

# Homework - 3 Submission by Haritha Pulletikurti

## Homework3Solutions.R

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### Question 5.1

Using crime data from the file `uscrime.txt` (<http://www.statsci.org/data/general/uscrime.txt>, description at <http://www.statsci.org/data/general/uscrime.html>), test to see whether there are any outliers in the last column (number of crimes per 100,000 people). Use the `grubbs.test` function in the `outliers` package in R.

Implementation:

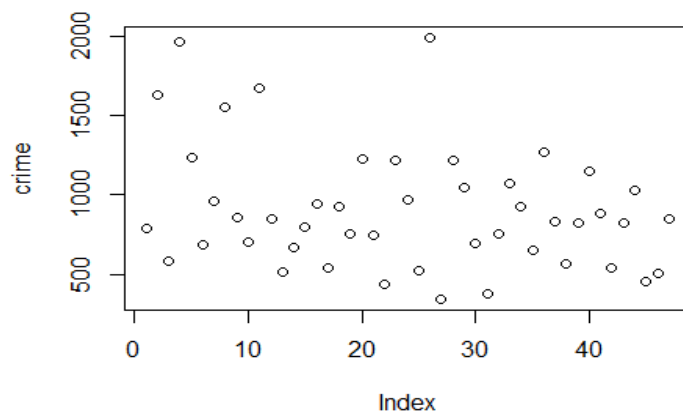
```
# Start with a clear environment
rm(list = ls())

#Load the libraries
library(knitr)
library(stringr)
library(outliers)
#Load the crime data with headers
crime_data <- read.table("uscrime.txt", stringsAsFactors = FALSE, header = TRUE)

set.seed(1)
dim(crime_data)

## [1] 47 16

crime <- crime_data[, "Crime"]
plot(crime)
```

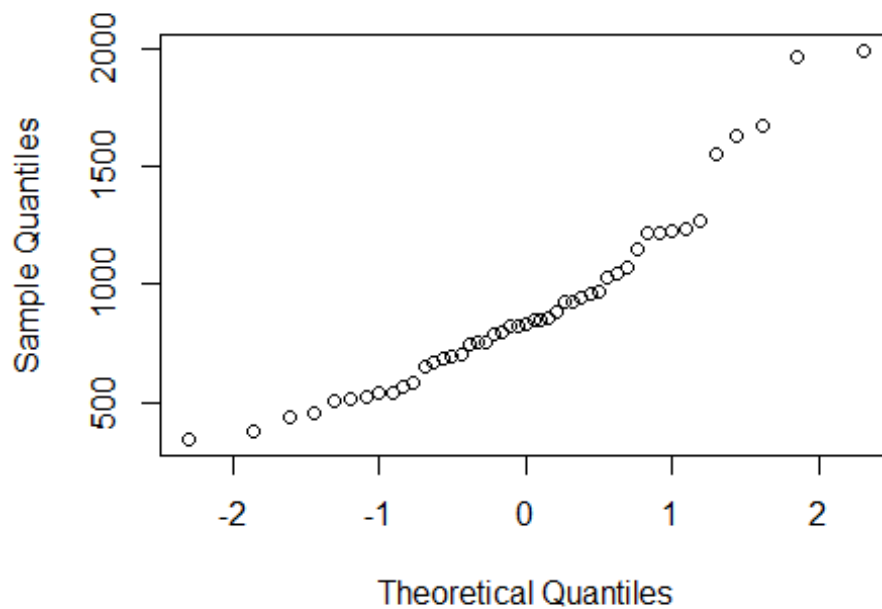


```
shapiro.test(crime)

##
##  Shapiro-Wilk normality test
##
## data:  crime
## W = 0.91273, p-value = 0.001882

qqnorm(crime)
```

### Normal Q-Q Plot



```

#The qq norm show that the data is 90% of the data is almost normal

#Using Grubbs Test find the minimum and maximum outliers using type = 11
#type = 11 gives 2 outliers one- min and one-max
# I am not using type = 20 as it accepts less data around 30 data values.
# As we have more data, type = 20 gives error. So choosing type = 11

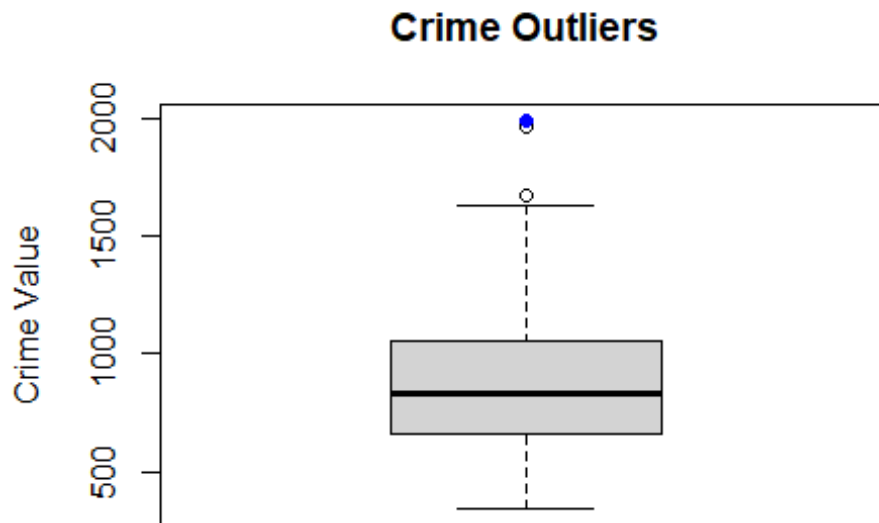
outlier_results<-grubbs.test(crime_data[,16],type=11)
outlier_results

##
## Grubbs test for two opposite outliers
##
## data:  crime_data[, 16]
## G = 4.26877, U = 0.78103, p-value = 1
## alternative hypothesis: 342 and 1993 are outliers

#Inference: 343 and 1993 are outliers. Let us plot them in boxplot and
visualize

values<- as.numeric(str_extract_all(outlier_results$alternative, "[0-
9]+")[[1]])
Outliers_data<- subset(crime_data, Crime %in% values)
boxplot(crime_data[,16],
        ylab="Crime Value")
points(Outliers_data[,ncol(Outliers_data)], pch=19,col='blue')
title(main="Crime Outliers")

```



**Inference:** Based on the box plot, the blue dot is 1993. Also looks like the 1969 is also an outlier.

Since grubbs test only gets the min and max outliers (only 2) 1969 is not listed in the test result but it is shown in the boxplot next to 1993. Also 342(min value) is returned as outlier in the grubbs.test. Boxplot did not show it. So, looks like the 342 is within the reasonable range according to boxplot.

#### Question 6.1

Describe a situation or problem from your job, everyday life, current events, etc. for which a Change Detection model would be appropriate. Applying the CUSUM technique, how would you choose the critical value and the threshold?

**Answer:**

The Cusum Approach can be used in Production Assembly lines where a lot of Robots are involved in assembling the parts of the units. A small change in the movement of the Robotic Holding Parts will make a huge impact on whether the assembly takes place successfully or the process crashes.

**Example:**

Consider a car manufacturing plant, where in each assembly line a different car part is being assembled by the robots.

Suppose the robot hand must drop an item onto the conveyor belt at an angle of 45 - 50 degrees and the item successfully land at the place

Say the angle is changed to 51 degrees instead of the allowed threshold of 50 degrees, the item fails to land successfully.

Using cusum approach on the everyday data collected of such processes, we can determine at what point the most failures happen and we will be able to correct the process to be more successful

## Question 6.2

1. Using July through October daily-high-temperature data for Atlanta for 1996 through 2015, use a CUSUM approach to identify when unofficial summer ends (i.e., when the weather starts cooling off) each year. You can get the data that you need from the file temps.txt or online, for example at <http://www.iweather.net.com/atlanta-weather-records> or <https://www.wunderground.com/history/airport/KFTY/2015/7/1/CustomHistory.html> You can use R if you'd like, but it's straightforward enough that an Excel spreadsheet can easily do the job too.

```
rm(list = ls())
data <- read.delim("temps.txt", header=T)

S= c()
DetectedDecreaseIndex = c()
DetectedDecrease = c()
S[0] = 0

# Let c= 5 and T = 20
# WE need to find when the temperature decreases so the summer ends.

#Detecting a decrease:  $S(t)=\text{MAX}\{0, S(t-1)+(\text{Mean}(X)-X(t)-C)\}$ 

t=20
C=5
for(j in 2:ncol(data))
{
  for(i in 1:nrow(data))
  {
    S[i] = max(0,S[i-1]+(mean(data[,j])-data[i,j] - C))
    if(S[i]>t)
```

```

    {
        DetectedDecreaseIndex[j-1] = i
        DetectedDecrease[j-1]=S[i]
        break
    }
}
}

```

#### #Preparing Data for the cusum table

```

cusum_year = colnames(data[-1])
cusum_decrease_date = c()
cusum_c = c()
cusum_t =c()
cusum_st = c()
for(k in 1:length(DetectedDecreaseIndex))
{
    cusum_decrease_date[k] = data[DetectedDecreaseIndex[k],1]
    cusum_st[k]=DetectedDecrease[k]
    cusum_c[k] = C
    cusum_t[k] = t
}

```

#### #put all the values into a matrix so we can display as a table

```

matrix.c = cbind(cusum_year,cusum_decrease_date,cusum_st,cusum_c,cusum_t)
colnames(matrix.c) = c("Year","End of Summer", "S(t)", "C","Threshold")
matrix.c = as.table(matrix.c)
matrix.c

```

##	Year	End of Summer	S(t)	C	Threshold
## A	X1996	30-Sep	25.1463414634146	5	20
## B	X1997	27-Sep	30.0243902439024	5	20
## C	X1998	9-Oct	21.0406504065041	5	20
## D	X1999	30-Sep	20.9349593495935	5	20
## E	X2000	7-Sep	26.0650406504065	5	20
## F	X2001	26-Sep	22.6585365853658	5	20
## G	X2002	27-Sep	22.3414634146341	5	20
## H	X2003	1-Oct	23.9186991869919	5	20
## I	X2004	12-Oct	22.349593495935	5	20
## J	X2005	9-Oct	26.4308943089431	5	20
## K	X2006	13-Oct	32.390243902439	5	20
## L	X2007	12-Oct	21.7967479674797	5	20
## M	X2008	19-Oct	31.5365853658537	5	20
## N	X2009	5-Oct	22.9430894308943	5	20
## O	X2010	30-Sep	23.0569105691057	5	20
## P	X2011	8-Sep	26.3821138211382	5	20
## Q	X2012	3-Oct	25.6016260162602	5	20
## R	X2013	17-Aug	24	5	20

```
## S X2014 29-Sep      23.6016260162601 5 20
## T X2015 26-Sep      23.8048780487805 5 20
```

### Inference :

From the Year "1996 -2002", Summer ended around mid to end of September  
 From the Year "2003-2009", Summer ended around Mid October  
 From Year "2010-2011 and 2014-2015" Summer ended at end of September  
 For Years 2013 Summer ended very soon in mid August. The Values ranged between 60's through 70's

### #Question(2)

# Use a CUSUM approach to make a judgment of whether Atlanta's summer climate has gotten warmer  
 #in that time (and if so, when).  
 # Start with a clear environment

```
rm(list = ls())
data <- read.delim("temps.txt", header=T)
```

```
St= c()
DetectedIncreaseIndex = c()
DetectedIncrease = c()
St[0] = 0
```

# Let  $c = 5$  and  $T = 20$   
 # WE need to find when the temperature rises

#Detecting a Increase:  $S(t) = \text{MAX}\{0, S(t-1) + (X(t) - \text{Mean}(X) - C)\}$

```
t=10
C=5
for(j in 2:ncol(data))
{
  for(i in 1:nrow(data))
  {
    St[i] = max(0, St[i-1] + (data[i,j] - mean(data[,j]) - C))
    if(St[i] > t)
    {
      DetectedIncreaseIndex[j-1] = i
      DetectedIncrease[j-1] = St[i]
      break
    }
  }
}
}
cusum_year = colnames(data[-1])
cusum_increase_date = c()
```

```

cusum_c = c()
cusum_t =c()
cusum_st_inc = c()
for(k in 1:length(DetectedIncreaseIndex))
{
  cusum_increase_date[k] = data[DetectedIncreaseIndex[k],1]
  cusum_st_inc[k]=DetectedIncrease[k]
  cusum_c[k] = C
  cusum_t[k] = t
}

matrix.HighSummer =
cbind(cusum_year,cusum_increase_date,cusum_st_inc,cusum_c,cusum_t)
colnames(matrix.HighSummer) = c("Year","Increased Summer", "Cusum S(t)",
"C","Threshold")
matrix.HighSummer = as.table(matrix.HighSummer)
matrix.HighSummer

```

##	Year	Increased Summer	Cusum S(t)	C	Threshold
## A	X1996	3-Jul	16.5691056910569	5	10
## B	X1997	4-Jul	13.9756097560976	5	10
## C	X1998	8-Jul	14.4390243902439	5	10
## D	X1999	23-Jul	10.5691056910569	5	10
## E	X2000	4-Jul	11.9024390243902	5	10
## F	X2001	11-Jul	11.6829268292683	5	10
## G	X2002	8-Jul	10.0731707317074	5	10
## H	X2003	21-Jul	10.1219512195122	5	10
## I	X2004	8-Jul	10.1788617886179	5	10
## J	X2005	23-Jul	10.4959349593496	5	10
## K	X2006	4-Jul	12.8536585365854	5	10
## L	X2007	4-Aug	14.609756097561	5	10
## M	X2008	12-Jul	11.8780487804878	5	10
## N	X2009	4-Jul	12.0243902439025	5	10
## O	X2010	9-Jul	10.3658536585366	5	10
## P	X2011	4-Jul	10.1707317073171	5	10
## Q	X2012	3-Jul	12.6991869918699	5	10
## R	X2013	10-Aug	11.3333333333333	5	10
## S	X2014	7-Aug	10.2276422764228	5	10
## T	X2015	10-Jul	10.7967479674797	5	10

#### Inference :

Using the CUSUM approach, I calculated the increase in Atlanta Temperatures. The most high summers are in July(90 and above) based on the above table.

I have selected the Threshold = 10 and C=5.

Note : When The Threshold is 20 or above, few year's St value is null.

So,Threshold = 10 is choosen as ideal.