

**COMPUTATIONAL INVESTIGATION  
ON SUPERSONIC PROPELLING NOZZLE OF  
ROCKET ENGINE**

*A THESIS*

*Submitted by:*

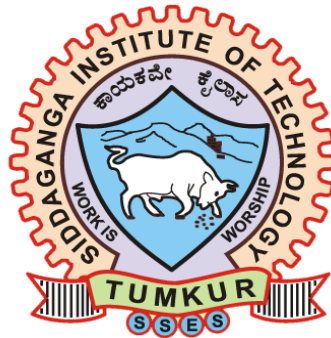
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*Is submitted in partial fulfilment of the requirement for the award of*  
**BACHELOR OF ENGINEERING**



**DEPARTMENT OF MECHANICAL ENGINEERING  
SIDDAGANGA INSTITUTE OF TECHNOLOGY  
TUMAKURU-572103**

**JULY-2022**

## Department of Mechanical Engineering



### **CERTIFICATE**

This is to certify that the Major Project entitled “**COMPUTATIONAL INVESTIGATION ON SUPERSONIC PROPELLING NOZZLE OF ROCKET ENGINE**” is carried out by **Gagan R Preeth (1SI18ME034), Harish G R (1SI18ME038), Hemanth C (1SI18ME040), Manjunath Gowda K R (1SI18ME052)** bonafide students of Siddaganga Institute of Technology, Tumakuru, and submitted report in partial fulfilment of the requirement for the award of Bachelor of Engineering in Mechanical Engineering of Visvesvaraya Technological University, Belagavi during the year 2021-22. It is certified that all corrections/suggestions indicated for Internal Assessment have been incorporated in the report deposited in the departmental library. The Major Project report has been approved as it satisfies the academic requirements in respect of Major Project work prescribed for the said Degree.

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1. ....
2. ....

*Dedicated to our parents, our teachers, our guide and our team mates who supported us through thick and thin during the course of the project and to all the engineers who strive out there to build a better tomorrow.....*

## THESIS CERTIFICATE

This is to certify that the thesis entitled “**COMPUTATIONAL INVESTIGATION ON SUPERSONIC PROPELLING NOZZLE OF ROCKET ENGINE**” submitted to the Siddaganga Institute of Technology, for the award of the degree of Bachelor **of Engineering** is a bonafide record of project work carried out by us under the supervision of **Dr. Nithesh K G**. The contents of this thesis, in full or in parts, have not been submitted to any other Institute or University for the award of any degree or diploma.

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## ABSTRACT

A nozzle in a rocket engine propels hot exhaust to create thrust in accordance with Newton's third law of motion. The amount of thrust produced by the engine is determined by the mass flow rate through the engine, the exit velocity of the flow, and the pressure at the engine's exit. The value of these three flow variables is governed by the rocket nozzle design. In addition, the design of the nozzle is an important consideration when attempting to accomplish a maximum Mach number or supersonic speed.

Rocket nozzles typically consist of a fixed convergent part followed by a fixed divergent section. A convergent-divergent, or CD, nozzle is the name given to this arrangement of nozzles. The hot exhaust from the combustion chamber converges on the nozzle's minimum area, or throat, in a CD rocket nozzle. The high temperature, high pressure, and low velocity gas are all converted into high velocity, low pressure gas at the exit by this nozzle.

Numerical simulations of supersonic flow through the rocket's nozzle have been performed. The goal of this study is to model a 3D convergent-divergent nozzle and examine the variations in flow parameters (pressure, temperature, and Mach number) brought on by altering the convergent angles of the nozzle ( $24^\circ$ ,  $26^\circ$ ,  $28^\circ$ ,  $30^\circ$ , and  $32^\circ$ ) while keeping the same throat and outlet diameters.

In order to determine the appropriate convergent angle, the flow characteristics variation at the nozzle exit is investigated. The Mach number and thrust at the nozzle's exit are found to be 1.7 and 13610.7N from the analysis for a convergent angle of  $26^\circ$ . When all of the converging angle results were taken into account,  $26^\circ$  produced the highest Thrust and Mach number, which will enhance the nozzle's performance and, as a result, increase the power and effectiveness of a propulsion system.

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# **CHAPTER 1**

## **INTRODUCTION**

### **1.1 ROCKET PROPULSION SYSTEM**

The nozzle plays a crucial role in the propulsion system and is primarily responsible for accelerating the hot gases that flow through it. Along with directing and controlling pressure, it also controls the flow. It also turns the pressure energy into kinetic energy. The nozzle's performance has a big impact on the propulsion system's efficiency. Usually, there are a few distinct categories into which nozzles can be divided. Convergent-divergent nozzles are among those that are in great demand to produce the supersonic speeds required in a number of technical specializations.

The Convergent-Divergent (CD) nozzle, used in rocket engines, supersonic jet engines, and some variants of steam turbines, is a common design. It also goes by the name "de-Laval nozzle" in some contexts. The gas expands and accelerates to a speed faster than the speed of sound. The performance of this nozzle is determined by flow characteristics, which are impacted by the nozzle's geometry.

Rocket propulsion is a type of jet propulsion in which thrust is generated by ejecting stored material known as propellant. This type of propulsion is used in rockets. Rocket propulsion systems can be classified based on their energy source (chemical, nuclear, or solar), with the primary function remaining the same (booster stage, sustainer, altitude control, orbit station keeping, etc.,) The size of the vehicle (plane, missile, space vehicle, etc.), type of construction, propellant type, and number of rocket propulsion units utilized in a certain vehicle are all aspects to consider.

Rocket nozzles typically consist of a fixed convergent part followed by a fixed divergent section. A convergent-divergent, or CD, nozzle is the name given to this arrangement of nozzles. The hot exhaust from the combustion chamber converges on the nozzle's minimum area, or throat, in a CD rocket nozzle. The high temperature, high pressure, and low velocity gas are all converted into high velocity, low pressure gas at the exit by this nozzle.

## 1.2 CLASSIFICATION OF ROCKET PROPULSION

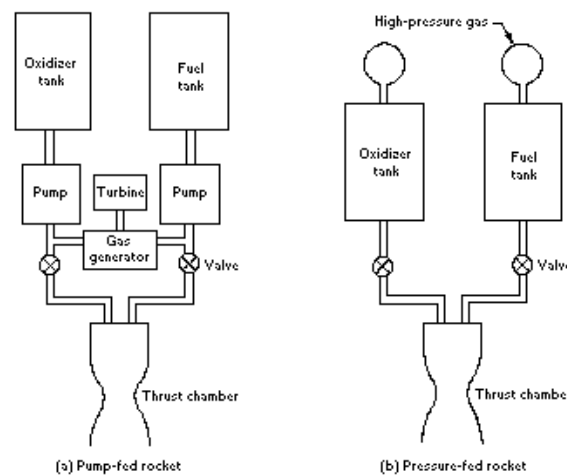
Rocket propulsion is classified as follows:

- Chemical rocket propulsion
- Nuclear rocket propulsion
- Electric rocket propulsion
- Solar rocket propulsion

### CHEMICAL ROCKET PROPULSION

Chemical propellants are commonly used to provide exact impulse values ranging from around 175 seconds to nearly 300 seconds. Maximum active chemical propellants are potentially capable of producing accurate impulses lasting up to 400 seconds.

To be efficient, a propellant must have a high rate of combustion to produce high temperatures and must produce combustion products including simple, mild molecules like as hydrogen (the lightest), carbon, oxygen, and the lighter metals (aluminum, beryllium, lithium).



**Fig 1.1:** Fuel and Oxidizer feeding system [1]

The density of a propellant is another crucial element. When compared to a low-density propellant of the same weight, a dense propellant can be transported in a smaller, lighter tank.

Other criteria must be addressed when selecting propellants. Some compounds with high specific impulse cause issues in engine functioning. Some are insufficient as coolants for the heated thrust-chamber walls. Others have anomalies in combustion that make their use difficult or impossible. Some are unstable to varied degrees and cannot be properly kept or handled. Such characteristics exclude its application in rocket propulsion.

Unfortunately, practically any useful propellant is likely to be a very active chemical, thus, most propellants are corrosive, combustible, or toxic, and are frequently all three.

The availability of a rocket propellant is also important when selecting one. In rare circumstances, a completely new chemical facility is required to obtain sufficient amounts of a propellant. Furthermore, because some propellants are utilized in huge amounts, raw material availability must be considered.

It is further classified into:

- Liquid propellant
- Solid propellant
- Gaseous propellant
- Hybrid propellant

## **NUCLEAR ROCKET ENGINE**

Nuclear rockets no longer employ any kind of combustion process. Rather, the most recent exhaust fuel line is created by sending a working fluid through a fission reactor.

Even though no power is provided to the rocket by any chemical reaction, nuclear rockets should employ some chemical as an operational fluid or propellant.

The reactor generates all of the heat. Liquid hydrogen is the best substance up to this point because the main focus is on lowering the molecular weight of the exhaust gasoline. Fission reactors, radioactive isotope decay, and fusion reactors are the three types of nuclear power sources that have been researched.

## **ELECTRIC ROCKET PROPULSION**

Electro thermal, electro static, and electromagnetic propulsion are all explored. Electric driven rocket propulsion has the highest specific impulse of all rocket propulsion methods. Electro jet, arc jet, magneto plasma dynamic thruster, pulsed plasma thruster, corridor thruster, etc. are a few examples of electrical propulsion.

## **SOLAR ROCKET PROPULSION**

A variety of proposals have been put up to use the Sun's radiation to provide a space spacecraft with propulsion power. Solar radiation can be used for propulsion in "open" environments even if its energy density is relatively low compared to chemical launch rockets' enormous power.

A very small amount of thrust will be sufficient to drastically change or accelerate a vehicle's trajectory once it has travelled far from Earth or another planetary body or has been placed in a satellite orbit.

### **1.3 PRINCIPLE OF OPERATION OF ROCKET ENGINES**

The rocket, in one of its many variants, is considered the easiest way to meet space flight speed requirements. The reaction pressure created by ejecting debris from a nozzle opening at a high rate of speed is known as rocket thrust. These ejected particles may be made of solids, liquids, gases, or even bundles of radiant energy.

As long as the delivery of debris or flowing fluid persists, the engine's ability to produce thrust will experience the simplest changes. Without the ability to expel fabric, no thrust can be produced, regardless of how much power is supplied. Fabric expulsion is the essence of the thrust production.

Due to this crucial aspect, an important criterion for evaluating rocket performance is exact impulse, which measures the efficiency with which a rocket utilizes its fuel or operating fluid to generate thrust.

For gaseous flowing fluids, precision impulse can be accelerated by,

- (1) Increasing combustion chamber temperatures.
- (2) Increasing the proportion of lighter gases, especially hydrogen, in the exhaust.

The load of engine and running fluid box necessary in measuring the advantage of a propulsion device in particular software is the different vital aspect, because such weights have an effect on the achievable propellant fraction.

### **1.4 PERFORMANCE PARAMETERS**

The rocket engine's performance is mostly determined by the four characteristics listed below.

1. Thrust
2. Specific impulse
3. Effective exhaust velocity
4. Characteristic velocity

All of the above criteria are mostly determined by the following:

- a) The chamber pressure
- b) The atmospheric pressure
- c) Ratio of expansion area
- d) Nozzle design and exit angle
- e) The composition and mixing ratio of propellants
- f) Assumption and correction in theoretical performance calculations
- g) Propeller initial temperature

## **THRUST**

The thrust is the force produced by the action of a rocket propulsion system on a vehicle. Momentum is a vector quantity defined as the product of mass multiplied by velocity.

The thrust, due to change in momentum is given below.

$$F_T = \dot{m}_e U_e + A_e (p_e - p_{amb}) \quad [2]$$

When the nozzle exit pressure equals the ambient pressure, this force represents the total propulsion force.

## **SPECIFIC IMPULSE**

Specific impulse is the best indicator of a rocket motor's overall performance. In seconds, a specific impulse is expressed. The particular impulse is the length of time for which the rocket engine produces a thrust equal to the weight of the propellant used while the thrust and flow rate remain constant during the propellant burning.

$$I_{sp} = \frac{F_T}{\dot{m}_{ejects}} \quad [2]$$

Because the ambient pressure is taken into account in the expression for the thrust for a given engine, the specific impulse has different values on the ground and in the vacuum of space. It is crucial to specify whether the value of a certain impulse is that at sea level or in a vacuum.

### **EFFECTIVE EXHAUST VELOCITY**

The average equivalent velocity at which propellant leaves the vehicle is known as the effective exhaust velocity.

$$c = \frac{F_T}{\dot{m}_e} = I_s g_o \quad [2]$$

### **CHARACTERISTIC EXHAUST VELOCITY**

Characteristic velocity, which is used to compare various propellants, is a measurement of the combustion performance of a rocket engine independent of nozzle performance.

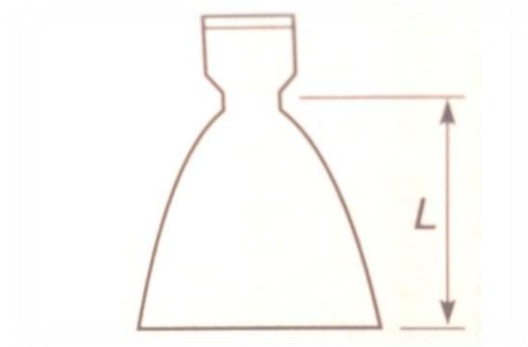
$$c = U_e + \frac{(p_e - p_a)A_e}{\dot{m}_e} \quad [2]$$

$$C^* = \frac{P_c A_t}{\dot{m}_e} \quad [2]$$

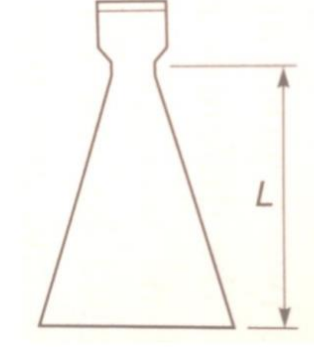
There may be a significant amount of losses in practice even though the rocket engine's theoretical performance criteria have been established. A rocket engine contains some losses, the main ones being those brought on by the ineffectiveness of the combustion process, losses from the nozzle, and losses from the pumps. The overall performance of the given impulse is impacted by the losses.

This is the ratio of the actual specific impulse (at sea level or in a vacuum) to the theoretical specific impulse acquired with a large nozzle from gases produced by a full chemical reaction.

Losses of the inner surprise waves inside the supersonic flow were reduced to a minimum by the bell-contoured nozzle. Since the 1960s, both rockets using liquid propellant and those using stable propellant have used bell-shaped nozzles. Before the transition to bell-shaped discharge nozzles, conical nozzles had been utilized often in the past. Figures 1.2 and 1.3, respectively, demonstrate how a Rao nozzle and conical nozzle are shaped.



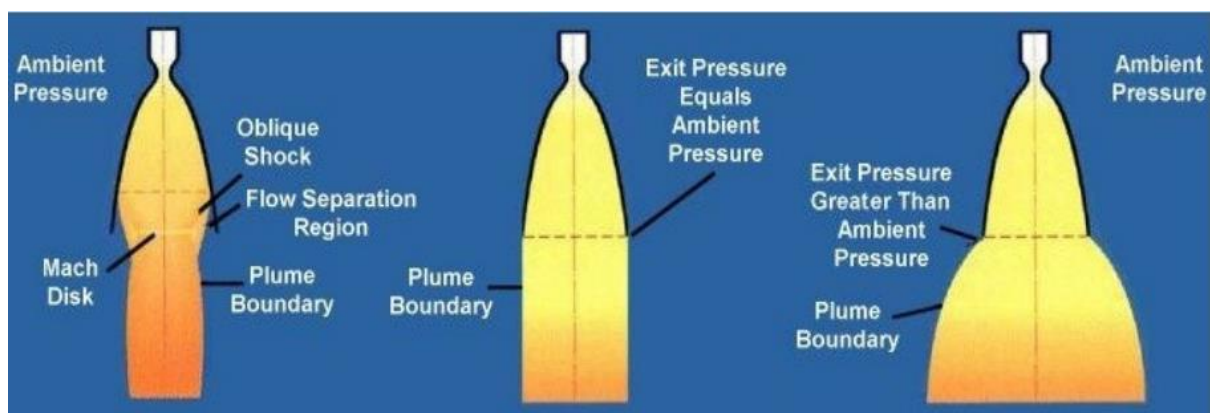
**Fig 1.2:** Rao nozzle [3]



**Fig 1.3:** Conical Nozzle [3]

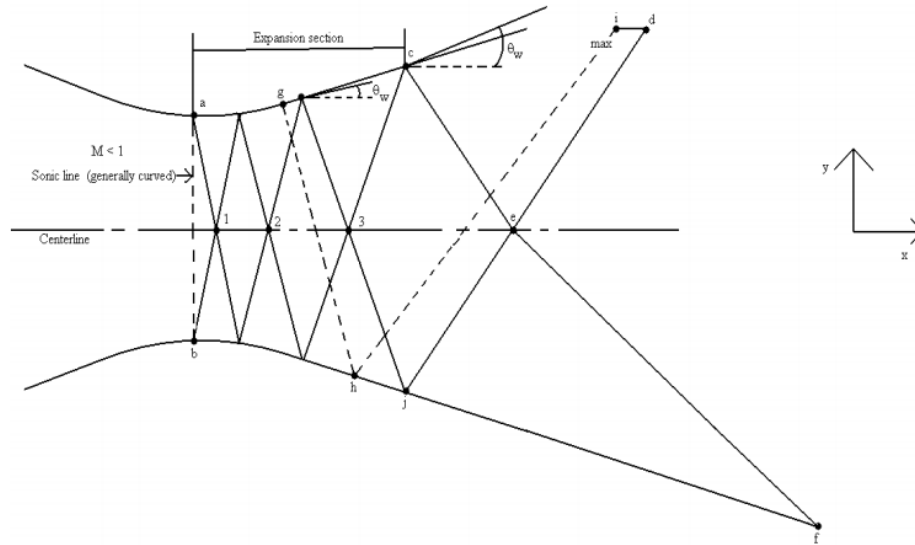
At high altitudes, an under-expanded nozzle develops when the exit pressure is higher than the surrounding pressure. Beyond the nozzle exit, the exhaust plume keeps growing, decreasing efficiency. When the outlet pressure is equal to the ambient pressure, the nozzle expands properly, resulting in optimum efficiency.

An over-expanded nozzle occurs when the exit pressure is less than the ambient pressure at low altitudes such as sea level. The exhaust plume is pinched inward in fluid separation from the walls creating compression waves or shock waves inside the diverging nozzle section. Fig 1.4 below shows the under-expanded, over-expanded, and perfectly expanded nozzles.



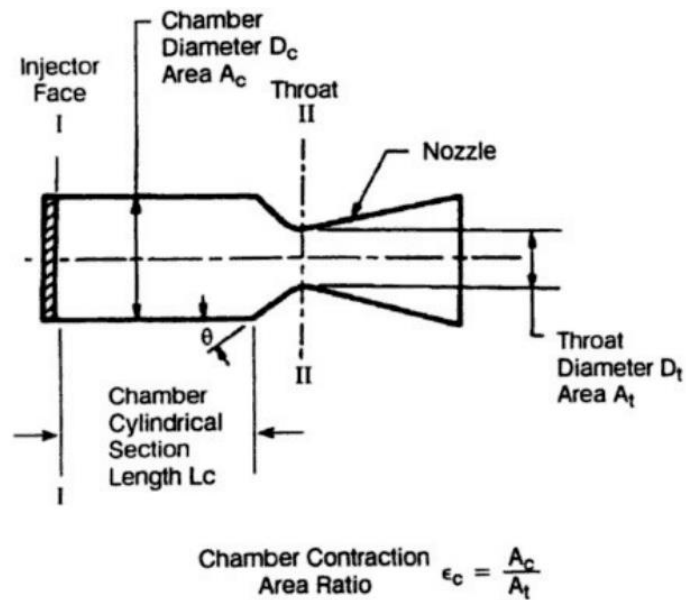
**Fig 1.4:** Under-Expanded, Over-Expanded, & Perfectly Expanded Nozzles [4]





**Fig 1.5:** Schematic of Supersonic Nozzle Design by the MOC [5]

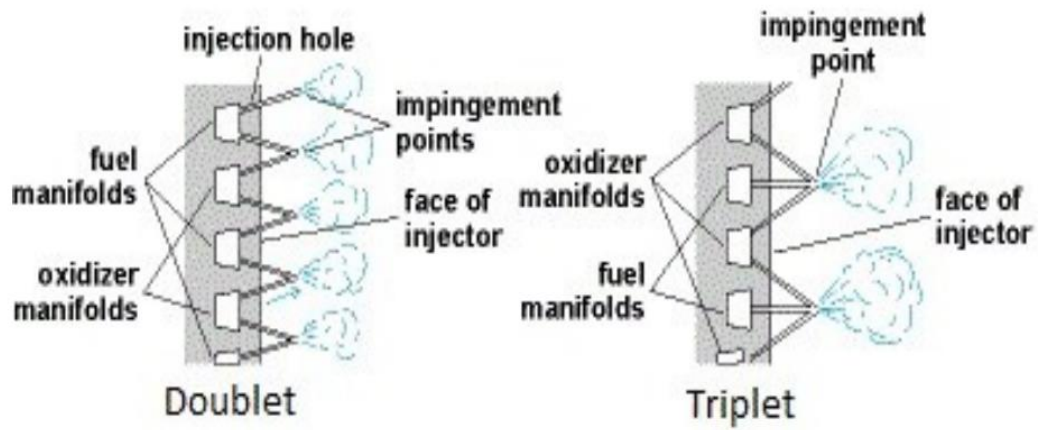
The most popular combustion chamber for rockets is cylindrical because it is easier to manufacture and performs better than a spherical or nearly spherical chamber. Figure following illustrates a concept sketch for a cylindrical combustion chamber.



**Fig 1.6:** Rocket Cylindrical Combustion Chamber [6]

Liquid propellant is injected into the combustion chamber using injectors, particularly a doublet or triplet impinging flow sample configuration.

The doublet impinging flow sample performs admirably when the gasoline hollow length is the same as the oxidizer hollow length.

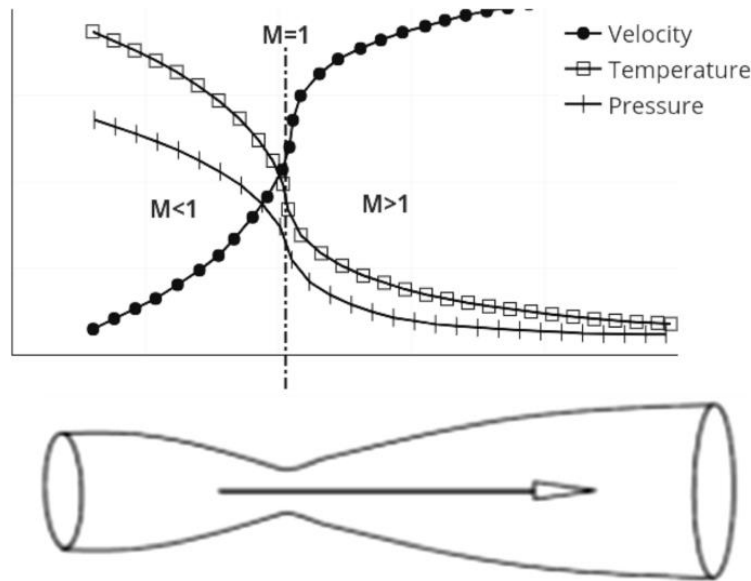


**Fig 1.7:** Schematic Diagrams of the Doublet and Triplet Injector Types [3]

## CHAPTER - 2

### LITERATURE SURVEY

The main reason for the invention of the nozzles was to modify the flow properties, such as pressure and velocity. A convergent-divergent (CD) nozzle was created in 1890 by Carl Gustaf Patrik de Laval that could accelerate a steam jet to supersonic speed [7].



**Fig 2.1:** Variations in pressure, temperature, and velocity along a De Laval nozzle [7].

The principal means of propulsion for space travel is the rocket, which stores its own mass of fuel and expels it rapidly to provide thrust [8].

This thrust is created by accelerating the exhaust gases of a rocket engine to the required speed and direction [9]. Simply described the nozzle increases the amount of force by leveraging the pressure inside the combustion chamber to accelerate the combustion products to a high supersonic velocity.

The creation of cutting-edge rocket nozzles for launch vehicles is a challenging task [10]. To ensure that they perform as expected at higher altitudes, the nozzles are constructed with high area ratios.

In addition to the recently developed multi nozzle grid (MNG), there are many different rocket nozzle designs available, including ideal, conical, bell, plug, expansion-deflection (E-D), and dual bell [11].

Due to its simplicity and ease of production, the conical form has historically been the most popular shape for rocket nozzles [12].

The area ratio and exit velocity of a conical nozzle are practically one-dimensional (1D), but the flow is not axial over the output area, leading to performance loss from flow divergence [13].

Conical type short nozzles are used in small thrust and solid rocket boosters because of their significant divergence losses, which are preferred over aerodynamic performance [14].

The nozzle wall can be contoured to reduce thrust loss; this design is known as a bell nozzle. This is so that the flow can be controlled to turn more toward the axial direction [15].

The plug nozzle is a form of rocket nozzle that accommodates for altitude, as opposed to a standard CD nozzle that expands the flow to a set area ratio regardless of the free stream circumstances. The free jet boundary, which acts as a plug nozzle's virtual outer wall, expands to meet the free stream ambient pressure [16].

The flow from the chamber is directed radially outward and away from the nozzle axis in the E-D nozzle. The flow is directed towards the outer diverging nozzle wall's curved contour [17].

A more modern concept known as Multi Nozzle Grid (MNG) proposes the use of a short, light plate with several small nozzles rather than a long, heavy single nozzle. A MNG with 100 nozzlettes is ten times smaller than a single nozzle of the same size, and the length savings are proportional to the square root of the number of small nozzles (nozzlettes) [18].

To overcome the complexity of experimental approaches, numerical methods are used with the aid of computer analysis software. CFD approach is carried out using ANSYS FLUENT to simulate the nozzle flow. Since the divergent angle affects performance, the conical nozzle has been tested so far at divergent angles of 7, 13, and 15, while maintaining the same intake and outlet diameters, and dependent parameters such as Mach number, static pressure, and shocks are reported [19].

Conical nozzle visualizations of supersonic expansion through CD nozzles produced results that were similar to experimental Schlieren photos and average shadowgraph images [20, 21].

An estimate of the exit pressure ratio is obtained by using reversible adiabatic and normal shock relations. With this exit pressure ratio, a more refined verification is done by computational analysis using ANSYS Fluent software for a contour nozzle with exit Mach number 5.5. The spalart Allmaras and k-epsilon model were used for turbulence modeling. Divergent nozzle contours were plotted for different exit mach numbers. The estimated exit area was similar to the theoretical one. The contours obtained through fluent simulation were close to the theoretical values of mach number at the exit [22].

ANSYS Fluent, software for computational fluid dynamics (CFD), is used to validate these formulas. CFD considers the factors like boundary layer effects, shock waves, radial velocity component and so on, which leads to some variance from theoretical results [23].

The challenge for designers of rocket nozzles is to continually find ways to harvest a greater specific impulse with a smaller size nozzle while optimizing cost savings and reducing structural complexity. Some of the most desired characteristics of a rocket nozzle include reduced weight, maximum performance, and simplicity of construction.

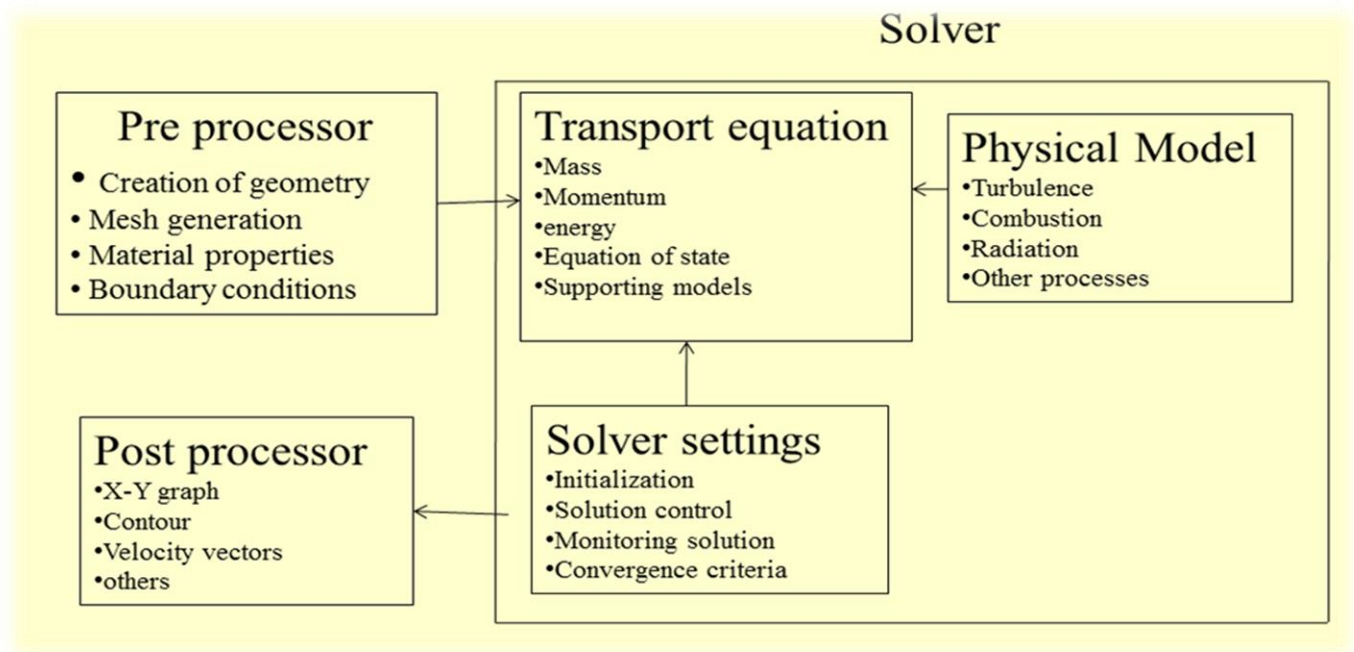
The detailed literature analysis demonstrates, each design has unique strengths and disadvantages, and no design comes out as clearly superior to the others.

## CHAPTER – 3

### CFD MODELING AND ANALYSIS

#### 3.1 INTRODUCTION

The computational fluid dynamics (CFD) tool is an engineering tool that assists in experimenting. In the computational fluid dynamics (CFD) analysis of the nozzle, the following processes were carried out: modeling, meshing, pre-processing, solution, and post-processing.



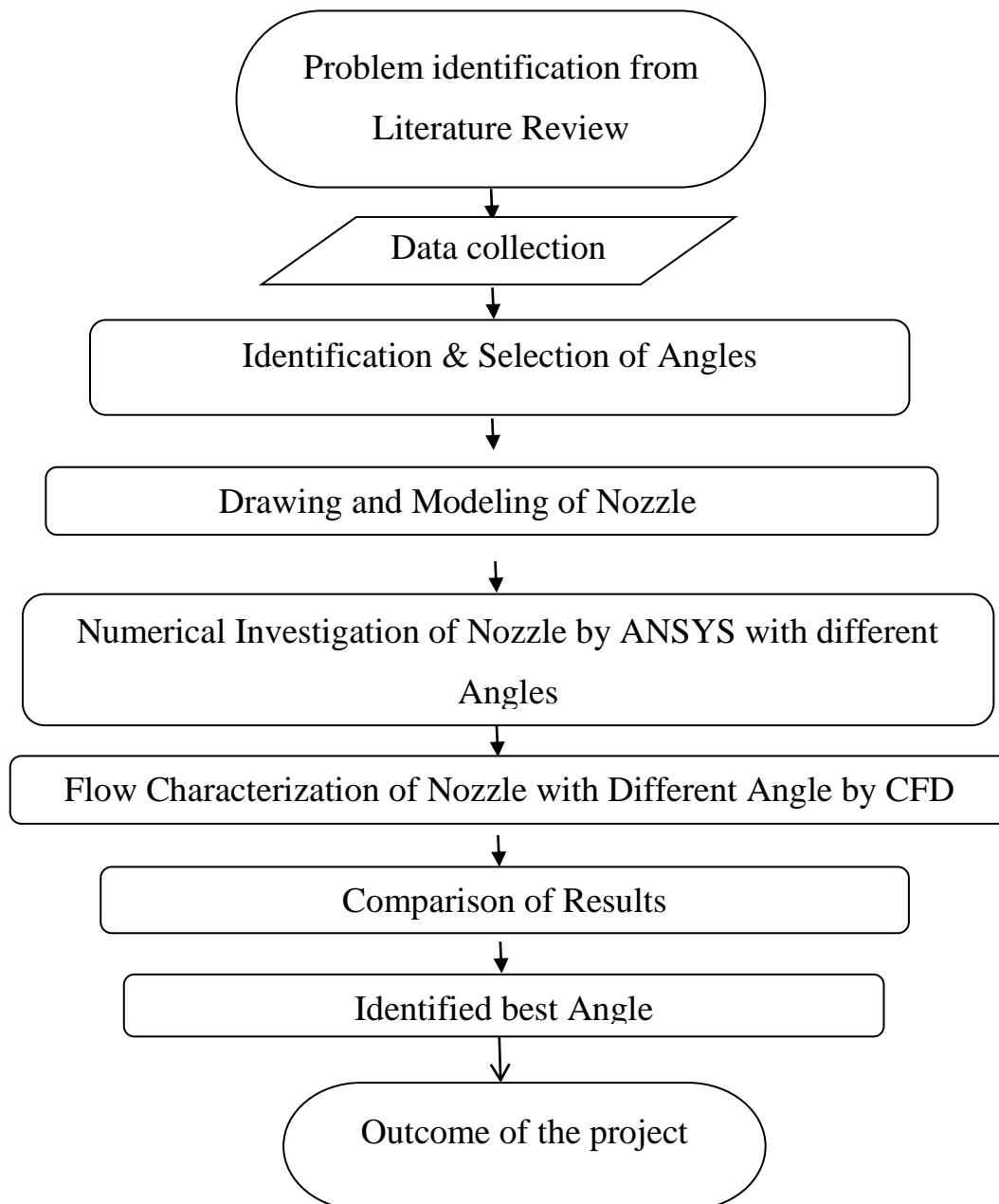
**Fig 3.1:** Main Elements of CFD Analysis [3]

This project comprises the process of numerical research for the characteristics of several convergent angles in nozzle by using CFD. The approach includes the procedure sequentially which was carried out is as shown in the fig 3.1.

### 3.2 METHODOLOGY

Modeling and flow analysis of 3-D models of the nozzle were carried out using CATIA and ANSYS software.

The methodology includes the process sequentially which carried out, this project includes the process of numerical investigation with different convergent angles (24°, 26°, 28°, 30°, 32°) in nozzle by ANSYS CFD.

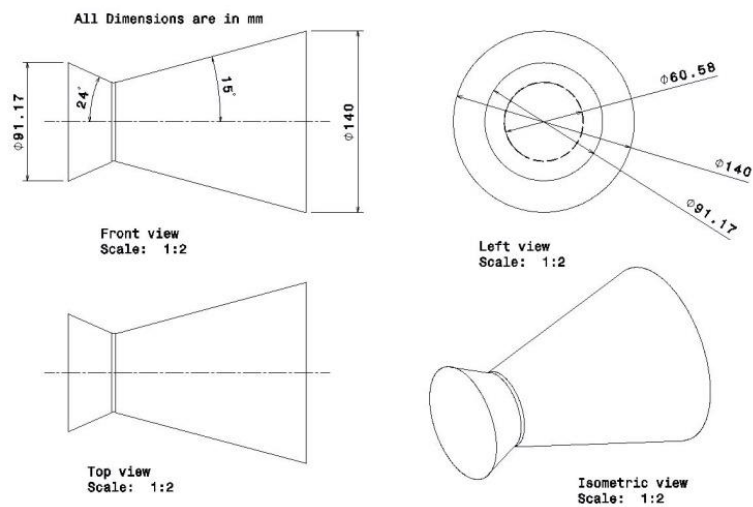


**Fig 3.2:** Flow chart

**3.3 MODELING:** Using CATIA and ANSYS software, 3-D models of the nozzle were modeled and their flow was examined. The dimensions of the CD nozzle are presented in the table given below.

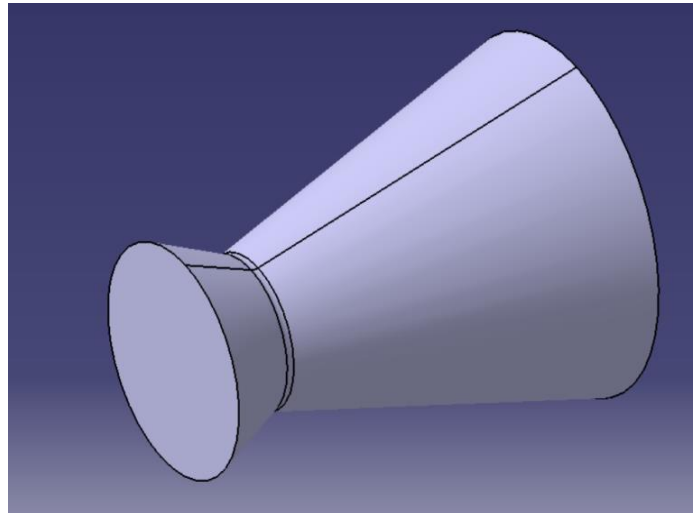
**Table 3.1:** Nozzle dimensions

Parameters	Dimensions				
Convergence angle (deg)	24	26	28	30	32
Divergence angle (deg)	15				
Inlet diameter (mm)	91.17	94.14	97.22	100.41	103.74
Throat diameter (mm)	60				
Outlet diameter (mm)	140				



**Fig 3.3:** Dimensions of Nozzle





**Fig 3.4:** Nozzle 3-D Model

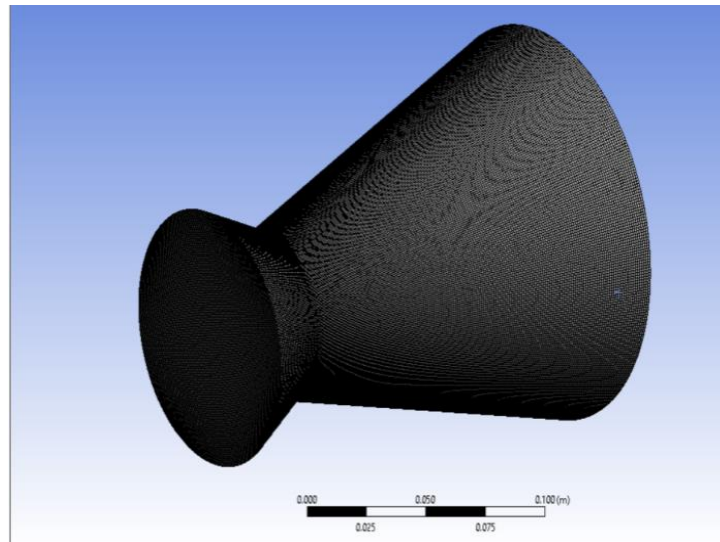
### 3.4 MESHING

The model made using the aforementioned dimensions was meshed using ANSYS mesh mode. Once the meshing of the nozzle is complete and the inflation control is set to "Program Controlled," the named selections for the INLET, OUTLET, and WALL are defined, and the meshing is updated. The best mesh is required to avoid numerical diffusion. The goal of measuring the best mesh quality is accomplished by considering a number of metrics, although the skewness is the most important one.

For Fluent, the most essential mesh metrics are Skewness and Aspect Ratio. Poor mesh quality may result in inaccurate results for all or most applications. In all or most uses, For Skewness, it should be less than 0.8 for Hexa, Tri, and Quad. Less than 0.9 will result in an incorrect solution and/or a slow convergence for tetrahedral problems. Tetrahedral shapes require a value of less than 0.9. Aspect Ratio: It should be less than 40, though the flow characteristics will determine exactly what that is.

0-0.25	0.25-0.50	0.50-0.80	0.80-0.95	0.95-0.98	0.98-1.00*
Excellent	very good	good	acceptable	bad	Inacceptable*

**Fig 3.5:** Classification of the mesh quality metrics based on skewness

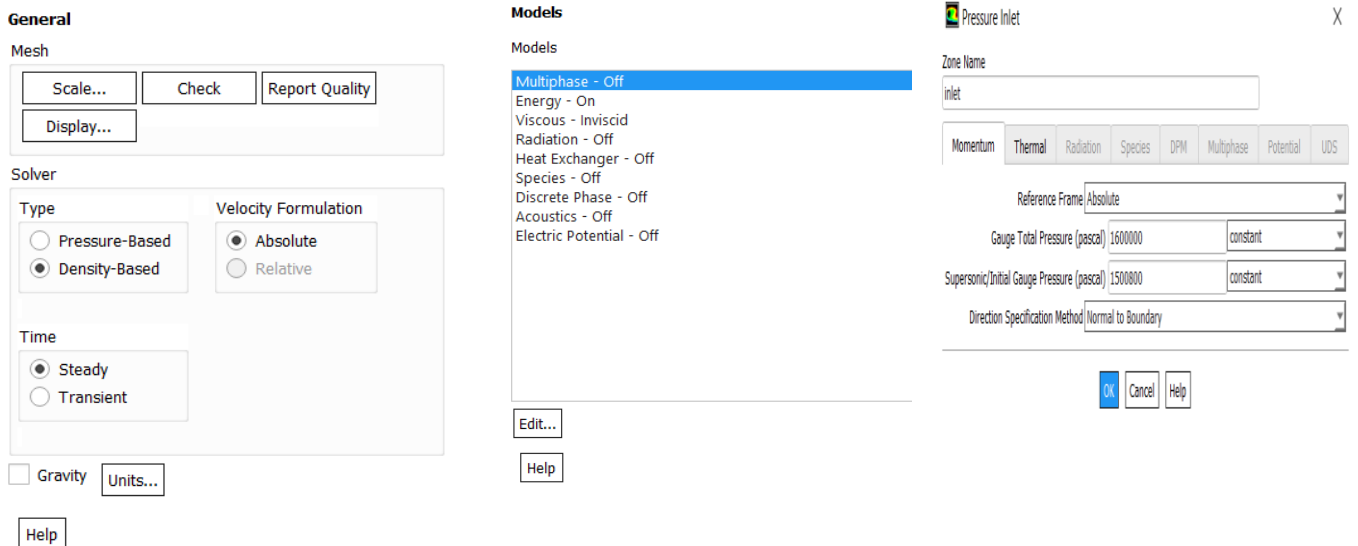


**Fig 3.6:** Meshing of the Nozzle

### 3.5 PRE-PROCESSING

Preprocessing comes after meshing in the CFD process. The meshed model is subjected to the proper boundary conditions during preprocessing. The nozzle was pre-processed using ANSYS FLUENT. Double precision settings were employed.

#### DETAILS:



Create/Edit Materials

Name: air Material Type: fluid

Chemical Formula: air

Order Materials by: Name

Properties:

Density (kg/m<sup>3</sup>): ideal-gas

Cp (Specific Heat) (J/kg-K): constant

Molecular Weight (kg/mol): constant

1006.43

28.966

Change/Create Delete Close Help

Pressure Inlet

Zone Name: inlet

Momentum Thermal Radiation Species DPM Multiphase Potential UDS

Total Temperature (K): 1500 constant

OK Cancel Help

Pressure Outlet

Zone Name: outlet

Momentum Thermal Radiation Species DPM Multiphase Potential UDS

Backflow Reference Frame: Absolute

Gauge Pressure (pascal): 10 constant

Pressure Profile Multiplier: 1

Backflow Direction Specification Method: Normal to Boundary

Backflow Pressure Specification: Total Pressure

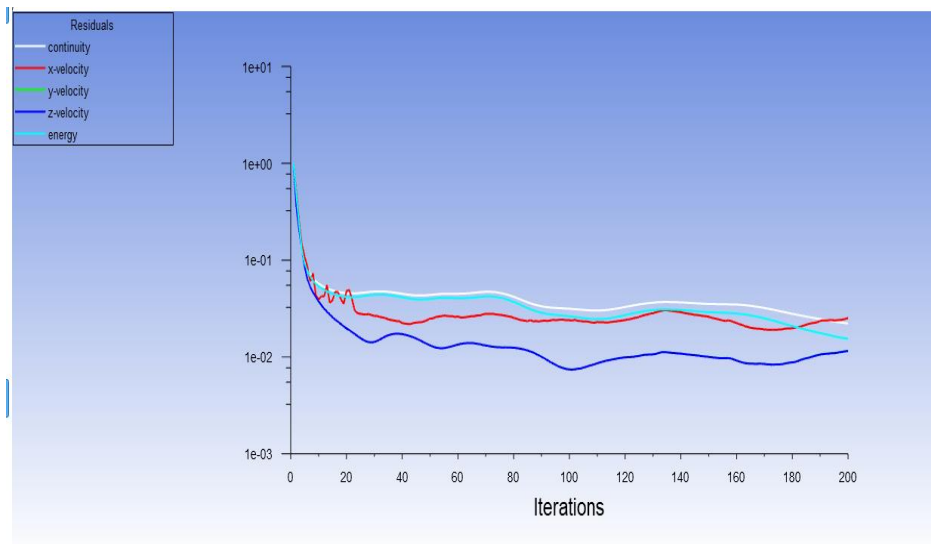
Radial Equilibrium Pressure Distribution: ☐

Average Pressure Specification: ☐

Target Mass Flow Rate: ☐

Acoustic Wave Model: ☒ Off ☐ Non Reflecting

OK Cancel Help



Pressure Outlet

Zone Name

Momentum Thermal Radiation Species DPM Multiphase Potential UDS

Backflow Total Temperature (k)  constant

OK Cancel Help

## Reference Values

Compute from

inlet

Reference Values

Area (m2)

Density (kg/m3)

Enthalpy (j/kg)

Length (m)

Pressure (pascal)

Temperature (k)

Velocity (m/s)

Ratio of Specific Heats

Reference Zone

solid-freeparts

Help

## Solution Initialization

Initialization Methods

- ☐ Hybrid Initialization  
☒ Standard Initialization

Compute from

inlet

Reference Frame

- ☒ Relative to Cell Zone  
☐ Absolute

Initial Values

Gauge Pressure (pascal)

X Velocity (m/s)

Y Velocity (m/s)

Z Velocity (m/s)

Temperature (k)

Initialize Reset Patch...

Reset DPM Sources Reset Statistics

## Run Calculation

Check Case...

Update Dynamic Mesh...

Options

☐ Data Sampling for Steady Statistics

Sampling Interval  
 Sampling Options...

Iterations Sampled

Number of Iterations

200

Reporting Interval

1

Profile Update Interval

1

☐ Solution Steering

Data File Quantities...

Acoustic Signals...

Acoustic Sources FFT...

Calculate

Help

## CHAPTER - 4

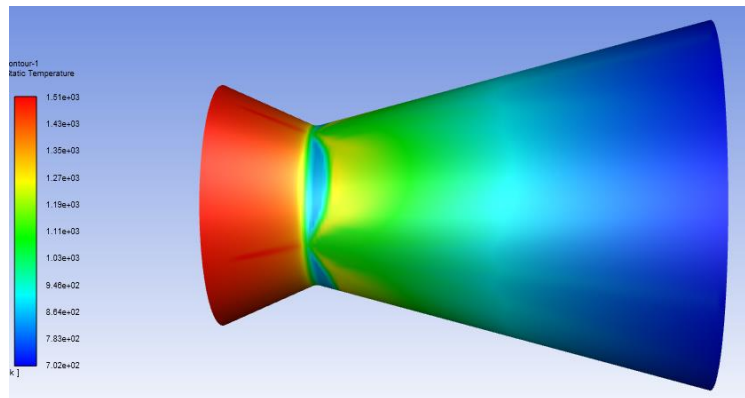
### RESULTS AND DISCUSSION

#### 4.1 INTRODUCTION:

This chapter attempts to analyze and discuss the major project work outcome in the area of rocket nozzles and is summarized. The different cases of nozzle analysis have been carried out. To validate the results, the simulation results are compared to the theoretical approach. For cases 1 to 5, the convergent angle will be  $24^\circ$ ,  $26^\circ$ ,  $28^\circ$ ,  $30^\circ$ , and  $32^\circ$ , respectively.

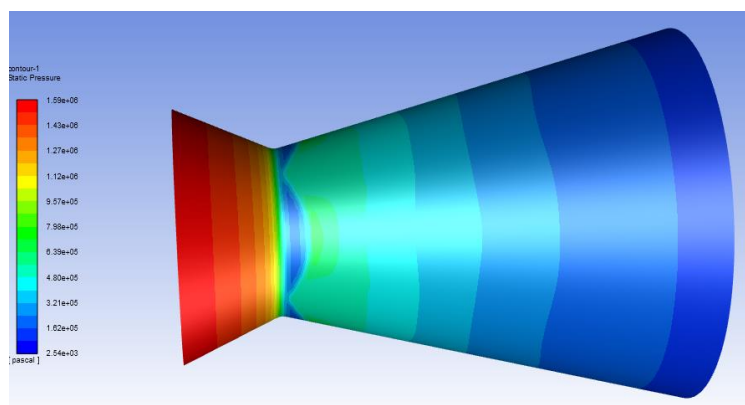
#### 4.2 CFD RESULTS FOR $26^\circ$ CONVERGENT ANGLE

**Temperature Contour:** The temperature is maximum at the inlet and goes on decreasing till the outlet. The magnitude of temperature at the outlet is 779 K.



**Fig 4.1:** Temperature Contour

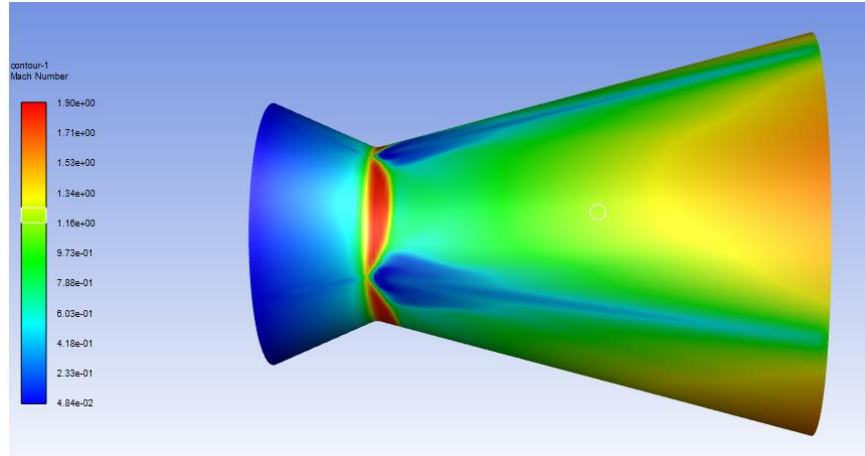
**Pressure Contour:** The pressure is maximum at the inlet and goes on decreasing till the outlet. The static pressure at the outlet is 157922.3 Pa. There is sudden decrease in pressure due to shock wave just after the throat section.



**Fig 4.2:** Pressure Contour

### Mach number Contour:

The velocity is minimum at the inlet and goes on increasing till the nozzle exit. The velocity magnitude is Mach 1 at the throat section of the nozzle. This condition is known as choked flow condition. The Exit Mach is 1.7.



**Fig 4.3:** Mach number Contour

## 4.3 THEORETICAL RESULTS FOR 26° CONVERGENT ANGLE:

### 1. EXIT MACH:

$$M_e = V/a = 558/331 = 1.68$$

$$M_e = 1.68$$

### 2. EXIT TEMPERATURE:

$$(T_e/T_t) = [1 + ((\gamma - 1)/2)M_e^2]^{-1}$$

$$T_e = 1200 * [1 + ((1.4 - 1)/2) * (1.68)^2]^{-1}$$

$$T_e = 767K$$

### 3. EXIT PRESSURE:

$$(P_e/P_t) = [1 + ((\gamma - 1)/2)M_e^2]^{-(\gamma/(\gamma - 1))}$$

$$P_e = 7.9 * 10^5 * [1 + ((1.4 - 1)/2) * (1.68)^2]^{-(1.4/(1.4 - 1))}$$

$$P_e = 164942.29Pa$$

### 4. THRUST:

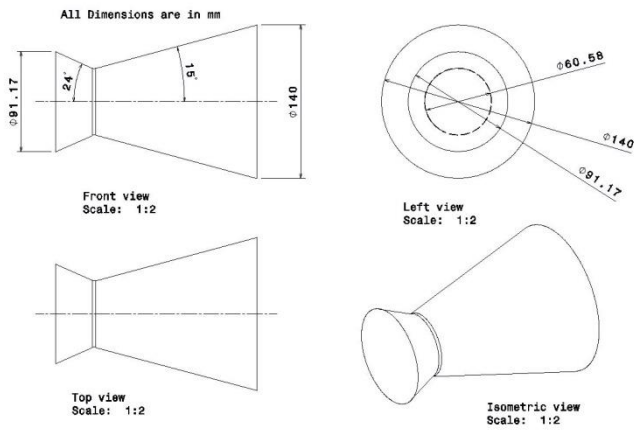
$$F = \dot{m}V_e + (P_e - P_o)A_e$$

$$F = (9.1 * 959) + (164942.29 - 0) * 0.015392$$

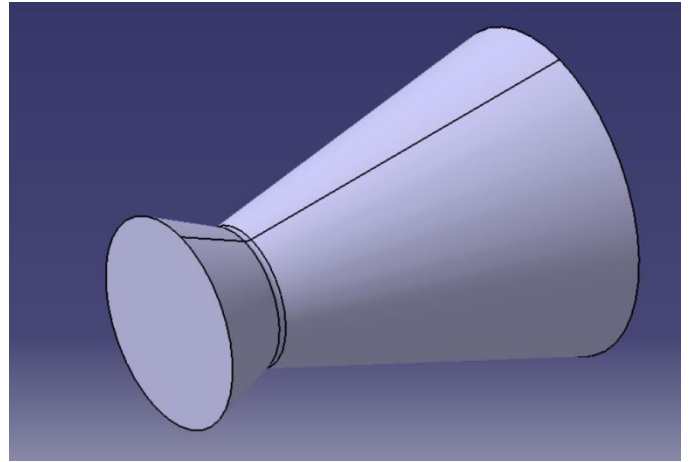
$$F = 11565.69N$$

## 4.4 CASE-1 CONVERGENT ANGLE 24°:

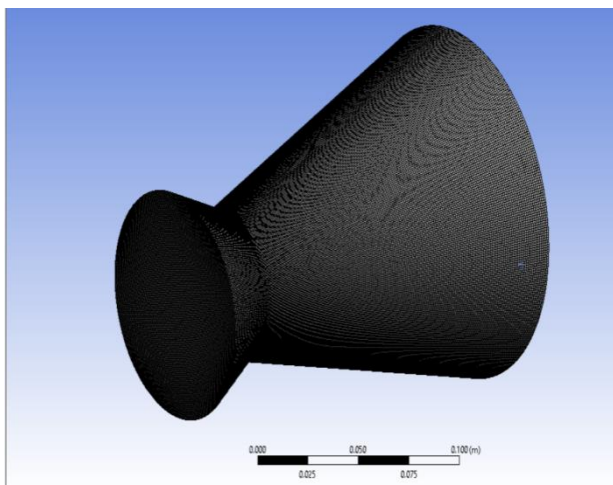
### NOZZLE DIMENSIONS:



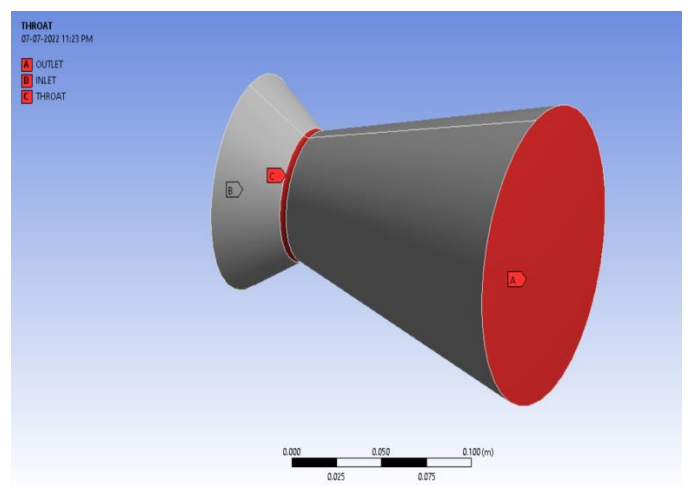
### 3-D GEOMETRY:



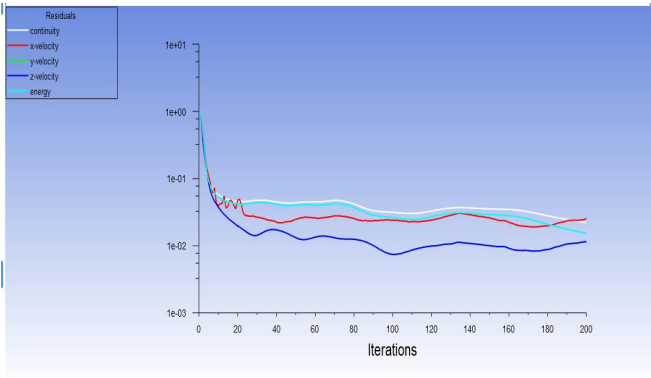
### MESHING:



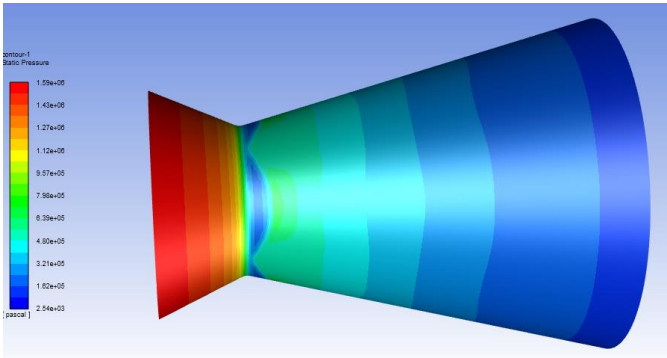
### NAMED SELECTION:



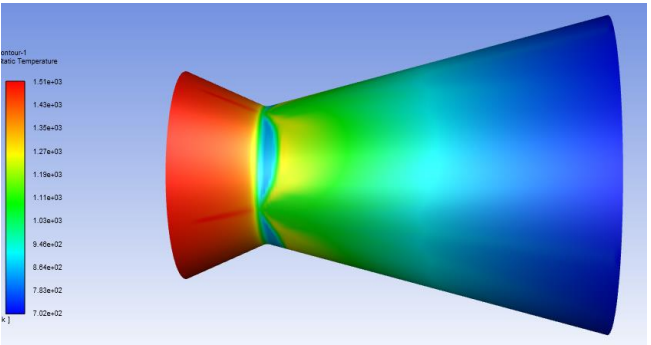
**RESIDUALS:**



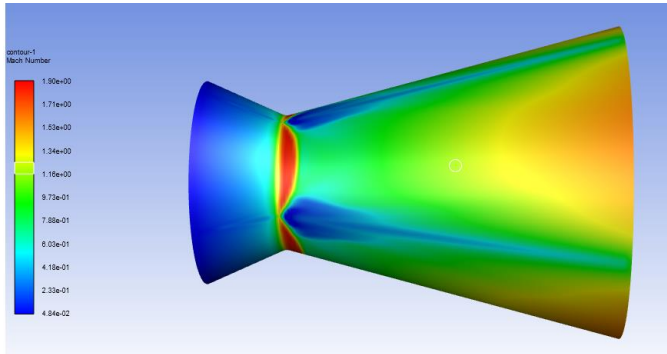
**PRESSURE CONTOUR:**



**TEMPERATURE CONTOUR:**



**MACH NUMBER CONTOUR:**





DETAILS:

**General**

Mesh

Scale...

Check

Report Quality

Display...

Solver

Type

☐ Pressure-Based

☒ Density-Based

Velocity Formulation

☒ Absolute

☐ Relative

Time

☒ Steady

☐ Transient

☐ Gravity

Units...

Help

**Models**

Models

Multiphase - Off

Energy - On

Viscous - Inviscid

Radiation - Off

Heat Exchanger - Off

Species - Off

Discrete Phase - Off

Acoustics - Off

Electric Potential - Off

Edit...

Help

Pressure Inlet

X

Zone Name

inlet

Momentum

Thermal

Radiation

Species

DPM

Multiphase

Potential

UDS

Reference Frame

Absolute

Gauge Total Pressure (pascal)

1600000

constant

Supersonic/Initial Gauge Pressure (pascal)

1500800

constant

Direction Specification Method

Normal to Boundary

OK

Cancel

Help

Create/Edit Materials

X

Name

air

Material Type

fluid

Order Materials by

☒ Name

☐ Chemical Formula

Chemical Formula

Fluent Fluid Materials

air

Fluent Database...

Mixture

User-Defined Database...

Properties

Density (kg/m3)

ideal-gas

Edit...

Cp (Specific Heat) (J/kg-K)

constant

Edit...

Molecular Weight (kg/mol)

constant

Edit...

1006.43

28.966

Change/Create

Delete

Close

Help

Pressure Inlet

X

Zone Name

inlet

Momentum

Thermal

Radiation

Species

DPM

Multiphase

Potential

UDS

Total Temperature (K)

1500

constant

OK

Cancel

Help

Pressure Outlet

X

Zone Name

outlet

Momentum

Thermal

Radiation

Species

DPM

Multiphase

Potential

UDS

Backflow Reference Frame

Absolute

Gauge Pressure (pascal)

10

constant

Pressure Profile Multiplier

1

Backflow Direction Specification Method

Normal to Boundary

Backflow Pressure Specification

Total Pressure

☐ Radial Equilibrium Pressure Distribution

☐ Average Pressure Specification

☐ Target Mass Flow Rate

Acoustic Wave Model

☒ Off

☐ Non Reflecting

OK

Cancel

Help

Pressure Outlet

Zone Name

Momentum Thermal Radiation Species DPM Multiphase Potential UDS

Backflow Total Temperature (k)  constant

OK Cancel Help

## Reference Values

Compute from

inlet

Reference Values

Area (m2)

Density (kg/m3)

Enthalpy (j/kg)

Length (m)

Pressure (pascal)

Temperature (k)

Velocity (m/s)

Ratio of Specific Heats

Reference Zone

solid-freeparts

Help

## Solution Initialization

Initialization Methods

- ☐ Hybrid Initialization  
☒ Standard Initialization

Compute from

inlet

Reference Frame

- ☒ Relative to Cell Zone  
☐ Absolute

Initial Values

Gauge Pressure (pascal)

X Velocity (m/s)

Y Velocity (m/s)

Z Velocity (m/s)

Temperature (k)

Initialize Reset Patch...

Reset DPM Sources Reset Statistics

## Run Calculation

Check Case...

Update Dynamic Mesh...

Options

☐ Data Sampling for Steady Statistics

Sampling Interval  
 Sampling Options...

Iterations Sampled

Number of Iterations

200

Reporting Interval

1

Profile Update Interval

1

☐ Solution Steering

Data File Quantities...

Acoustic Signals...

Acoustic Sources FFT...

Calculate

Help

## **ANALYTICAL METHOD ( 24° )**

### **1. EXIT MACH:**

$$M_e = V/a = 558/331 = 1.68$$

$$M_e = 1.68$$

### **2. EXIT TEMPERATURE:**

$$(T_e/T_t) = [1 + ((\gamma - 1)/2)M_e^2]^{-1}$$

$$T_e = 1200 * [1 + ((1.4 - 1)/2) * (1.68)^2]^{-1}$$

$$T_e = 767K$$

### **3. EXIT PRESSURE:**

$$(P_e/P_t) = [1 + ((\gamma - 1)/2)M_e^2]^{-(\gamma/(\gamma - 1))}$$

$$P_e = 7.9 * 10^5 * [1 + ((1.4 - 1)/2) * (1.68)^2]^{-(1.4/(1.4 - 1))}$$

$$P_e = 164942.29Pa$$

### **4. THRUST:**

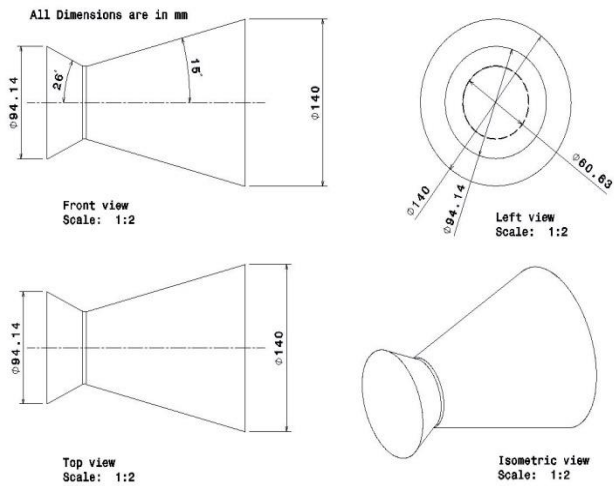
$$F = \dot{m}V_e + (P_e - P_o)A_e$$

$$F = (9.1 * 959) + (164942.29 - 0) * 0.015392$$

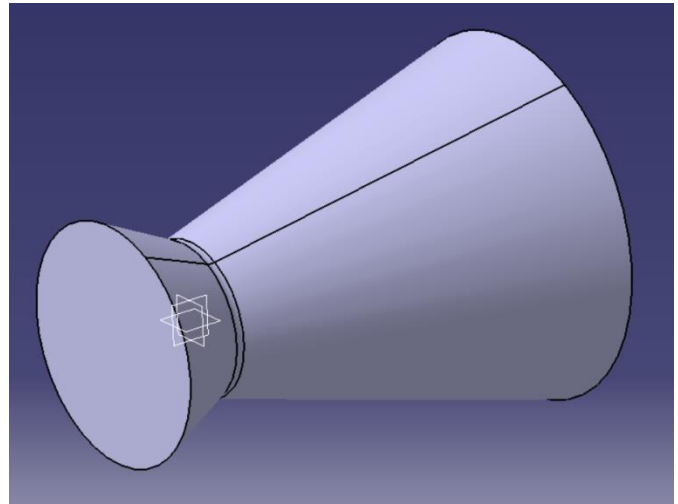
$$F = 11565.69N$$

## 4.5 CASE-2 CONVERGENT ANGLE 26°:

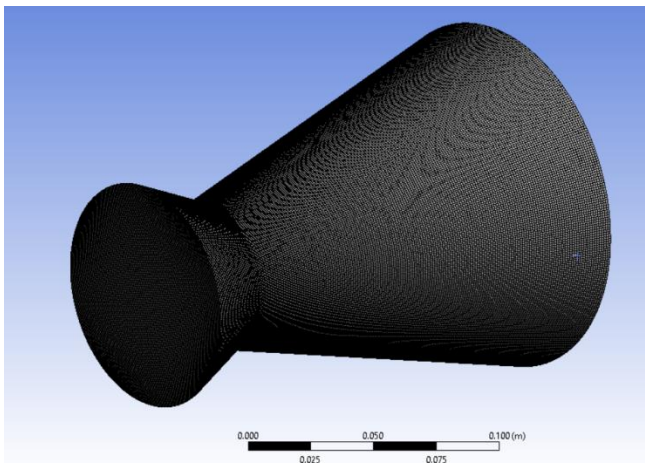
### NOZZLE DIMENSIONS:



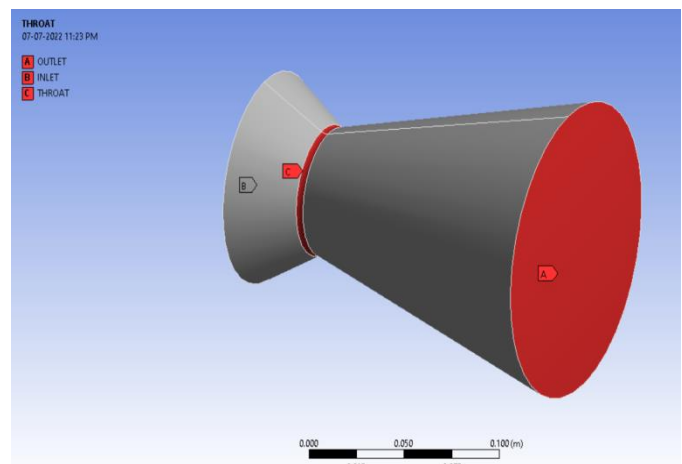
### 3-D GEOMETRY:



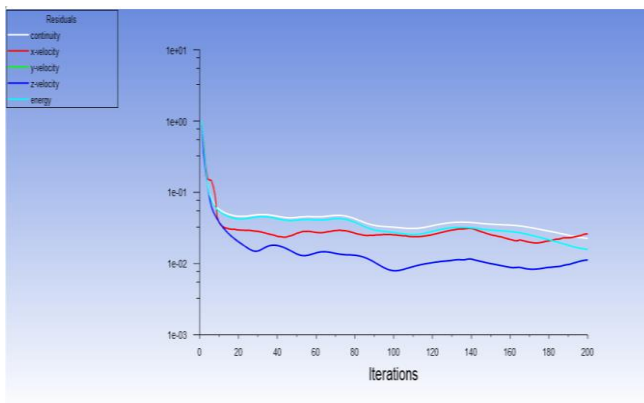
### MESHING:



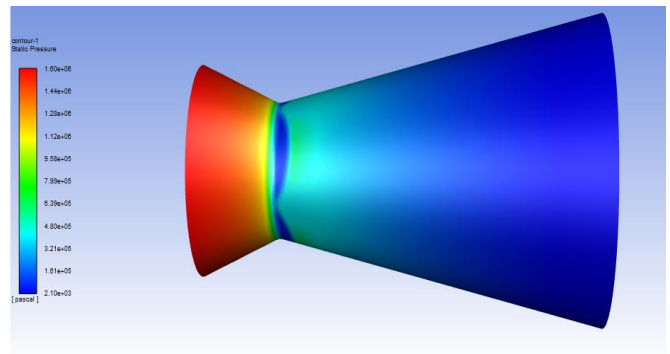
### NAMED SELECTION:



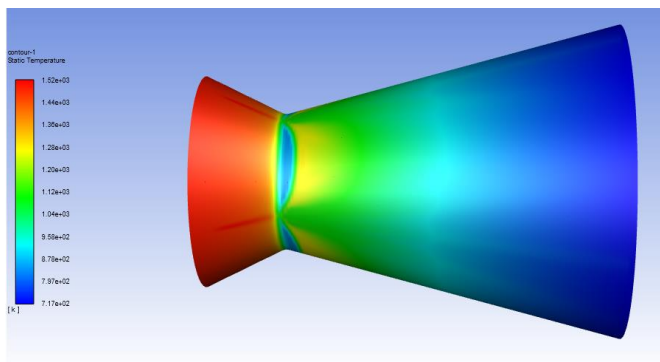
## RESIDUALS:



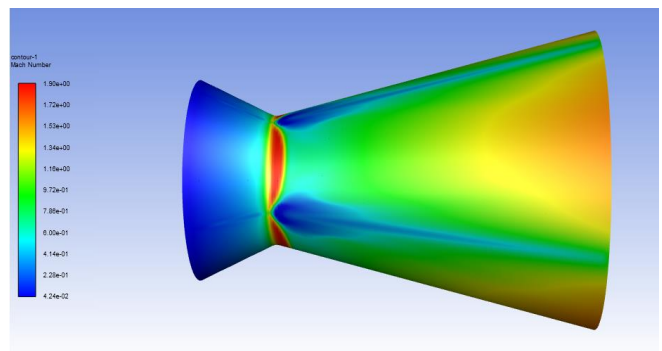
## PRESSURE CONTOUR:



## TEMPERATURE CONTOUR:



## MACH NUMBER CONTOUR:



DETAILS:

General

Mesh

Scale...

Check

Report Quality

Display...

Solver

Type

Pressure-Based

Density-Based

Velocity Formulation

Absolute

Relative

Time

Steady

Transient

Gravity

Units...

Help

Models

Models

Multiphase - Off

Energy - On

Viscous - Inviscid

Radiation - Off

Heat Exchanger - Off

Species - Off

Discrete Phase - Off

Acoustics - Off

Electric Potential - Off

Edit...

Help

Pressure Inlet

Zone Name

inlet

Momentum

Thermal

Radiation

Species

DPM

Multiphase

Potential

UDS

Reference Frame

Absolute

Gauge Total Pressure (pascal)

1600000

constant

Supersonic/Initial Gauge Pressure (pascal)

1500800

constant

Direction Specification Method

Normal to Boundary

OK

Cancel

Help

Create/Edit Materials

Name

air

Material Type

fluid

Order Materials by

Name

Chemical Formula

Chemical Formula

Fluent Fluid Materials

air

Fluent Database...

Mixture

none

User-Defined Database...

Properties

Density (kg/m3)

ideal-gas

Edit...

Cp (Specific Heat) (J/kg-K)

constant

Edit...

1006.43

Molecular Weight (kg/mol)

constant

Edit...

28.966

Change/Create

Delete

Close

Help

Pressure Inlet

Zone Name

inlet

Momentum

Thermal

Radiation

Species

DPM

Multiphase

Potential

UDS

Total Temperature (K)

1500

constant

OK

Cancel

Help

Pressure Outlet

Zone Name

outlet

Momentum

Thermal

Radiation

Species

DPM

Multiphase

Potential

UDS

Backflow Reference Frame

Absolute

Gauge Pressure (pascal)

10

constant

Pressure Profile Multiplier

1

Backflow Direction Specification Method

Normal to Boundary

Backflow Pressure Specification

Total Pressure

Radial Equilibrium Pressure Distribution

Average Pressure Specification

Target Mass Flow Rate

Acoustic Wave Model

Off

Non Reflecting

OK

Cancel

Help

Pressure Outlet

Zone Name  
outlet

Momentum Thermal Radiation Species DPM Multiphase Potential UDS

Backflow Total Temperature (k) 300 constant

OK Cancel Help

### Reference Values

Compute from

inlet

#### Reference Values

Area (m2) 1

Density (kg/m3) 3.549933

Enthalpy (j/kg) 1509645

Length (m) 1

Pressure (pascal) 1500800

Temperature (k) 1472.867

Velocity (m/s) 233.7004

Ratio of Specific Heats 1.4

Reference Zone

solid-freeparts

Help

### Solution Initialization

Initialization Methods

- ☐ Hybrid Initialization
- ☒ Standard Initialization

Compute from

inlet

Reference Frame

- ☒ Relative to Cell Zone
- ☐ Absolute

Initial Values

Gauge Pressure (pascal)

1500800

X Velocity (m/s)

233.7004

Y Velocity (m/s)

1.368473e-15

Z Velocity (m/s)

2.297544e-15

Temperature (k)

1472.867

Initialize

Reset

Patch...

Reset DPM Sources

Reset Statistics

### Run Calculation

Check Case...

Update Dynamic Mesh...

Options

☐ Data Sampling for Steady Statistics

Sampling Interval

1

Sampling Options...

Iterations Sampled

0

Number of Iterations

200

Reporting Interval

1

Profile Update Interval

1

☐ Solution Steering

Data File Quantities...

Acoustic Signals...

Acoustic Sources FFT...

Calculate

Help

## **ANALYTICAL METHOD ( 26° )**

### **1. EXIT MACH:**

$$M_e = V/a = 554.69/331 = 1.67$$

$$M_e = 1.67$$

### **2. EXIT TEMPERATURE:**

$$(T_e/T_t) = [1 + ((\gamma - 1)/2)M_e^2]^{-1}$$

$$T_e = 1200 * [1 + ((1.4 - 1)/2) * (1.67)^2]^{-1}$$

$$T_e = 770.32K$$

### **3. EXIT PRESSURE:**

$$(P_e/P_t) = [1 + ((\gamma - 1)/2)M_e^2]^{-(\gamma/(\gamma - 1))}$$

$$P_e = 7.95 * 10^5 * [1 + ((1.4 - 1)/2) * (1.67)^2]^{-(1.4/(1.4 - 1))}$$

$$P_e = 165986.29Pa$$

### **4. THRUST:**

$$F = \dot{m}V_e + (P_e - P_o)A_e$$

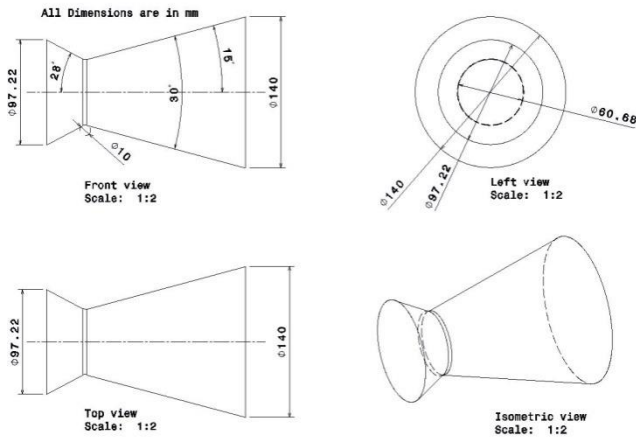
$$F = (9.7 * 960) + (165986.29 - 0) * 0.015392$$

$$F = 11867N$$

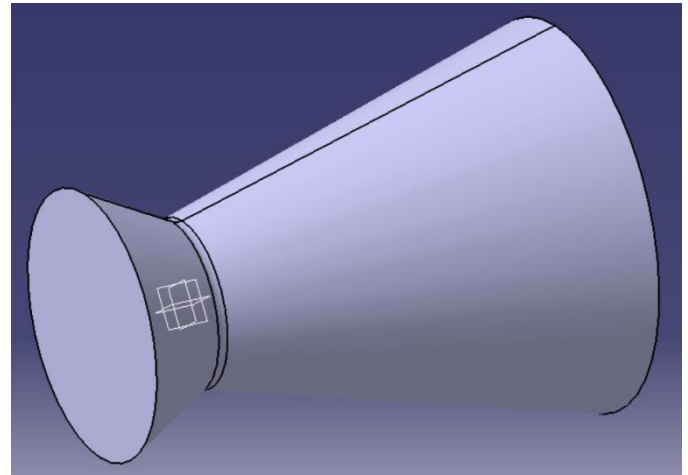


## 4.6 CASE-3 CONVERGENT ANGLE 28°:

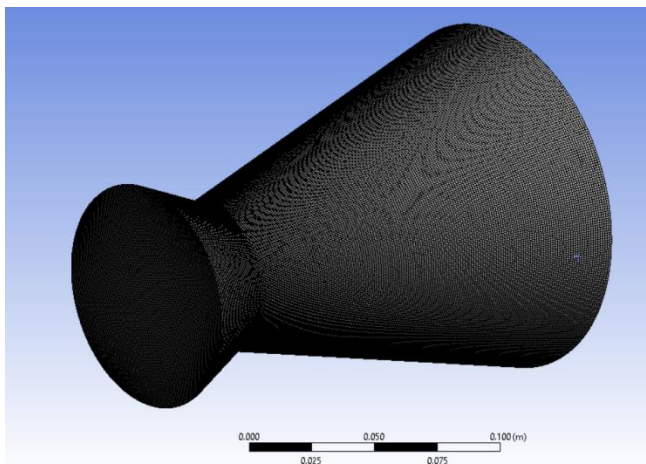
### NOZZLE DIMENSIONS:



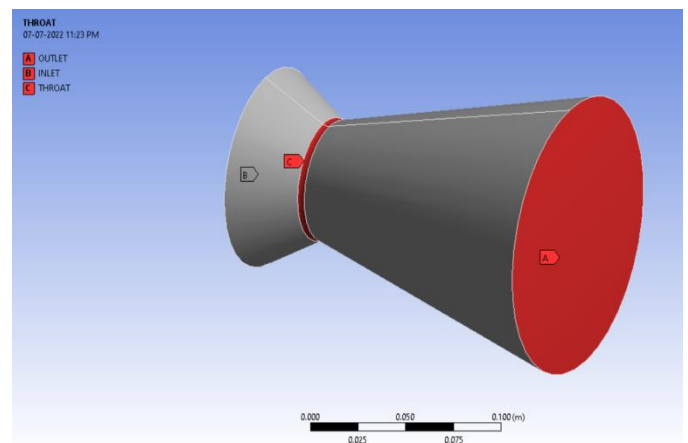
### 3-D GEOMETRY:



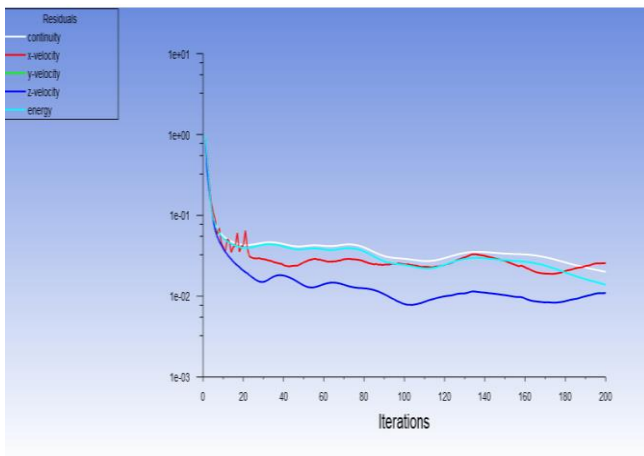
### MESHING:



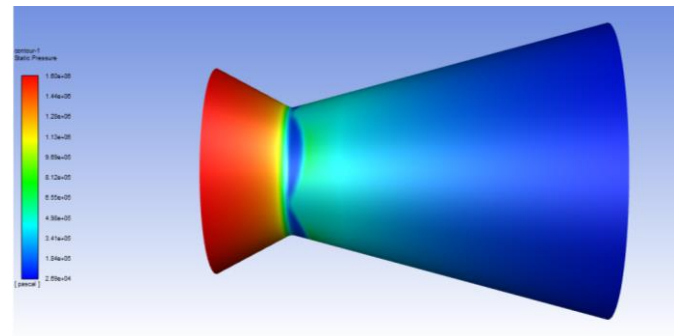
### NAMED SELECTION:



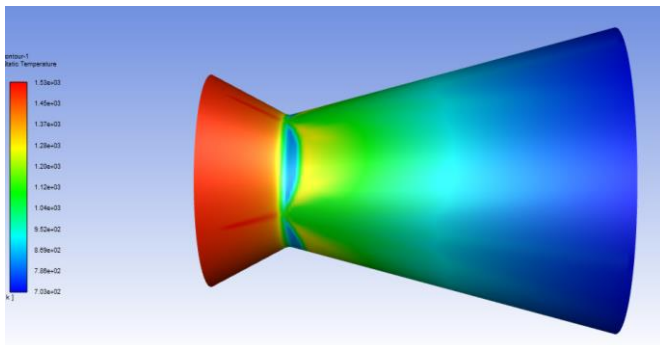
## RESIDUALS:



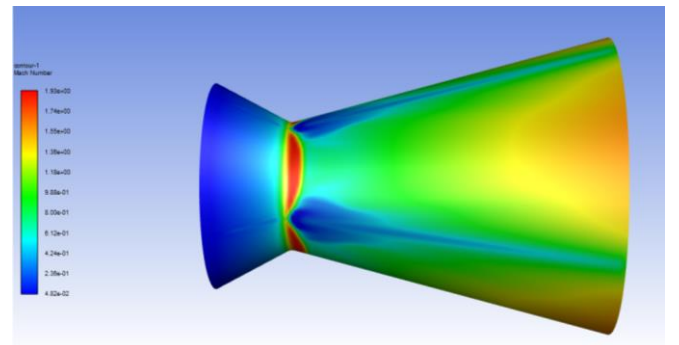
## PRESSURE CONTOUR:



## TEMPERATURE CONTOUR:



## MACH NUMBER CONTOUR:



DETAILS:

**General**

Mesh

Scale...

Check

Report Quality

Display...

Solver

Type

☐ Pressure-Based

☒ Density-Based

Velocity Formulation

☒ Absolute

☐ Relative

Time

☒ Steady

☐ Transient

☐ Gravity

Units...

Help

**Models**

Models

Multiphase - Off

Energy - On

Viscous - Inviscid

Radiation - Off

Heat Exchanger - Off

Species - Off

Discrete Phase - Off

Acoustics - Off

Electric Potential - Off

Edit...

Help

Pressure Inlet

X

Zone Name

inlet

Momentum

Thermal

Radiation

Species

DPM

Multiphase

Potential

UDS

Reference Frame

Absolute

Gauge Total Pressure (pascal)

1600000

constant

Supersonic/Initial Gauge Pressure (pascal)

1500800

constant

Direction Specification Method

Normal to Boundary

OK

Cancel

Help

Create/Edit Materials

X

Name

air

Material Type

fluid

Order Materials by

☒ Name

☐ Chemical Formula

Chemical Formula

Fluent Fluid Materials

air

Fluent Database...

Mixture

none

User-Defined Database...

Properties

Density (kg/m3)

ideal-gas

Edit...

Cp (Specific Heat) (J/kg-K)

constant

Edit...

Molecular Weight (kg/mol)

constant

Edit...

1006.43

28.966

Change/Create

Delete

Close

Help

Pressure Inlet

X

Zone Name

inlet

Momentum

Thermal

Radiation

Species

DPM

Multiphase

Potential

UDS

Total Temperature (K)

1500

constant

OK

Cancel

Help

Pressure Outlet

X

Zone Name

outlet

Momentum

Thermal

Radiation

Species

DPM

Multiphase

Potential

UDS

Backflow Reference Frame

Absolute

Gauge Pressure (pascal)

10

constant

Pressure Profile Multiplier

1

P

Backflow Direction Specification Method

Normal to Boundary

Backflow Pressure Specification

Total Pressure

☐ Radial Equilibrium Pressure Distribution

☐ Average Pressure Specification

☐ Target Mass Flow Rate

Acoustic Wave Model

☒ Off

☐ Non Reflecting

OK

Cancel

Help

Pressure Outlet

Zone Name  
outlet

Momentum Thermal Radiation Species DPM Multiphase Potential UDS

Backflow Total Temperature (K) 300 constant

OK Cancel Help

## Reference Values

Compute from

inlet

### Reference Values

Area (m2) 1

Density (kg/m3) 3.549933

Enthalpy (J/kg) 1509645

Length (m) 1

Pressure (pascal) 1500800

Temperature (K) 1472.867

Velocity (m/s) 233.7004

Ratio of Specific Heats 1.4

Reference Zone

solid-freeparts

Help

## Solution Initialization

Initialization Methods

- ☐ Hybrid Initialization
- ☒ Standard Initialization

Compute from

inlet

Reference Frame

- ☒ Relative to Cell Zone
- ☐ Absolute

Initial Values

Gauge Pressure (pascal)  
1500800

X Velocity (m/s)  
233.7004

Y Velocity (m/s)  
1.368473e-15

Z Velocity (m/s)  
2.297544e-15

Temperature (K)  
1472.867

Initialize Reset Patch...

Reset DPM Sources Reset Statistics

## Run Calculation

Check Case...

Update Dynamic Mesh...

Options

☐ Data Sampling for Steady Statistics

Sampling Interval

1

Sampling Options...

Iterations Sampled

0

Number of Iterations

200

Reporting Interval

1

Profile Update Interval

1

☐ Solution Steering

Data File Quantities...

Acoustic Signals...

Acoustic Sources FFT...

Calculate

Help

## **ANALYTICAL METHOD ( 28° )**

### **1. EXIT MACH:**

$$M_e = V/a = 563.54/331 = 1.70$$

$$M_e = 1.70$$

### **2. EXIT TEMPERATURE:**

$$(T_e/T_t) = [1 + ((\gamma - 1)/2)M_e^2]^{-1}$$

$$T_e = 1250 * [1 + ((1.4 - 1)/2) * (1.70)^2]^{-1}$$

$$T_e = 792.125K$$

### **3. EXIT PRESSURE:**

$$(P_e/P_t) = [1 + ((\gamma - 1)/2)M_e^2]^{-(\gamma/(\gamma - 1))}$$

$$P_e = 848000 * [1 + ((1.4 - 1)/2) * (1.7)^2]^{-(1.4/(1.4 - 1))}$$

$$P_e = 171799.28Pa$$

### **4. THRUST:**

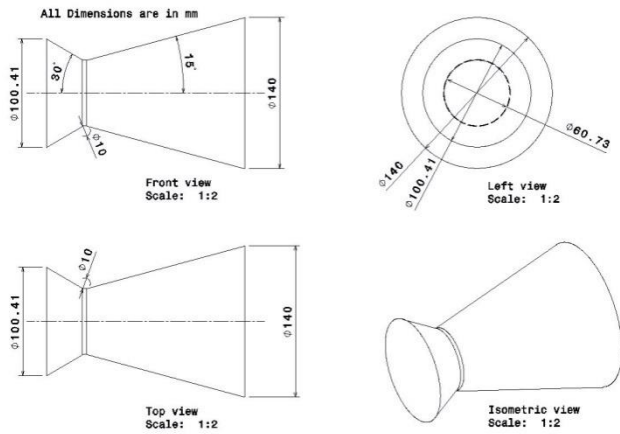
$$F = \dot{m}V_e + (P_e - P_o)A_e$$

$$F = (9.13 * 779) + (171799.28 - 0) * 0.015392$$

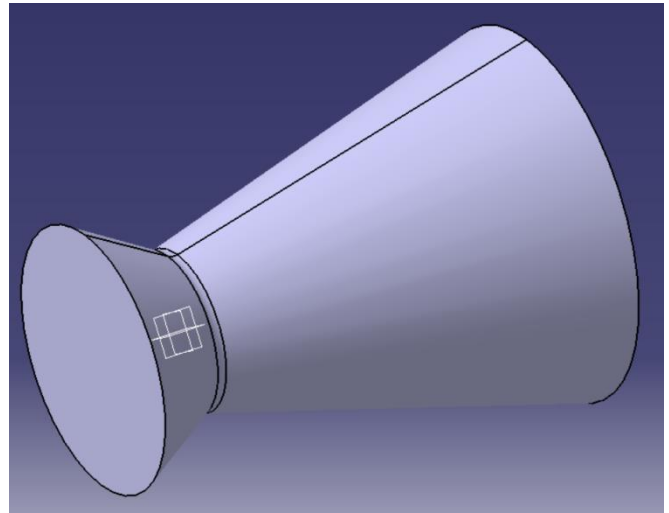
$$F = 9740.79N$$

## 4.7 CASE-4 CONVERGENT ANGLE 30°:

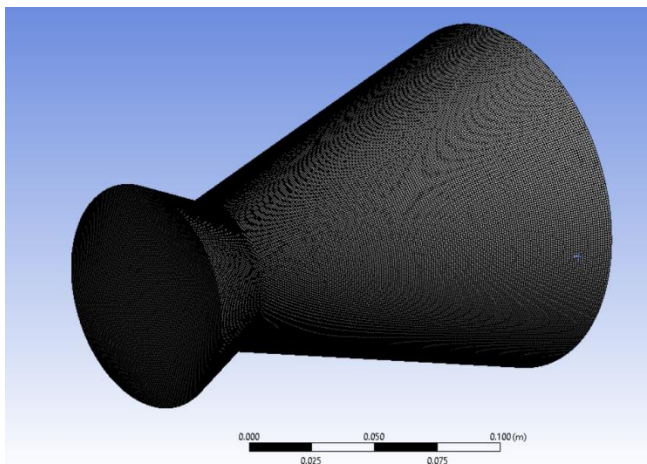
### NOZZLE DIMENSIONS:



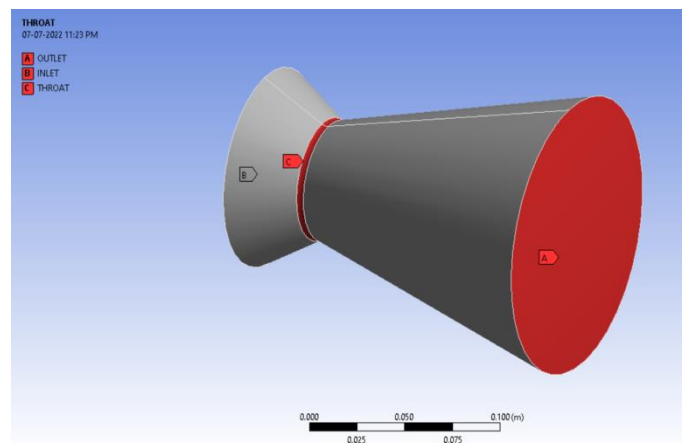
### 3-D GEOMETRY:



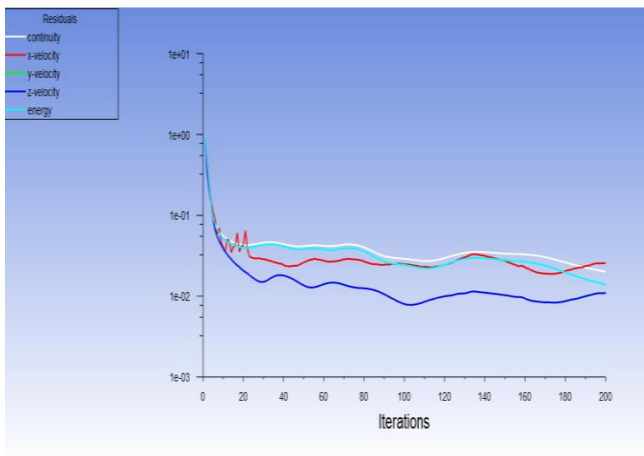
### MESHING:



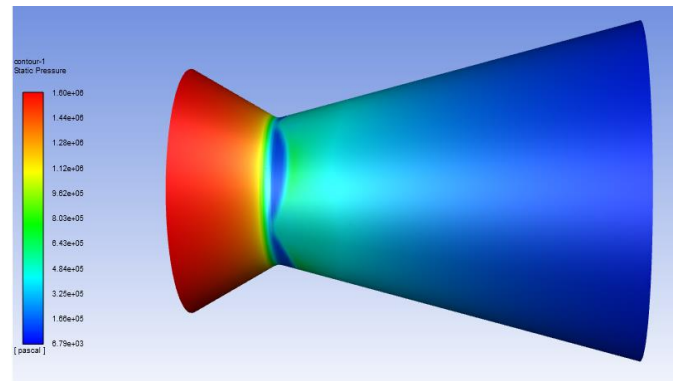
### NAMED SELECTION:



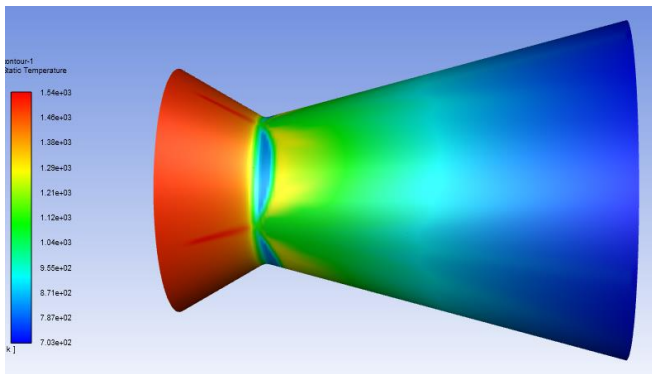
## RESIDUALS:



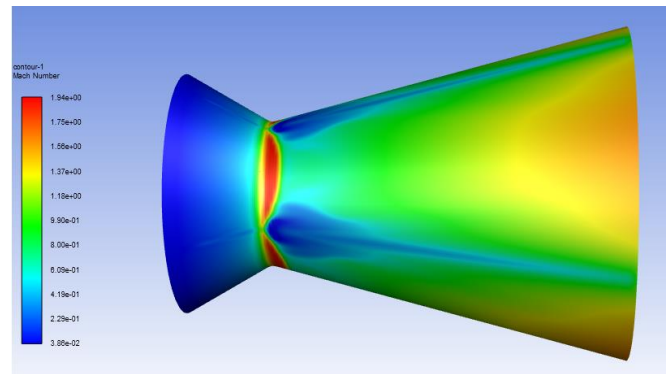
## PRESSURE CONTOUR:



## TEMPERATURE CONTOUR:



## MACH NUMBER CONTOUR:



DETAILS:

**General**

Mesh

Scale...

Check

Report Quality

Display...

Solver

Type

☐ Pressure-Based

☒ Density-Based

Velocity Formulation

☒ Absolute

☐ Relative

Time

☒ Steady

☐ Transient

☐ Gravity

Units...

Help

**Models**

Models

Multiphase - Off

Energy - On

Viscous - Inviscid

Radiation - Off

Heat Exchanger - Off

Species - Off

Discrete Phase - Off

Acoustics - Off

Electric Potential - Off

Edit...

Help

Pressure Inlet

X

Zone Name

inlet

Momentum

Thermal

Radiation

Species

DPM

Multiphase

Potential

UDS

Reference Frame

Absolute

Gauge Total Pressure (pascal)

1600000

constant

Supersonic/Initial Gauge Pressure (pascal)

1500800

constant

Direction Specification Method

Normal to Boundary

OK

Cancel

Help

Create/Edit Materials

X

Name

air

Material Type

fluid

Order Materials by

☒ Name

☐ Chemical Formula

Chemical Formula

Fluent Fluid Materials

air

Fluent Database...

Mixture

none

User-Defined Database...

Properties

Density (kg/m3)

ideal-gas

Edit...

Cp (Specific Heat) (J/kg-K)

constant

Edit...

Molecular Weight (kg/mol)

constant

Edit...

1006.43

28.966

Change/Create

Delete

Close

Help

Pressure Inlet

X

Zone Name

inlet

Momentum

Thermal

Radiation

Species

DPM

Multiphase

Potential

UDS

Total Temperature (K)

1500

constant

OK

Cancel

Help

Pressure Outlet

X

Zone Name

outlet

Momentum

Thermal

Radiation

Species

DPM

Multiphase

Potential

UDS

Backflow Reference Frame

Absolute

Gauge Pressure (pascal)

10

constant

Pressure Profile Multiplier

1

P

Backflow Direction Specification Method

Normal to Boundary

Backflow Pressure Specification

Total Pressure

☐ Radial Equilibrium Pressure Distribution

☐ Average Pressure Specification

☐ Target Mass Flow Rate

Acoustic Wave Model

☒ Off

☐ Non Reflecting

OK

Cancel

Help



Pressure Outlet

Zone Name  
outlet

Momentum Thermal Radiation Species DPM Multiphase Potential UDS

Backflow Total Temperature (k) 300 constant

OK Cancel Help

## Reference Values

Compute from

inlet

### Reference Values

Area (m2) 1

Density (kg/m3) 3.549933

Enthalpy (j/kg) 1509645

Length (m) 1

Pressure (pascal) 1500800

Temperature (k) 1472.867

Velocity (m/s) 233.7004

Ratio of Specific Heats 1.4

Reference Zone

solid-freeparts

Help

## Solution Initialization

Initialization Methods

- ☐ Hybrid Initialization
- ☒ Standard Initialization

Compute from

inlet

Reference Frame

- ☒ Relative to Cell Zone
- ☐ Absolute

Initial Values

Gauge Pressure (pascal)  
1500800

X Velocity (m/s)  
233.7004

Y Velocity (m/s)  
1.368473e-15

Z Velocity (m/s)  
2.297544e-15

Temperature (k)  
1472.867

Initialize Reset Patch...

Reset DPM Sources Reset Statistics

## Run Calculation

Check Case...

Update Dynamic Mesh...

Options

☐ Data Sampling for Steady Statistics

Sampling Interval

1

Sampling Options...

Iterations Sampled 0

Number of Iterations

200

Reporting Interval

1

Profile Update Interval

1

☐ Solution Steering

Data File Quantities...

Acoustic Signals...

Acoustic Sources FFT...

Calculate

Help

## **ANALYTICAL METHOD ( 30° )**

### **1. EXIT MACH:**

$$M_e = V/a = 553/331 = 1.67$$

$$M_e = 1.67$$

### **2. EXIT TEMPERATURE:**

$$(T_e/T_t) = [1 + ((\gamma - 1)/2)M_e^2]^{-1}$$

$$T_e = 1299 * [1 + ((1.4 - 1)/2) * (1.67)^2]^{-1}$$

$$T_e = 833.82K$$

### **3. EXIT PRESSURE:**

$$(P_e/P_t) = [1 + ((\gamma - 1)/2)M_e^2]^{-(\gamma/(\gamma - 1))}$$

$$P_e = 858062 * [1 + ((1.4 - 1)/2) * (1.67)^2]^{-(1.4/(1.4 - 1))}$$

$$P_e = 181864.20Pa$$

### **4. THRUST:**

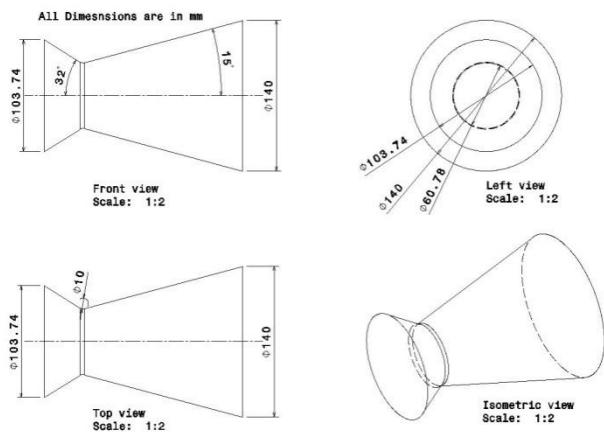
$$F = \dot{m}V_e + (P_e - P_o)A_e$$

$$F = (9.14 * 963) + (181864.20 - 0) * 0.015392$$

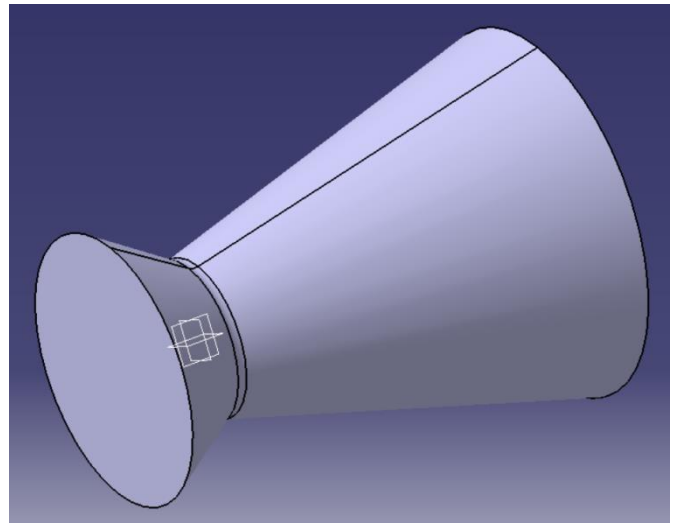
$$F = 11584.3N$$

## 4.8 CASE-5 CONVERGENT ANGLE 32°:

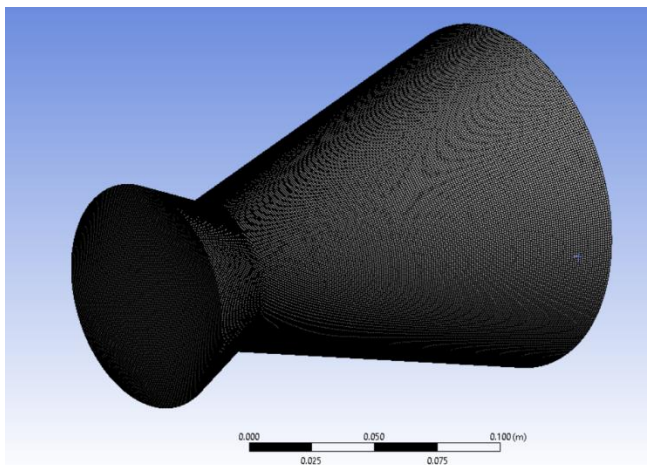
### NOZZLE DIMENSION:



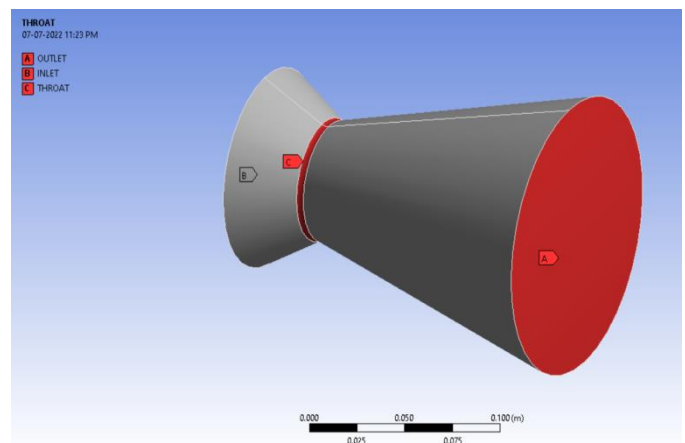
### 3-D GEOMETRY:



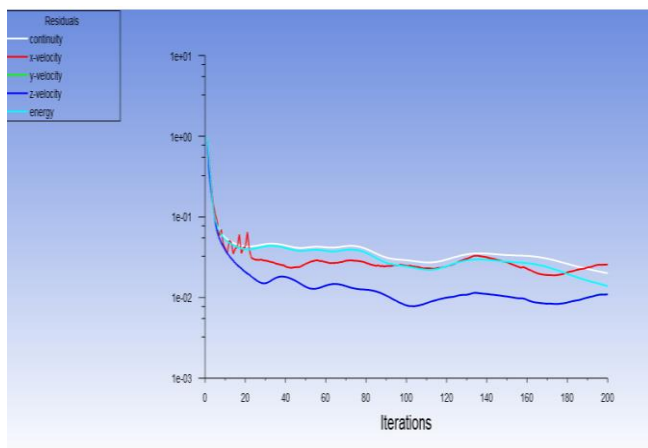
### MESHING:



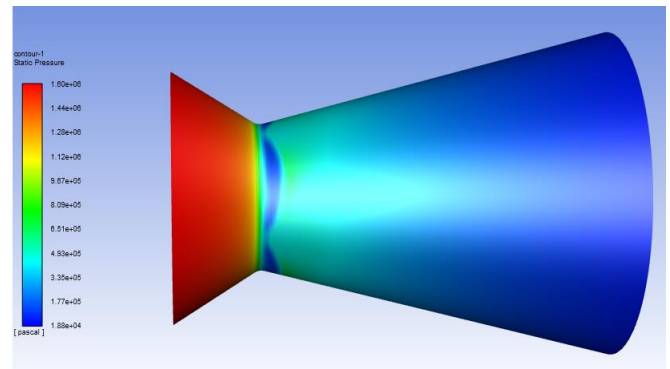
### NAMED SELECTION:



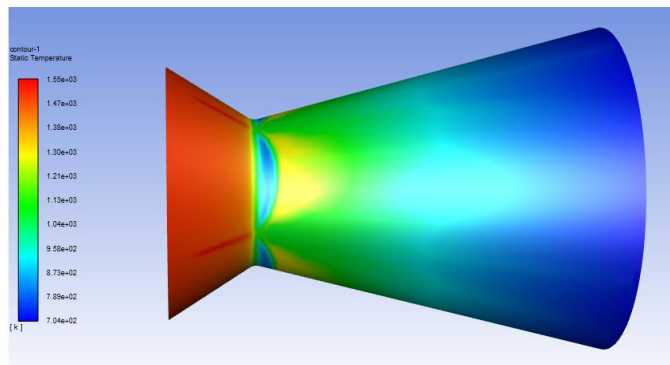
## RESIDUALS:



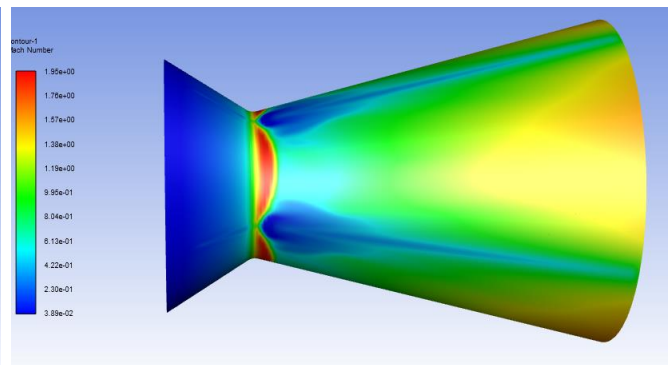
## PRESSURE CONTOUR:



## TEMPERATURE CONTOUR:



## MACH NUMBER CONTOUR:



DETAILS:

General

Mesh

Scale...

Check

Report Quality

Display...

Solver

Type

☐ Pressure-Based

☒ Density-Based

Velocity Formulation

☒ Absolute

☐ Relative

Time

☒ Steady

☐ Transient

☐ Gravity

Units...

Help

Models

Multiphase - Off

Energy - On

Viscous - Inviscid

Radiation - Off

Heat Exchanger - Off

Species - Off

Discrete Phase - Off

Acoustics - Off

Electric Potential - Off

Edit...

Help

Pressure Inlet

Zone Name

inlet

Momentum

Thermal

Radiation

Species

DPM

Multiphase

Potential

UDS

Reference Frame

Absolute

Gauge Total Pressure (pascal)

1600000

constant

Supersonic/Initial Gauge Pressure (pascal)

1500800

constant

Direction Specification Method

Normal to Boundary

OK

Cancel

Help

Create/Edit Materials

Name

air

Material Type

Fluid

Order Materials by

☒ Name

☐ Chemical Formula

Chemical Formula

Fluent Fluid Materials

air

Fluent Database...

Mixture

none

User-Defined Database...

Properties

Density (kg/m3)

ideal-gas

Edit...

Cp (Specific Heat) (J/kg-K)

constant

Edit...

1006.43

Molecular Weight (kg/mol)

constant

Edit...

28.966

Change/Create

Delete

Close

Help

Pressure Inlet

Zone Name

inlet

Momentum

Thermal

Radiation

Species

DPM

Multiphase

Potential

UDS

Total Temperature (K)

1500

constant

OK

Cancel

Help

Pressure Outlet

Zone Name

outlet

Momentum

Thermal

Radiation

Species

DPM

Multiphase

Potential

UDS

Backflow Reference Frame

Absolute

Gauge Pressure (pascal)

10

constant

Pressure Profile Multiplier

1

Backflow Direction Specification Method

Normal to Boundary

Backflow Pressure Specification

Total Pressure

☐ Radial Equilibrium Pressure Distribution

☐ Average Pressure Specification

☐ Target Mass Flow Rate

Acoustic Wave Model

☒ Off

☐ Non Reflecting

OK

Cancel

Help

Pressure Outlet

Zone Name

outlet

Momentum

Thermal

Radiation

Species

DPM

Multiphase

Potential

UDS

Backflow Total Temperature (k)

300

constant

OK

Cancel

Help

## Reference Values

Compute from

inlet

Reference Values

Area (m2)

1

Density (kg/m3)

3.549933

Enthalpy (j/kg)

1509645

Length (m)

1

Pressure (pascal)

1500800

Temperature (k)

1472.867

Velocity (m/s)

233.7004

Ratio of Specific Heats

1.4

Reference Zone

solid-freeparts

Help

## Solution Initialization

Initialization Methods

- ☐ Hybrid Initialization  
☒ Standard Initialization

Compute from

inlet

Reference Frame

- ☒ Relative to Cell Zone  
☐ Absolute

Initial Values

Gauge Pressure (pascal)

1500800

X Velocity (m/s)

233.7004

Y Velocity (m/s)

1.368473e-15

Z Velocity (m/s)

2.297544e-15

Temperature (k)

1472.867

Initialize

Reset

Patch...

Reset DPM Sources

Reset Statistics

## Run Calculation

Check Case...

Update Dynamic Mesh...

Options

☐ Data Sampling for Steady Statistics

Sampling Interval

1

Sampling Options...

Iterations Sampled

0

Number of Iterations

200

Reporting Interval

1

Profile Update Interval

1

☐ Solution Steering

Data File Quantities...

Acoustic Signals...

Acoustic Sources FFT...

Calculate

Help

## **ANALYTICAL METHOD ( 32° )**

### **1. EXIT MACH:**

$$M_e = V/a = 562.3/331 = 1.69$$

$$M_e = 1.69$$

### **2. EXIT TEMPERATURE:**

$$(T_e/T_t) = [1 + ((\gamma - 1)/2)M_e^2]^{-1}$$

$$T_e = 1250 * [1 + ((1.4 - 1)/2) * (1.69)^2]^{-1}$$

$$T_e = 795.5K$$

### **3. EXIT PRESSURE:**

$$(P_e/P_t) = [1 + ((\gamma - 1)/2)M_e^2]^{-(\gamma/(\gamma - 1))}$$

$$P_e = 867885 * [1 + ((1.4 - 1)/2) * (1.69)^2]^{-(1.4/(1.4 - 1))}$$

$$P_e = 178497.72Pa$$

### **4. THRUST:**

$$F = \dot{m}V_e + (P_e - P_o)A_e$$

$$F = (9.15 * 964) + (178497.72 - 0) * 0.015392$$

$$F = 11569.29N$$

## 4.9 COMPARISON OF RESULTS FOR VARIOUS CASES

**Table 4.1:** Comparison of Results for Various Cases

CASE	CONVERGENT ANGLE	PARAMETERS	CFD RESULTS	THEORETICAL RESULTS	ERROR %
1	24°	EXIT MACH	1.6	1.68	4.76
		EXIT TEMPERATURE	777.78K	767K	1.38
		EXIT PRESSURE	156083Pa	164942.29Pa	5.37
		THRUST	12719N	11565.69N	9.06
2	26°	EXIT MACH	1.7	1.67	1.76
		EXIT TEMPERATURE	779K	770.32K	1.11
		EXIT PRESSURE	157922Pa	165986.29Pa	4.85
		THRUST	13610.7N	11867N	12.81
3	28°	EXIT MACH	1.6	1.7	5.88
		EXIT TEMPERATURE	779.5K	792.125K	1.59
		EXIT PRESSURE	156498Pa	171799.28Pa	8.9
		THRUST	10427.3N	9740.79N	6.58
4	30°	EXIT MACH	1.6	1.67	4.19
		EXIT TEMPERATURE	780.6K	833.82K	6.38
		EXIT PRESSURE	156660Pa	181864.2Pa	13.85
		THRUST	12656.5N	11584.3N	8.47
5	32°	EXIT MACH	1.58	1.69	6.5
		EXIT TEMPERATURE	775K	795.5K	2.57
		EXIT PRESSURE	156783Pa	178497.72Pa	12.16
		THRUST	12640N	11569.29N	8.47



## **CHAPTER – 5**

### **CONCLUSION AND FUTURE WORK**

#### **5.1 CONCLUSION**

We have discussed the fundamental concepts behind a converging- diverging nozzle for rocket in this Thesis. Through this research and analysis, we were able to determine the values of variation in nozzle parameters using both theoretical formulae and CFD. Thus, we draw the conclusion that the values obtained using both of these methods are consistent.

A rocket nozzle with a convergent angle of  $26^\circ$  is the most suitable and offers the optimum mach number and thrust. According to the numerical and flow characteristics of the Nozzle with various angles achieved in this project. This optimal design when implemented can result in increased nozzle performance and as a result, an improved propulsion system performance can be achieved. According to the findings of the study, the mach number and thrust at the exit of the nozzle are respectively 1.7 and 13610.7N when the convergent angle is  $26^\circ$ .

#### **5.2 FUTURE SCOPE**





- Structural analysis of the nozzle material can be carried out in future.
- Different combination of nozzles can be considered for the CFD analysis.
- Conducting an experimental investigation.
- Comparing and analyzing the outcomes of the numerical technique with the experiments.

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### ABSTRACT

A nozzle in a rocket engine propels hot exhaust to create thrust in accordance with Newton's third law of motion. The amount of thrust produced by the engine is determined by the mass flow rate through the engine, the exit velocity of the flow, and the pressure at the engine's exit. The value of these three flow variables is governed by the rocket nozzle design. In addition, the design of the nozzle is an important consideration when attempting to accomplish a maximum Mach number or supersonic speed.

Rocket nozzles typically consist of a fixed convergent part followed by a fixed divergent section. A convergent-divergent, or CD, nozzle is the name given to this arrangement of nozzles. The hot exhaust from the combustion chamber converges on the nozzle's minimum area, or throat, or a CD rocket nozzle. The high temperatures, high pressure, and low velocity gas are all converted into high velocity, low pressure gas at the exit by this nozzle.

Numerical simulations of supersonic flow through the rocket's nozzle have been performed. The goal of this study is to model a 3D divergent-convergent nozzle and examine the variations in flow parameters (static pressure, static temperature, and Mach number) brought on by altering the convergent angle of the nozzle (24, 26, 28, 30, and 32 degrees) while keeping the same throat and outlet diameters.

In order to determine the appropriate convergent angle, the flow characteristics variation at the nozzle exit is investigated. The Mach number and thrust at the nozzle's exit are found to be 1.7 and 13800.7N from the analysis for a convergent angle of 26°. When all of the converging angle results were taken into account, 26° produced the highest Thrust and Mach number, which will enhance the nozzle's performance and, as a result, increase the power and efficiency of a propulsion system.

## A nozzle in a rocket engine

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