# UNIT II ANALOG COMMUNICATION

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## Objective

1. Solving Problems related to AM



Q1. A 400 W carrier is modulated to a depth of 75 percent. Calculate the total power in the modulated wave?

A carrier signal with power of 40W is amplitude modulated by a sinusoidal signal. Compute the power of modulated signal if the modulation index is 0.7. (May/June-16)



#### Given:

Carrier Power  $P_c = 400W$ ,

Depth of modulation=75%, hence modulation index m = 0.75

#### Answer:

Total power in the modulated wave,

$$P_{T} = P_{C} \left( 1 + \frac{m^{2}}{2} \right)$$

$$= 400 \left( 1 + \frac{0.75^{2}}{2} \right)$$

$$P_{T} = 512.4W$$



Q2. A broadcast radio transmitter radiates 10kilowatts when the modulation percentage is 60. Calculate the carrier power.



Given:  $P_T = 10kW = 10 \times 10^3$ 

Modulation index (m) = 0.6

Answer:

We know,  $P_T = P_C \left(1 + \frac{m^2}{2}\right)$ 

Then,  $P_C = \frac{P_T}{(1+m^2/2)}$ 

$$=\frac{10\times10^3}{\left(1+\frac{0.6^2}{2}\right)}$$

$$P_C = 8.47kW$$



Q3. A 1 MHz carrier with an amplitude of 1 volt peak is modulated by a 1 kHz signal with modulation index 0.5. Sketch the frequency spectrum.



### Given:

Carrier frequency-  $f_c = 1MHz$ 

Carrier amplitude-  $E_c = 1V$ 

Message signal frequency-  $f_m = 1kHz$ 

Answer:

Upper side band component:  $f_c + f_m = 1000kHz + 1kHz = 1001kHz$ 

Upper sideband amplitude  $\underline{mE_c}$ 

$$= \frac{0.5 \times 1}{2} = 0.25V$$

Lower sideband component:  $f_c - f_m = 1000kHz - 1kHz = 999kHz$ Lower sideband amplitude  $= \frac{0.5 \times 1}{2} = 0.25V$   Q4. An amplitude modulated wave is described by the equation

 $e_{AM} = 10(1 + 0.4 \cos 1000t + 0.2 \cos 800t)\cos 10^6 t$ Specify different frequencies present in the AM signal.



$$f_{m1} = \frac{1000}{2\pi} = 159.09 \ Hz$$

$$f_{m2} = \frac{800}{2\pi} = 127.27 \ Hz$$

$$f_c = \frac{10^6}{2\pi} = 159.09 \, kHz$$

$$BW = 2 \times f_{m(\text{max})} = 2 \times 159.09 Hz = 318.18 Hz$$



## Q5. The output modulated wave of a standard AM transmitter is represented

$$S(t) = 500(1 + 0.4\sin 3140t)\cos 6.28 \times 10^7 t$$

This voltage is fed to a load of  $600\Omega$ . Find

- 1) Modulating frequency
- 2) Carrier frequency
- 3) Mean power output.



## May/June-16

 A 1000 kHz carrier is simultaneously modulated with 300 Hz, 800 Hz and 2 kHz audio sine waves. Find the frequencies present in the output.



Q6. AM radio channel bandwidth is 10 kHz.
 What is the maximum modulation frequency?

Answer:

Bandwidth of AM signal  $=2f_m$ 

$$f_m = \frac{Bandwidth}{2}$$
$$= \frac{10kHz}{2} = 5kHz$$



- Q7. For an AM DSB-FC transmitter with an un-modulated carrier power  $P_c = 100W$  that is modulated simultaneously by three modulating signals with coefficient of modulation  $m_1 = 0.2, m_2 = 0.4$  and  $m_3 = 0.5$ , determine,
- i) Total coefficient of modulation
- ii) Upper and lower sideband power
- iii) Total transmitted power



Given: Carrier power  $P_c = 100W$ 

Modulation indices:  $m_1 = 0.2$ ,  $m_2 = 0.4$  and  $m_3 = 0.5$ 

Answer:

Modulation index 
$$(m) = \sqrt{(m_1^2 + m_2^2 + m_3^2)}$$
  
=  $\sqrt{(0.2^2 + 0.4^2 + 0.5^2)}$   
 $m = 0.67$ 

Upper and lower sideband power  $P_{USB} = P_{LSB} = P_C \frac{m^2}{4}$ =11.25W

Total transmitted power 
$$P_T = P_C \left(1 + \frac{m^2}{2}\right)$$
  
 $P_T = 122.45W$ 



## Q8. What is the efficiency of AM system, when the modulation index is one?

$$\eta = \frac{m^2}{2 + m^2} \times 100$$

$$\eta = \frac{1}{2+1} \times 100 = \frac{1}{3} \times 100 = 33.33\%$$



- Q9. A Modulating signal  $20\sin(2\pi \times 10^3 t)$  is used to modulate a carrier signal  $40\sin(2\pi \times 10^4 t)$ . Find out,
- i) Modulation index
- ii) Percentage modulation
- iii) Frequencies of sideband and their amplitudes
- iv) Bandwidth of modulating signal
- v) Draw the spectrum of AM wave.



Given: Modulating signal:  $20\sin(2\pi \times 10^3 t)$ 

Carrier signal  $40 \sin(2\pi \times 10^4 t)$ 

Given information's are compared with generalized expression of modulating and carrier signal.

$$e_m = E_m \cos 2\pi f_m t$$

$$E_m = 20 \qquad f_m = 10^3$$

$$e_c = E_c \cos 2\pi f_c t$$

$$E_c = 40; \quad f_c = \mathbf{10^4}$$

Modulation index 
$$m = \frac{E_m}{E_s}$$
  $m = \frac{20}{40} = \frac{1}{2} = 0.5$ 

Percentage of modulation =  $m \times 100 = 0.5 \times 100 = 50\%$ 

Frequencies of sidebands

Upper sideband 
$$f_c + f_m = 10^4 + 10^3 = 10kHz + 1kHz = 11kHz$$

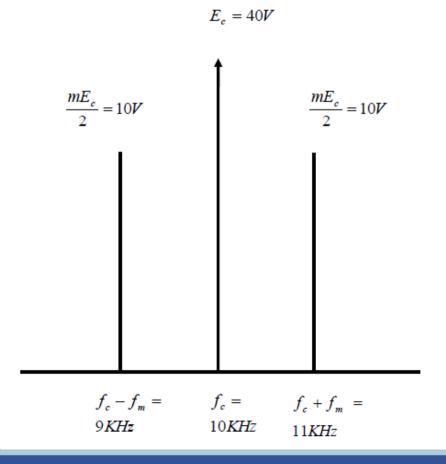
Lower sideband 
$$f_c - f_m = \mathbf{10}kHz + \mathbf{1}kHz = \mathbf{9}kHz$$

Sideband amplitudes 
$$= \frac{mE_C}{2} = \frac{0.5 \times 40}{2} = 10V$$

Bandwidth = 
$$2f_m = 2 \times 1kHz = 2kHz$$



## • Frequency spectrum:





Q10. An AM signal with a carrier of 1kW has 200W in each sideband. What is the percentage of modulation?

m=89.44%



Q11. In AM signal, power in upper sideband is 500 W for 100% modulation. Determine the power in carrier.



## Given

$$P_{USB} = 500W, m = 1, P_C = ?$$
 As we know,

$$P_{USB} = \frac{m^2 P_C}{4}$$
$$P_C = 2000 W$$



Q12. A complex modulating signal consisting of a sinewave of amplitude 3V peak and frequency 1 kHz, and a cosine wave of amplitude 5V and frequency 3 kHz modulates a 500 kHz and 10 V peak carrier voltage. Plot the spectrum of AM signal.



#### Given

### Modulating signal:

$$E_{m1} = 3V; f_{m1} = 1kHz$$

$$E_{m2} = 5V; f_{m2} = 3kHz$$

Carrier signal:  $E_c = 10V$ ;  $f_c = 500kHz$ 

Answer: 
$$m_1 = \frac{E_{m1}}{E_c} = \frac{3}{10} = 0.3$$
  $m_2 = \frac{E_{m2}}{E_c} = \frac{5}{10} = 0.5$ 

Total modulation index:  $m = \sqrt{(m_1^2 + m_2^2)}$   $m = \sqrt{(0.3^2 + 0.5^2)} = 0.583$ 

Upper sideband components;  $f_c + f_{m1} = 500kHz + 1kHz = 501kHz$ 

$$f_c + f_{m2} = 500kHz + 3kHz = 503kHz$$

Lower sideband components;

$$f_c - f_{m1} = 500kHz - 1kHz = 499kHz$$
  
 $f_c - f_{m2} = 500kHz - 3kHz = 497kHz$ 

Bandwidth = 
$$2 \times f_{m(\text{max})}$$



