

# Electromagnetic Characterisation of a Short-Stroke Ferromagnetic Actuator

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***Abstract***—This experiment demonstrated the use of FEMM as an analysis tool for a short stroke ferromagnetic actuator.

## I. INTRODUCTION

Finite Element Method Magnetics (FEMM) is a subset of Finite Element Analysis (FEA) that specialises in electromagnetics. This tool, in combination with MatLab, can be used to program a series of analytical situations, from which the mechanical aspects of the system can be characterised. The actuator and core of the system share the same ferromagnetic properties, windings cover the top and bottom of the core and three air gaps of note exist.

## II. WINDING RESISTANCE

## III. WINDING INDUCTANCE

## IV. FORCE ON THE ARMATURE

## V. CONCLUSION

## VI. APPENDIX

The following is a listing of the Matlab script written to achieve this analysis.

```
% CI ACTUATOR FEMM ANALYSIS PROGRAM

% show matlab where femm files are and setup
addpath(genpath('C:\femm42'));
openfemm()
opendocument('femm_template.fem');
mi_saveas('actuator.fem');

% load in position and group no. for all components.
load('coil1p.mat');
load('coil2p.mat');
load('coil3p.mat');
load('coil4p.mat');
load('corep.mat');
load('moverp.mat');

% set create component array
components = {corep moverp coil1p coil2p coil3p coil4p};

mi_probdef(0, 'millimeters', 'planar', 1e-008, 20, 30, 0)

% add all nodes from data
mi_addnode(components{1}(:,1), components{1}(:,2))
mi_addnode(components{2}(:,1), components{2}(:,2))
mi_addnode(components{3}(:,1), components{3}(:,2))
mi_addnode(components{4}(:,1), components{4}(:,2))
mi_addnode(components{5}(:,1), components{5}(:,2))
mi_addnode(components{6}(:,1), components{6}(:,2))

% set node groups and draw lines for all components
for i = 1:length(components)
    modifyNodes(components{i});
    addLines(components{i});
end

% create array with coordinates of centre's of component blocks
blockCoords = [(min(components{1}(:,1)) + 3) mean(components{1}(:,2));
    mean(components{2}(:,1)) mean(components{2}(:,2));
    mean(components{3}(:,1)) mean(components{3}(:,2));
    mean(components{4}(:,1)) mean(components{4}(:,2));
    mean(components{5}(:,1)) mean(components{5}(:,2));
    mean(components{6}(:,1)) mean(components{6}(:,2));
    -25 0];

% create array of block properties
blockProps = {'core_linear' 1 0 '<None>' 0 1 0;
    'core_linear' 1 0 '<None>' 0 2 0;
    'copper' 1 0 'winding_1' 0 3 100;
    'copper' 1 0 'winding_1' 0 4 -100;
    'copper' 1 0 'winding_2' 0 5 100;
    'copper' 1 0 'winding_2' 0 6 -100;
    'air' 1 0 '<None>' 0 7 0};
```

```

% for all the different blocks, add labels and set its properties
for i = 1:max(size(blockCoords))
    mi_addblocklabel(blockCoords(i,1), blockCoords(i,2));
    mi_selectlabel(blockCoords(i,1), blockCoords(i,2));
    mi_setblockprop(blockProps{i,1}, blockProps{i,2}, ...
                    blockProps{i,3}, blockProps{i,4}, ...
                    blockProps{i,5}, blockProps{i,6}, ...
                    blockProps{i,7});
    mi_clearselected
end

% create system boundary, switch on smart-meshing & set winding currents
mi_makeABC();
smartmesh(1);
mi_setcurrent('winding_1', 0);
mi_setcurrent('winding_2', 0);

% set number of steps for the armature to move and initialise 3D psi array
numOfSteps = 10;
psi = zeros(numOfSteps,4,10);

% for all the different currents, get inductances and hence psi values
for i = 10:1:30
    mi_setcurrent('winding_1', i);
    mi_setcurrent('winding_2', i);
    inductances = getInductances(blockProps, blockCoords, numOfSteps);
    psi(:, :, i) = inductances(:,2:5) * i;
end

% figure('Name', 'Psi - I')
% hold on
%
% plot(2:2:10, psi(1,4,:), 'x')
% plot(2:2:10, psi(2,4,:), 'x')
% plot(2:2:10, psi(3,4,:), 'x')
% plot(2:2:10, psi(4,4,:), 'x')
% plot(2:2:10, psi(5,4,:), 'x')
% hold off

figure('Name', 'Inductance vs displacement')
hold on
plot(inductances(:,1), inductances(:,2), 'x');
plot(inductances(:,1), inductances(:,3), 'x');
plot(inductances(:,1), inductances(:,4), 'x');
plot(inductances(:,1), inductances(:,5), 'x');
hold off

mi_saveas('actuator.fem');

function inductances = getInductances(blockProps, blockCoords, numOfSteps)
    % reset armature to zero, define max & min positions & step size
    armaturePos = 0.0;

```

```

maxPos = -4.9;
minPos = 0.0;
stepSize = (maxPos-minPos)/(numOfSteps-1);

% initialise arrays for each type of analysis (linear/non-linear)
linearInductances = zeros(numOfSteps, 4);
nonlinearInductance = zeros(numOfSteps,1);

% set the core and mover properties to linear
for i = 1:2
    mi_selectlabel(blockCoords(i,1), blockCoords(i,2));
    mi_setblockprop('core_linear', blockProps{i,2}, ...
        blockProps{i,3}, blockProps{i,4}, ...
        blockProps{i,5}, blockProps{i,6}, ...
        blockProps{i,7});
    mi_clearselected
end

% for all the linear states, analyse and get inductances
for i = 1:numOfSteps
    mi_purgemesh();
    mi_createmesh();
    linearInductances(i,:) = getLinearInductances(armaturePos);
    % catch to stop the mover being displaced into the core on last
    % iteration
    if i < numOfSteps
        moveArmature(stepSize);
        armaturePos = armaturePos + stepSize;
    end
end

% reset armature to zero displacement
moveArmature(-armaturePos);
armaturePos = 0.0;

% set core and mover properties to non-linear
for i = 1:2
    mi_selectlabel(blockCoords(i,1), blockCoords(i,2));
    mi_setblockprop('core_nonlinear', blockProps{i,2}, ...
        blockProps{i,3}, blockProps{i,4}, ...
        blockProps{i,5}, blockProps{i,6}, ...
        blockProps{i,7});
    mi_clearselected
end

% for all the non-linear states, analyse and get inductances
for i = 1:numOfSteps
    mi_purgemesh();
    mi_createmesh();
    nonlinearInductance(i) = nonlinearInductances();
    if i < numOfSteps
        moveArmature(stepSize);
        armaturePos = armaturePos + stepSize;
    end
end

```

```

% reset armature to zero displacement
moveArmature(-armaturePos);
armaturePos = 0.0;

% collate all data outcomes
inductances = [linearInductances(:,1) linearInductances(:,2) ...
               linearInductances(:,3) linearInductances(:,4) ...
               nonlinearInductance(:,1)];

end

function linearInductances = getLinearInductances(armaturePos)
    g = 5 + armaturePos;
    Rcore = (134.5e-3)/(4e-7 * pi * 1000 * 400e-6);
    Rair = (0.5e-3)/(4e-7 * pi * 400e-6);
    Rarmature = ((70 - g)*10^-3)/(4e-7 * pi * 1000 * 400e-6);
    Rairvariable = (g*10^-3)/(4e-7 * pi * 400e-6);
    Rtot = Rcore + Rair + Rarmature + Rairvariable;
    Rairfringe = (0.5e-3)/(4e-7 * pi * (20e-3 + g*10^-3)^2);
    Rairvariablefringe = (g*10^-3)/(4e-7 * pi * (20e-3 + g*10^-3)^2);
    Rtotfringe = Rcore + Rairfringe + Rarmature + Rairvariablefringe;
    Lanalytical = (100^2)/Rtot;
    Lanalyticalfringe = (100^2)/Rtotfringe;
    mi_saveas('linear.fem');
    mi_analyze();
    mi_loadsolution();
    CP = mo_getcircuitproperties('winding_1');
    Lnumericallinear = CP(3)/CP(1);
    linearInductances = [armaturePos Lanalytical ...
                        Lanalyticalfringe Lnumericallinear];

end

function Lnumericalnonlinear = nonlinearInductances()

    mi_saveas('nonlinear.fem');
    mi_analyze();
    mi_loadsolution();
    CP = mo_getcircuitproperties('winding_1');
    Lnumericalnonlinear = CP(3)/CP(1);

end

function moveArmature(dx)
    mi_selectgroup(2)
    mi_movetranslate(dx,0)
    mi_clearselected()
end

function modifyNodes(component)
    for j = 1:size(component,1)
        mi_selectnode(component(j,1), component(j,2));
        mi_setnodeprop(component, component(j,3));
        mi_clearselected
    end
end
end

```

```

function addLines(component)
    for j = 1: size(component,1)
        if j < size(component,1)
            mi_addsegment(component(j,1), component(j,2), ...
                           component(j+1,1), component(j+1,2));
            if j == 10 && component(j,3) == 1
                mi_selectsegment(midpoint([component(j,1) component(j,2)...
                                             component(j+1,1) component(j+1,2)]));
                mi_setsegmentprop('<None>', 0.5, 0, 0, component(j,3));
            end
            mi_selectsegment(midpoint([component(j,1) component(j,2) ...
                                       component(j+1,1) component(j+1,2)]));
            mi_setsegmentprop('<None>', 0, 1, 0, component(j,3));
            mi_clearselected
        else
            mi_addsegment(component(j,1), component(j,2), ...
                           component(1,1), component(1,2));
            if component(j,3) == 2
                mi_selectsegment(midpoint([component(j,1) component(j,2)...
                                             component(1,1) component(1,2)]));
                mi_setsegmentprop('<None>', 0.5, 0, 0, component(j,3));
            end
            mi_selectsegment(midpoint([component(j,1) component(j,2) ...
                                       component(1,1) component(1,2)]));
            mi_setsegmentprop('<None>', 0, 1, 0, component(j,3));
            mi_clearselected
        end
    end
end

function mid = midpoint(coords)
    mid = [(coords(1) + coords(3))/2 (coords(2) + coords(4))/2];
end

```