Electromagnetic Characterisation of a Short-Stroke Ferromagnetic Actuator

R. M. Inston and H. Karimjee

Abstract—This experiment demonstrated the use of FEMM as an analysis tool for a short stroke ferromagnetic actuator.	
I. Introduction	
II. Winding Resistance	
III. Winding Inductance	
IV. FORCE ON THE ARMATURE	

V. CONCLUSION

The following is a listing of the Matlab script written to achieve this analysis.

% CI ACTUATOR FEMM ANALYSIS PROGRAM

```
% show matlab where femm files are and setup
addpath(genpath('C:\femm42'));
openfemm()
opendocument('femm template.fem');
mi saveas ('actuator.fem');
% load in position and group no. for all components.
load('coil1p.mat');
load('coil2p.mat');
load('coil3p.mat');
load('coil4p.mat');
load('corep.mat');
load('moverp.mat');
% set create component array
components = {corep moverp coil1p coil2p coil3p coil4p};
mi_probdef(0, 'millimeters', 'planar', 1e-008, 20, 30, 0)
% add all nodes from data
mi\_addnode\,(\,components\,\{\,1\,\}\,(:\,,1)\,\,,\  \, components\,\{\,1\,\}\,(:\,,2))
mi_addnode(components\{2\}(:,1), components\{2\}(:,2))
mi_addnode(components \{3\}(:,1), components \{3\}(:,2))
mi_addnode(components \{4\}(:,1), components \{4\}(:,2))
mi_addnode(components \{5\}(:,1), components \{5\}(:,2))
mi_addnode(components \{6\}(:,1), components \{6\}(:,2))
% set node groups and draw lines for all components
for i = 1:length (components)
    modifyNodes(components{i});
    addLines (components { i });
end
% create array with coordinates of centre's of component blocks
blockCoords = [(\min(\text{components}\{1\}(:,1)) + 3) \pmod{(\text{components}\{1\}(:,2))};
                  mean(components \{2\}(:,1)) mean(components \{2\}(:,2));
                  mean(components \{3\}(:,1)) mean(components \{3\}(:,2));
                  mean(components \{4\}(:,1)) mean(components \{4\}(:,2));
                  mean(components \{5\}(:,1)) mean(components \{5\}(:,2));
                  mean(components \{6\}(:,1)) mean(components \{6\}(:,2));
                  -25 \ 0];
% create array of block properties
blockProps = {'core_linear' 1 0 '<None>' 0 1 0;
                core_linear' 1 0 '<None>' 0 2 0;
                'copper' 1 0 'winding_1' 0 3 100;
'copper' 1 0 'winding_1' 0 4 -100;
                'copper' 1 0 'winding_2' 0 5 100;
                'copper' 1 0 'winding_2' 0 6 -100;
                'air' 1 0 '<None>' 0 7 0};
```

```
% for all the different blocks, add labels and set its properties
for i = 1:max(size(blockCoords))
    mi\_addblocklabel(blockCoords(i\ ,1)\ ,\ blockCoords(i\ ,2));
    mi_selectlabel(blockCoords(i,1), blockCoords(i,2));
    mi_setblockprop(blockProps\{i,1\}, blockProps\{i,2\}, ...
                     blockProps\{i,3\}, blockProps\{i,4\}, ...
                     blockProps{i,5}, blockProps{i,6}, ...
                     blockProps { i, 7 });
    mi clearselected
end
% create system boundary, switch on smart-meshing & set winding currents
mi makeABC();
smartmesh(1);
mi_setcurrent('winding_1', 0);
mi setcurrent ('winding 2', 0);
% set number of steps for the armature to move and initialise 3D psi array
numOfSteps = 10;
psi = zeros (numOfSteps, 4, 10);
% for all the different currents, get inductances and hence psi values
for i = 10:1:30
    mi_setcurrent('winding_1', i);
    mi_setcurrent('winding_2', i);
    inductances = getInductances(blockProps, blockCoords, numOfSteps);
    psi(:,:,i) = inductances(:,2:5) * i;
end
\% figure ('Name', 'Psi - I')
% hold on
%
% plot(2:2:10, psi(1,4,:), 'x')
                            (x')
% plot(2:2:10, psi(2,4,:),
% plot(2:2:10, psi(3,4,:), 'x')
% plot(2:2:10, psi(4,4,:), 'x')
% plot(2:2:10, psi(5,4,:), 'x')
% hold off
figure ('Name', 'Inductance _-_ displacement')
hold on
plot(inductances(:,1), inductances(:,2), 'x');
plot(inductances(:,1), inductances(:,3), 'x');
plot(inductances(:,1), inductances(:,4), 'x');
plot(inductances(:,1), inductances(:,5), 'x');
hold off
mi_saveas('actuator.fem');
function inductances = getInductances (blockProps, blockCoords, numOfSteps)
    % reset armature to zero, define max & min positions & step size
    armaturePos = 0.0;
```

```
maxPos = -4.9;
minPos = 0.0;
stepSize = (maxPos-minPos)/(numOfSteps-1);
% initialise arrays for each type of analysis (linear/non-linear)
linearInductances = zeros(numOfSteps, 4);
nonlinearInductance = zeros (numOfSteps, 1);
% set the core and mover properties to linear
for i = 1:2
    mi_selectlabel(blockCoords(i,1), blockCoords(i,2));
    blockProps{i,5}, blockProps{i,6}, ...
                    blockProps { i, 7 });
    mi clearselected
end
% for all the linear states, analyse and get inductances
for i = 1:numOfSteps
    mi_purgemesh();
    mi_createmesh();
    linearInductances(i,:) = getLinearInductances(armaturePos);
    % catch to stop the mover being displaced into the core on last
    % iteration
    if i < numOfSteps</pre>
        moveArmature(stepSize);
        armaturePos = armaturePos + stepSize;
    end
end
% reset armature to zero displacement
moveArmature(-armaturePos);
armaturePos = 0.0;
% set core and mover properties to non-linear
for i = 1:2
    mi_selectlabel(blockCoords(i,1), blockCoords(i,2));
    mi_setblockprop('core_nonlinear', blockProps{i,2}, ...
                    blockProps{i,3}, blockProps{i,4}, \dots
                    blockProps{i,5}, blockProps{i,6}, ...
                    blockProps {i, 7});
    mi_clearselected
end
\% for all the non-linear states, analyse and get inductances
for i = 1:numOfSteps
    mi_purgemesh();
    mi_createmesh();
    nonlinearInductance(i) = nonlinearInductances();
    if i < numOfSteps
        moveArmature(stepSize);
        armaturePos = armaturePos + stepSize;
    end
end
```

```
% reset armature to zero displacement
    moveArmature(-armaturePos);
    armaturePos = 0.0;
    % collate all data outcomes
    inductances = [linearInductances(:,1) linearInductances(:,2) ...
                   linearInductances (:, 3) linearInductances (:, 4) ...
                   nonlinearInductance (:,1)];
end
function linearInductances = getLinearInductances(armaturePos)
    g = 5 + armaturePos;
    Rcore = (134.5e-3)/(4e-7 * pi * 1000 * 400e-6);
    Rair = (0.5e-3)/(4e-7 * pi * 400e-6);
    Rarmature = ((70 - g)*10^{-3})/(4e-7 * pi * 1000 * 400e-6);
    Rairvariable = (g*10^--3)/(4e-7*pi*400e-6);
    Rtot = Rcore + Rair + Rarmature + Rairvariable;
    Rairfringe = (0.5e-3)/(4e-7 * pi * (20e-3 + g*10^-3)^2);
    Rairvariablefringe = (g*10^{-}-3)/(4e-7*pi*(20e-3+g*10^{-}-3)^{2});
    Rtotfringe = Rcore + Rairfringe + Rarmature + Rairvariablefringe;
    Lanalytical = (100^2)/Rtot;
    Lanalyticalfringe = (100^2)/Rtotfringe;
    mi_saveas('linear.fem');
    mi_analyze();
    mi_loadsolution();
    CP = mo_getcircuitproperties('winding_1');
    Lnumericallinear = CP(3)/CP(1);
    linearInductances = [armaturePos Lanalytical ...
                          Lanalyticalfringe Lnumericallinear];
end
function Lnumericalnonlinear = nonlinearInductances()
    mi_saveas('nonlinear.fem');
    mi_analyze();
    mi_loadsolution();
    CP = mo_getcircuitproperties('winding_1');
    Lnumericalnonlinear = CP(3)/CP(1);
end
function moveArmature(dx)
    mi_selectgroup(2)
    mi_movetranslate(dx, 0)
    mi clearselected()
end
function modifyNodes (component)
    for j = 1: size (component, 1)
        mi_selectnode(component(j,1), component(j,2));
        mi_setnodeprop(component, component(j,3));
        mi_clearselected
    end
end
```

```
function addLines (component)
    for j = 1: size (component, 1)
        if j < size (component, 1)
            mi_addsegment(component(j,1), component(j,2), ...
                           component (j+1,1), component (j+1,2);
            if j == 10 \&\& component(j,3) == 1
                mi_selectsegment(midpoint([component(j,1) component(j,2)...
                                    component (j+1,1) component (j+1,2));
                mi_setsegmentprop('<None>', 0.5, 0, component(j,3));
            end
            mi_selectsegment(midpoint([component(j,1) component(j,2) ...
                                       component(j+1,1) component(j+1,2)]);
            mi_setsegmentprop('<None>', 0, 1, 0, component(j,3));
            mi clearselected
        else
            mi_addsegment(component(j,1), component(j,2), ...
                           component (1,1), component (1,2);
            if component (j,3) == 2
                mi_selectsegment(midpoint([component(j,1) component(j,2)...
                                           component(1,1) component(1,2)]));
                mi_setsegmentprop('<None>', 0.5, 0, 0, component(j,3));
            end
            mi_selectsegment(midpoint([component(j,1) component(j,2) ...
                                       component (1,1) component (1,2));
            mi_setsegmentprop('<None>', 0, 1, 0, component(j,3));
            mi_clearselected
        end
    end
end
function mid = midpoint(coords)
    mid = [(coords(1) + coords(3))/2 (coords(2) + coords(4))/2];
end
```