

### hysicsaholics



#### **DPP – 5 (Basic Maths)**

Video Solution on Website:-

https://physicsaholics.com/home/courseDetails/36

Video Solution on YouTube:-

https://youtu.be/LI7UgwqzscY

Written Solution on Website:-

https://physicsaholics.com/note/notesDetalis/70

Q 1. 
$$y = x \ln x$$
, Find  $\frac{dy}{dx}$ ?

(a) 
$$x + \ln x$$

(b) 
$$1 + \ln x$$

(d) 
$$x + x \ln x$$

Q 2. 
$$y = \sin x \cdot \cos x$$
, Find  $\frac{dy}{dx}$ ?

Q3 
$$y = (Sin x + cos x)^2$$
, Find  $\frac{dy}{dx}$ ?

Differentiate  $y = \ln x^2$  w.r.t. 'x': Q4.

(a) 
$$\frac{dy}{dx} = \frac{1}{x}$$

(b) 
$$\frac{\mathrm{d}y}{\mathrm{d}x} = 2$$

 $e^{x^2}$  w.r.t. 'x': Differentiate y Q 5.

(a) 
$$\frac{dy}{dx} = 2xe^{x^2}$$

(b) 
$$\frac{dy}{dx} = e^{x^2}$$

(c) 
$$\frac{dx}{dy} = 2e^x$$

(d) None of these

w.r.t. x'(where a = constant): Differentiate  $y = ae^x$ Q 6.

(a) 
$$\frac{\mathrm{d}y}{\mathrm{d}x} = axe^x$$

(b) 
$$\frac{\mathrm{dy}}{\mathrm{dx}} = a$$

(c) 
$$\frac{dx}{dx} = ae^x$$

(d) None of these

Differentiate  $F(x) = (x^2 - 1)(x + 5)$ , w.r.t. 'x': Q 7.

(a) 
$$F'(x) = 3x^2 + 10x - 1$$
  
(b)  $F'(x) = x^2 - 10x - 1$ 

(b) 
$$F'(x) = x^2 - 10x - 1$$

(c) 
$$F'(x) = (2x)(x)$$

(d) None of these

Q 8. Differentiate  $F(x) = \sin x \cos x$ , w.r.t. 'x':

(a) 
$$F'(x) = 1$$

(b) 
$$F'(x) = \cos^2 x - \sin^2 x$$

(c) 
$$F'(x) = \cos x - \sin x$$

(d) None of these

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Differentiate  $y = x^2 \ln x$  w.r.t. 'x': Q 9.

(a) 
$$\frac{dy}{dx} = x(2 \ln x + 1)$$
  
(c) 
$$\frac{dy}{dx} = x^2 \ln x + 1$$

(b) 
$$\frac{dy}{dx} = \ln x + 2x$$

(c) 
$$\frac{dx}{dx} = x^2 \ln x + 3$$

(d) None of these

Q 10. Differentiate  $y = \frac{e^x}{x}$ , w.r.t. 'x':

$$(a) \frac{\mathrm{dy}}{\mathrm{dx}} = -\frac{e^x}{x^2}$$

(b) 
$$\frac{dy}{dx} = \frac{e^x}{x^2} (x + 1)$$

(a) 
$$\frac{dy}{dx} = -\frac{e^x}{x^2}$$
 (b)  $\frac{dy}{dx} = \frac{e^x}{x^2}(x+1)$  (c)  $\frac{dy}{dx} = \frac{e^x}{x^2}(x-1)$  (d) None of these

Q 11. Differentiate  $y = \frac{\sin x}{\cos x}$ , w.r.t. 'x':

$$(a) \frac{\mathrm{dy}}{\mathrm{dx}} = \cos^2 x$$

(b) 
$$\frac{dy}{dx} = \frac{\cos^2 x - \sin^2 x}{\cos^2 x}$$

(a) 
$$\frac{dy}{dx} = \cos^2 x$$
  
(c)  $\frac{dy}{dx} = \sec^2 x$ 

(d) None of these

Q 12. Differentiate  $y = \frac{x}{\ln x}$ , w.r.t. 'x':

(a) 
$$\frac{dy}{dx} = 1$$

$$(b) \frac{dy}{dx} = \frac{\ln x - 1}{(\ln x)^2}$$

$$(c) \frac{dy}{dx} = \frac{1}{(\ln x)^2}$$

(d) None of these

Q 13. Differentiate  $y = \frac{6x^2}{2-x}$ , w.r.t. 'x

(a)  $\frac{dy}{dx} = \frac{24x - 6x^2}{(2-x)^2}$ (c)  $\frac{dy}{dx} = \frac{24x}{(2-x)^2}$ 

(a) 
$$\frac{dy}{dx} = \frac{24x - 6x^2}{(2-x)^2}$$

(b) 
$$\frac{dy}{dx} = \frac{6x^3 - 12x^2 + 24x}{(2-x)^2}$$

(c) 
$$\frac{dy}{dx} = \frac{24x}{(2-x)^2}$$

(d) None of these

Q 14. Find double derivative of  $y = x^3 - x^2 + x - 1$ , w.r.t. 'x'

(a) 
$$\frac{d^2y}{dx^2} = 3x^2 - 2x + 1$$

(b) 
$$\frac{d^2y}{dx^2} = 6x - 2$$

$$(c) \frac{d^2y}{dx^2} = 6$$

(d) None of these

Q 15. Find value of  $\frac{d^2y}{dx^2}$  at  $x = \frac{\pi}{2}$ , if  $y = \sin x$ :

$$(a) \frac{d^2y}{dx^2} = -1$$

(b) 
$$\frac{d^2y}{dx^2} = 1$$

(a) 
$$\frac{d^2y}{dx^2} = -1$$
 (b)  $\frac{d^2y}{dx^2} = 1$  (c)  $\frac{d^2y}{dx^2} = zero$  (d)  $\frac{d^2y}{dx^2} = 2$ 

$$(d) \frac{d^2y}{dx^2} = 2$$

Q 16. Find  $\frac{d^2y}{dx^2}$ , if  $y = e^x$ :



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(a) 
$$\frac{d^2y}{dx^2} = xe^x$$
  
(c) 
$$\frac{d^2y}{dx^2} = e^x$$

$$(b)\frac{d^2y}{dx^2} = e^x + 1$$

$$(c)\frac{\mathrm{d}^2 y}{\mathrm{d}x^2} = e^{2x}$$

(d) None of these

Q 17. Find 
$$\frac{d^2y}{dx^2}$$
, if  $y = \ln x$ :

(a) 
$$\frac{d^2y}{dx^2} = -x^2$$
 (b)  $\frac{d^2y}{dx^2} = -\frac{1}{x^2}$ 

(b) 
$$\frac{d^2y}{dx^2} = -\frac{1}{x^2}$$

$$(c) \frac{\mathrm{d}^2 y}{\mathrm{d}x^2} = \frac{1}{x^2}$$

(d) None of these

Q18. If 
$$y = x^x$$
,  $\frac{dy}{dx} = ?$ 

(a) 
$$x^{x}$$

(b) 
$$x^x(1 + \ln x)$$

(c) 
$$x^{x-1}$$

(d) 
$$x^{x+1}$$

Q19. If 
$$x^3 + y^3 = 2xy$$
, find value of  $\frac{dy}{dx}$  at (1,1)?

Q20. If 
$$2x = t^2$$
,  $y = t^3 + t^2$ . Find  $\frac{dy}{dx}$  at  $t = 1$ ?

(b) 
$$3$$

Q21. 
$$y = \sqrt{\ln x}$$
, Find  $\frac{dy}{dx}$ ?

(a) 
$$\frac{1}{2(\ln x)^{3/2}}$$

(b) 
$$\frac{1}{2x(\ln x)^{1/2}}$$

(c) 
$$\frac{-1}{2(\ln x)^{3/2}}$$

(d) 
$$\frac{1}{(\ln x)^{3/2}}$$

#### **Answer Key**

Q.1 b	Q.2 b	Q.3 d	Q.4 c	Q.5 a
		Q.8 b	Q.9 a	Q.10 c
Q.11 c	Q.12 b	Q.13 a	Q.14 b	Q.15 a
Q.16 c	Q.17 b	Q.18 b	Q.19 b	Q.20 d
Q.21 b		1		