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Electromagnetic Characterisation of a Short-Stroke Ferromagnetic Actuator

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Smart-	Dense	Mesh
meshing	Air gap	Elements
OFF	OFF	14790
OFF	ON	16334
ON	OFF	22668
ON	ON	24368

Abstract—This experiment demonstrated the use of FEMM as an analysis tool for a short stroke ferromagnetic actuator.

I. Introduction

Finite Element Method Magnetics (FEMM) is a subset of Finite Element Analysis (FEA) that specialises in electromagnetics. This tool, in combination with MatLab, can be used to program a series of analytical situations, from which the mechanical aspects of the system can be characterised. The actuator and core of the system share the same ferromagnetic properties, windings cover the top and bottom of the core and three air gaps of note exist.

II. MODEL MESHING

To perform FEA, a model is split into elements. The elements must be small enough to output an accurate enough answer despite the linearisation of the physics occuring. Conversely, the elements cannot be too small as otherwise the computational time increases to an unfeasible (or uneconomical) amount.

FEMM has a smart-meshing tool in which the software analyses the model and allocates a dense mesh where the analysis must be of higher resolution and a sparse mesh where it does not. This is evident in figures 1 & 2. Although useful, this feature increases the mesh elements (see table I) and it does not know any information about the overarching complexity of the problem. One example of this is the boundaries involved with moving armature. Smart-meshing fails to recognise these edges as paramount to the analysis and produces a grid seen in figure 3. By manually increasing the density of meshing along these lines, FEMM can produce a more functional mesh seen in figure 4. This accuracy has its cost in terms of mesh elements and thus computational time, as seen in table I.

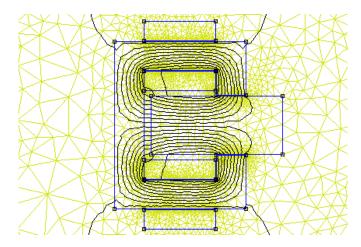


Fig. 1. Example mesh with smart-meshing disabled. Note the sparseness of the triangulation.

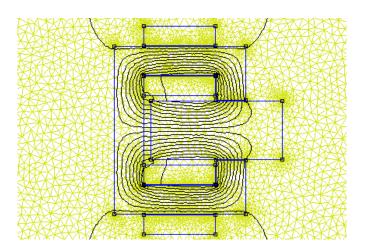


Fig. 2. Example mesh with smart meshing enabled. Note how the density increases around boundaries of interest.

III. WINDING RESISTANCE

IV. WINDING INDUCTANCE

V. FORCE ON THE ARMATURE

VI. CONCLUSION

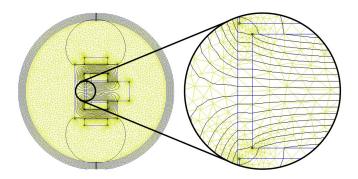


Fig. 3. FEMM smart-meshing output without specifying the area of interest. The density is low despite smart-meshing being on.

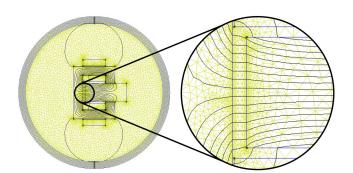


Fig. 4. FEMM smart-meshing output with specifying the area of interest and increasing the density of mesh elements within.

The following is a listing of the Matlab script written to achieve this analysis.

% CI ACTUATOR FEMM ANALYSIS PROGRAM

```
% show matlab where femm files are and setup
addpath(genpath('C:\femm42'));
openfemm()
opendocument('femm template.fem');
mi saveas ('actuator.fem');
% load in position and group no. for all components.
load('coil1p.mat');
load('coil2p.mat');
load('coil3p.mat');
load('coil4p.mat');
load('corep.mat');
load('moverp.mat');
% set create component array
components = {corep moverp coil1p coil2p coil3p coil4p};
mi_probdef(0, 'millimeters', 'planar', 1e-008, 20, 30, 0)
% add all nodes from data
mi\_addnode\,(\,components\,\{\,1\,\}\,(:\,,1)\,\,,\  \, components\,\{\,1\,\}\,(:\,,2))
mi_addnode(components\{2\}(:,1), components\{2\}(:,2))
mi_addnode(components \{3\}(:,1), components \{3\}(:,2))
mi_addnode(components \{4\}(:,1), components \{4\}(:,2))
mi_addnode(components \{5\}(:,1), components \{5\}(:,2))
mi_addnode(components \{6\}(:,1), components \{6\}(:,2))
% set node groups and draw lines for all components
for i = 1:length (components)
    modifyNodes(components{i});
    addLines (components { i });
end
% create array with coordinates of centre's of component blocks
blockCoords = [(\min(\text{components}\{1\}(:,1)) + 3) \pmod{(\text{components}\{1\}(:,2))};
                  mean(components \{2\}(:,1)) mean(components \{2\}(:,2));
                  mean(components \{3\}(:,1)) mean(components \{3\}(:,2));
                  mean(components \{4\}(:,1)) mean(components \{4\}(:,2));
                  mean(components \{5\}(:,1)) mean(components \{5\}(:,2));
                  mean(components \{6\}(:,1)) mean(components \{6\}(:,2));
                  -25 \ 0];
% create array of block properties
blockProps = {'core_linear' 1 0 '<None>' 0 1 0;
                core_linear' 1 0 '<None>' 0 2 0;
                'copper' 1 0 'winding_1' 0 3 100;
'copper' 1 0 'winding_1' 0 4 -100;
                'copper' 1 0 'winding_2' 0 5 100;
                'copper' 1 0 'winding_2' 0 6 -100;
                'air' 1 0 '<None>' 0 7 0};
```

```
% for all the different blocks, add labels and set its properties
for i = 1:max(size(blockCoords))
    mi\_addblocklabel(blockCoords(i\ ,1)\ ,\ blockCoords(i\ ,2));
    mi_selectlabel(blockCoords(i,1), blockCoords(i,2));
    mi_setblockprop(blockProps\{i,1\}, blockProps\{i,2\}, ...
                     blockProps\{i,3\}, blockProps\{i,4\}, ...
                     blockProps{i,5}, blockProps{i,6}, ...
                     blockProps { i, 7 });
    mi clearselected
end
% create system boundary, switch on smart-meshing & set winding currents
mi makeABC();
smartmesh(1);
mi_setcurrent('winding_1', 0);
mi setcurrent ('winding 2', 0);
% set number of steps for the armature to move and initialise 3D psi array
numOfSteps = 10;
psi = zeros (numOfSteps, 4, 10);
% for all the different currents, get inductances and hence psi values
for i = 10:1:30
    mi_setcurrent('winding_1', i);
    mi_setcurrent('winding_2', i);
    inductances = getInductances(blockProps, blockCoords, numOfSteps);
    psi(:,:,i) = inductances(:,2:5) * i;
end
\% figure ('Name', 'Psi - I')
% hold on
%
% plot(2:2:10, psi(1,4,:), 'x')
                            (x')
% plot(2:2:10, psi(2,4,:),
% plot(2:2:10, psi(3,4,:), 'x')
% plot(2:2:10, psi(4,4,:), 'x')
% plot(2:2:10, psi(5,4,:), 'x')
% hold off
figure ('Name', 'Inductance _-_ displacement')
hold on
plot(inductances(:,1), inductances(:,2), 'x');
plot(inductances(:,1), inductances(:,3), 'x');
plot(inductances(:,1), inductances(:,4), 'x');
plot(inductances(:,1), inductances(:,5), 'x');
hold off
mi_saveas('actuator.fem');
function inductances = getInductances (blockProps, blockCoords, numOfSteps)
    % reset armature to zero, define max & min positions & step size
    armaturePos = 0.0;
```

```
maxPos = -4.9;
minPos = 0.0;
stepSize = (maxPos-minPos)/(numOfSteps-1);
% initialise arrays for each type of analysis (linear/non-linear)
linearInductances = zeros (numOfSteps, 4);
nonlinearInductance = zeros (numOfSteps, 1);
% set the core and mover properties to linear
for i = 1:2
    mi_selectlabel(blockCoords(i,1), blockCoords(i,2));
    blockProps{i,5}, blockProps{i,6}, ...
                    blockProps { i, 7 });
    mi clearselected
end
% for all the linear states, analyse and get inductances
for i = 1:numOfSteps
    mi_purgemesh();
    mi_createmesh();
    linearInductances(i,:) = getLinearInductances(armaturePos);
    % catch to stop the mover being displaced into the core on last
    % iteration
    if i < numOfSteps</pre>
        moveArmature(stepSize);
        armaturePos = armaturePos + stepSize;
    end
end
% reset armature to zero displacement
moveArmature(-armaturePos);
armaturePos = 0.0;
% set core and mover properties to non-linear
for i = 1:2
    mi_selectlabel(blockCoords(i,1), blockCoords(i,2));
    mi_setblockprop('core_nonlinear', blockProps{i,2}, ...
                    blockProps{i,3}, blockProps{i,4}, \dots
                    blockProps{i,5}, blockProps{i,6}, ...
                    blockProps {i, 7});
    mi_clearselected
end
\% for all the non-linear states, analyse and get inductances
for i = 1:numOfSteps
    mi_purgemesh();
    mi_createmesh();
    nonlinearInductance(i) = nonlinearInductances();
    if i < numOfSteps
        moveArmature(stepSize);
        armaturePos = armaturePos + stepSize;
    end
end
```

```
% reset armature to zero displacement
    moveArmature(-armaturePos);
    armaturePos = 0.0;
    % collate all data outcomes
    inductances = [linearInductances(:,1) linearInductances(:,2) ...
                   linearInductances (:, 3) linearInductances (:, 4) ...
                   nonlinearInductance (:,1)];
end
function linearInductances = getLinearInductances(armaturePos)
    g = 5 + armaturePos;
    Rcore = (134.5e-3)/(4e-7 * pi * 1000 * 400e-6);
    Rair = (0.5e-3)/(4e-7 * pi * 400e-6);
    Rarmature = ((70 - g)*10^{-3})/(4e-7 * pi * 1000 * 400e-6);
    Rairvariable = (g*10^--3)/(4e-7*pi*400e-6);
    Rtot = Rcore + Rair + Rarmature + Rairvariable;
    Rairfringe = (0.5e-3)/(4e-7 * pi * (20e-3 + g*10^-3)^2);
    Rairvariablefringe = (g*10^{-}-3)/(4e-7*pi*(20e-3+g*10^{-}-3)^{2});
    Rtotfringe = Rcore + Rairfringe + Rarmature + Rairvariablefringe;
    Lanalytical = (100^2)/Rtot;
    Lanalyticalfringe = (100^2)/Rtotfringe;
    mi_saveas('linear.fem');
    mi_analyze();
    mi_loadsolution();
    CP = mo_getcircuitproperties('winding_1');
    Lnumericallinear = CP(3)/CP(1);
    linearInductances = [armaturePos Lanalytical ...
                          Lanalyticalfringe Lnumericallinear];
end
function Lnumericalnonlinear = nonlinearInductances()
    mi_saveas('nonlinear.fem');
    mi_analyze();
    mi_loadsolution();
    CP = mo_getcircuitproperties('winding_1');
    Lnumericalnonlinear = CP(3)/CP(1);
end
function moveArmature(dx)
    mi_selectgroup(2)
    mi_movetranslate(dx,0)
    mi clearselected()
end
function modifyNodes (component)
    for j = 1: size (component, 1)
        mi_selectnode(component(j,1), component(j,2));
        mi_setnodeprop(component, component(j,3));
        mi_clearselected
    end
end
```

```
function addLines (component)
    for j = 1: size (component, 1)
        if j < size (component, 1)
            mi_addsegment(component(j,1), component(j,2), ...
                           component (j+1,1), component (j+1,2);
            if j == 10 \&\& component(j,3) == 1
                mi_selectsegment(midpoint([component(j,1) component(j,2)...
                                    component (j+1,1) component (j+1,2));
                mi_setsegmentprop('<None>', 0.5, 0, component(j,3));
            end
            mi_selectsegment(midpoint([component(j,1) component(j,2) ...
                                       component(j+1,1) component(j+1,2)]);
            mi_setsegmentprop('<None>', 0, 1, 0, component(j,3));
            mi clearselected
        else
            mi_addsegment(component(j,1), component(j,2), ...
                           component (1,1), component (1,2);
            if component (j,3) == 2
                mi_selectsegment(midpoint([component(j,1) component(j,2)...
                                           component(1,1) component(1,2)]));
                mi_setsegmentprop('<None>', 0.5, 0, 0, component(j,3));
            end
            mi_selectsegment(midpoint([component(j,1) component(j,2) ...
                                       component (1,1) component (1,2));
            mi_setsegmentprop('<None>', 0, 1, 0, component(j,3));
            mi_clearselected
        end
    end
end
function mid = midpoint(coords)
    mid = [(coords(1) + coords(3))/2 (coords(2) + coords(4))/2];
end
```