change of $f(x)$ at $x = a$.
- (b) (3 pts) Using part (a) find the rate of change of $f(x)$ at $x = -1$.
- (c) (3 pts) Using part (a) find the rate of change of $f(x)$ at $x = 0$.
- (d) (12 pts) Using the above information find the equation of two different tangent lines that are parallel to the line that goes through the points $(-2, 4)$ and $(-5, 6)$. Write your answer in $y = mx + b$ form.
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6. The function $g(x) = x|x|$ is differentiable everywhere. Show this by

- (a) (5 pts) Define $g(x)$ as a piecewise function.
- (b) (12 pts) Using the definition of the derivative consider the left and right hand limits of the difference quotient at 0.
- (c) (1 pt.) Explain why the function is differentiable everywhere else.