## (Solutions)

## Math 1300-005 - Spring 2017

Linearization and Linear Approximation - 3/14/17

Guidelines: This will not be handed in, but is a study resource for Midterm 3.

1. Find the linearization, L(x), of each of the following functions at the given values of a.

Find the intertration, 
$$L(x)$$
, of each of the following functions at the given value  $f(x) = x^4 + 3x^2$ ,  $a = -1$ 

L(x) =  $f(a) + f'(a)(x-a)$ 

Here  $f(a) = -1$ ,  $f'(x) = U(x^3 + C(x))$ 
 $f'(-1) = U(-1)^3 + C(-1)$ 
 $f'(-1) = U(-1)^3 + C(-1)^3$ 
 $f$ 

(d) 
$$f(x) = x^{3/2}$$
,  $a = 16$   
Here,  $a = 16$ ,  $f'(x) = \frac{3}{4}x^{-1/4}$   
 $f'(16) = (16)^{3/4} = (16)^{1/4} = 2^3 = 8$   
 $f'(16) = \frac{3}{4}(16)^{-1/4} = \frac{3}{4} - \frac{1}{100}$ 

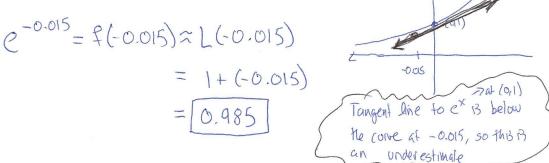
$$L(x) = f(16) + f'(16)(x-16)$$

$$G(x) = 8 + \frac{3}{8}(x-16)$$

- 2. In this problem, we shall estimate  $e^{-0.015}$  using linear approximation. The idea is that -0.015 is very close to 0 and since we know the value of  $e^0 = 1$ , we can use the linearization of  $f(x) = e^x$  at x = 0 to perform the estimate.
  - (a) Let  $f(x) = e^x$ . Find the linearization, L(x), of f at a = 0.

Here 
$$a=0$$
,  $f'(x)=e^{x}$ , so  $L(x)=f(0)+f'(0)(x-a)$   
 $f'(0)=1$   
 $f'(0)=1$   
 $C_{7}$   $L(x)=1+1(x-0)$   
 $C_{7}$   $C_{7}$ 

(b) Use L(x) to estimate  $e^{-0.015}$ . Is this an overestimate or underestimate? Please justify.



- 3. In this problem, we shall estimate  $(8.06)^{2/3}$  using linear approximation. The idea is that 8.06 is very close to 8 and since we know the value of  $8^{2/3} = (8^{1/3})^2 = 4$ , we can use the linearization of  $f(x) = x^{2/3}$  at x = 8 to perform the estimate.
  - (a) Let  $f(x) = x^{2/3}$ . Find the linearization, L(x), of f at a = 8.

$$f'(x) = \frac{2}{3}x^{-1/3}$$

$$f(9) = (8)^{2/3} = (8^{1/3})^2 = 2^2 = 4$$

$$f'(8) = \frac{2}{3}(8)^{-1/3} = \frac{2}{3 \cdot 2} = \frac{1}{3}$$

$$(x) = f(8) + f'(8)(x - 6)$$

$$(x) = f(8) + f'(8)(x - 6)$$

$$(x) = f(8) + f'(8)(x - 6)$$

(b) Use L(x) to estimate  $(8.06)^{2/3}$ . Is this an overestimate or underestimate? Please justify.

