

Family Name (Print):

ID: 700-

Given Name:

Score: /100

*Please provide complete work to get full credit.*

1. (10 pts) Write a regular expression that generates the same language as the following grammar:

$$S \rightarrow aSA \mid B$$

$$A \rightarrow c$$

$$B \rightarrow Bb \mid b$$

**Solution:**

2. (10 pts) Write a context-free grammar that generates the same language as the following regular expression:

$$(a \mid b)(a \mid cb)^+(c \mid \varepsilon)$$

**Solution:**

3. (10 pts) Remove the left recursion:

$$exp \rightarrow exp \text{ addop } term \mid term$$

**Solution:**

4. (10 pts) Left factor the grammar:

$$lexp \rightarrow atom \text{ list } \mid atom \text{ term1 term2 }$$

**Solution:**

5. (10 pts) Given CF grammar  $S \rightarrow aSS \mid \varepsilon$ .
- 1) Provide a left-most derivation for string  $aa$ .
  - 2) Show the grammar is ambiguous.

**Solution:**

1)

2)

6. (15 pts) Show the LL(1) parsing action table, according to the LL(1) parsing table shown below, to recognize the string  $()()$ .

M[N, T]	(	)	\$
S	$S \rightarrow (S)S$	$S \rightarrow \varepsilon$	$S \rightarrow \varepsilon$

**Solution:**

	Parsing Stack	Input	Action
1	\$	\$	
2	\$	\$	
3	\$	\$	
4	\$	\$	
5	\$	\$	
6	\$	\$	
7	\$	\$	
8	\$	\$	
9	\$	\$	
10	\$	\$	
11	\$	\$	
12	\$	\$	
13	\$	\$	
14	\$	\$	
15	\$	\$	
16	\$	\$	

7. (10 pts) Given grammar:

$$T \rightarrow A a \mid b$$

$$A \rightarrow A c \mid T d \mid \varepsilon$$

Remove left recursion.

**Solution:**

8. This question is on SLR(1) parsing (shift-reduce). Given the context-free grammar:

$$S \rightarrow (AS) \mid \varepsilon$$

$$A \rightarrow S \mid \varepsilon$$

- 1) (10 pts) Convert the given grammar to an augmented grammar with new start symbol and list all LR(0) items.

**Solution:**

**Augmented grammar:**

**LR(0) items:**

- 2) (15 pts) Construct the NFA of LR(0) items for the grammar.  
**Solution:**

- 3) (15 pts) Construct the DFA from the above NFA.  
**Solution:**

- 4) (15 pts) Show the parsing stack and the action of an SLR(1) parser for the input  $((()))$ .

**Solution:** (You may use R for “Reduce” and S for “Shift”.)

	Parsing Stack	Input	Action
1	\$	\$	
2	\$	\$	
3	\$	\$	
4	\$	\$	
5	\$	\$	
6	\$	\$	
7	\$	\$	
8	\$	\$	
9	\$	\$	
10	\$	\$	
11	\$	\$	
12	\$	\$	
13	\$	\$	
14	\$	\$	
15	\$	\$	
16	\$	\$	
17	\$	\$	
18	\$	\$	
19	\$	\$	
20	\$	\$	
21	\$	\$	

**The End**