

No:

Discrete Structure Assignment 12

Section : 2

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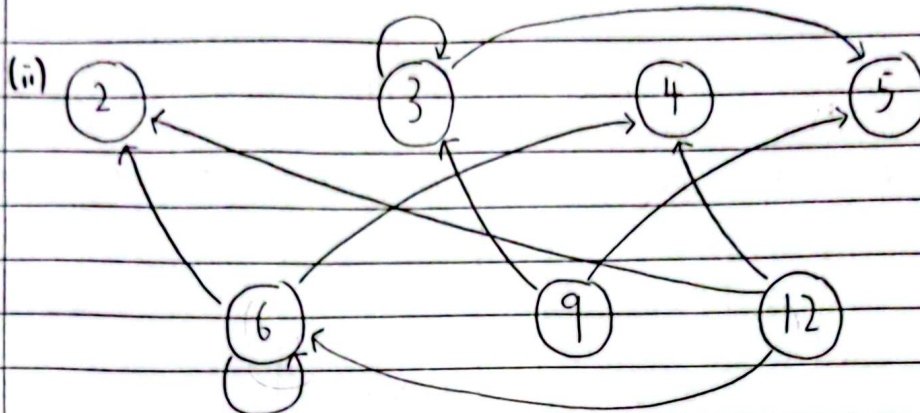
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1) (i) $aRb \leftrightarrow a-b \in \mathbb{Z}^{\text{even}}$

$$R = \{(6,2), (12,2), (3,3), (6,4), (4,2), (6,6), (9,3), (12,4), (4,5), (12,6)\}$$

$$R = \{(6,2), (12,2), (3,3), (9,3), (6,4), (12,4), (9,5), (6,6), (12,6)\} \cup \{(3,5)\}$$



(iii) The domain of R is $\{3, 6, 9, 12\}$.

The range of R is $\{2, 3, 4, 5, 6\}$.

2) $R = \{(1,8), (3,10), (8,15), (8,1), (10,3), (15,8), (1,15), (15,1)\}$

~~Since~~

Equivalent relation exist if a relation is reflexive, symmetric and transitive.

~~Since~~ xRy

such as no existent of $(1,1), (3,3), (8,8), (10,10)$ and $(15,15)$,

Since there is no any element related to itself, xRy is not reflexive.

Thus, this relation is not an equivalence relations.



3) (i)

$$M_R = \begin{matrix} & \begin{matrix} s & t & u & v \end{matrix} \\ \begin{matrix} s \\ t \\ u \\ v \end{matrix} & \begin{bmatrix} 1 & 1 & 1 & 0 \\ 0 & 1 & 1 & 1 \\ 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} \end{matrix}$$

(ii)		s	t	u	v
In-degree		2	2	3	1
Out-degree		3	3	2	0

(iii) If a relation is partial order, it is reflexive, antisymmetric and transitive.

Relation R is not reflexive, since there is no existent of (v, v) in R.

Relation R is not antisymmetric, since there are existent of (s, u) and (u, s) in R.

$$\begin{bmatrix} 1 & 1 & 1 & 0 \\ 0 & 1 & 1 & 1 \\ 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} \otimes \begin{bmatrix} 1 & 1 & 1 & 0 \\ 0 & 1 & 1 & 1 \\ 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

Since $M_R \otimes M_R \neq M_R$, relation R is not transitive.

In conclusion, relation R is not partial order.

4) If v and w is one-to-one, then when $v(x) = w(x)$, $x = x$.

~~$$v(x) = w(x)$$~~

~~$$4 - x^2 = 2x$$~~

~~$$0 = x^2 + 2x - 4$$~~

Since $x \neq x$, v and w not one-to-one relation.

$$4) \text{ When } x = -2, \quad v(x) = 4 - (-2)^2, \quad w(x) = 2(-2)$$

$$= 4 - 4 \quad = -4$$

$$= 0$$

$$\text{When } x = 0, \quad v(x) = 4 - (0)^2, \quad w(x) = 2(0)$$

$$= 4 - 0 \quad = 0$$

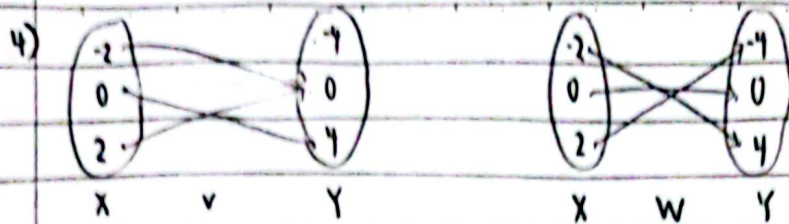
$$= 4$$

$$\text{When } x = 2, \quad v(x) = 4 - (2)^2, \quad w(x) = 2(2)$$

$$= 4 - 4 \quad = 4$$

$$= 0$$





Based on diagram, $v(x)$ is not one-to-one, not onto Y, thus not bijection (bijection exist when a relation is both one-to-one and onto Y.)

Based on diagram, $w(x)$ is one-to-one and onto Y. Thus, $w(x)$ is also bijection.

5) (i) $g(x) = \frac{2}{3}x$

Let $y = \frac{2}{3}x$

$x = \frac{3}{2}y$

$g^{-1}(x) = \frac{3}{2}x$

(ii) $(g \circ g \circ f)(x) = g(g(f(x)))$

$= g(g(7x-2))$

$= g(\frac{2}{3}(7x-2))$

$= \frac{2}{3}(\frac{2}{3}(7x-2))$

$= \frac{4}{9}(7x-2)$

$= \frac{28}{9}x - \frac{8}{9}$

6) (i) Chemical A and B combined become C.

F_0 of chemical A = 5.0 Fahrenheit.

F_1 of chemical B = 4.5 Fahrenheit.

For $t \geq 2$, $F_t = \frac{1}{3}(F_{t-1} + \frac{1}{2}F_{t-2})$

The recurrence relation of chemical (for $t \geq 2$) is $F_t = F_{t-1} + \frac{1}{3}F_{t-2}$, $F_0 = 5.0$, $F_1 = 4.5$.

(ii) $F_0 = 5.0$, $F_1 = 4.5$

$F_2 = F_1 + \frac{1}{3}F_0$

$= 4.5 + \frac{1}{3}(5.0)$

$= 4.5 + 1.0$

$= 5.5$



No.:

$$b) F_3 = F_2 + \frac{1}{3} F_1$$

$$= 5.5 + \frac{1}{3} (4.5)$$

$$= 5.5 + 1.5$$

$$= 6.4$$

$$F_4 = F_3 + \frac{1}{3} F_2$$

$$= 6.4 + \frac{1}{3} (5.5)$$

$$= 6.4 + 1.1$$

$$= 7.5$$

$$F_5 = F_4 + \frac{1}{3} F_3$$

$$= 7.5 + \frac{1}{3} (6.4)$$

$$= 7.5 + 1.28$$

$$= 8.78$$

7) ~~f(n)~~ w(n)

{ if (n=0)

return 5

else if (n=1)

return 7

else

return ~~w~~ 2w(n-1) + w(n-2)

}

~~w(4)~~ Trace output of n=4 in w(n)

w(4)

n=4

Since n ≠ 0 and 1,

return 2w(3) + w(2) ← Return 2(45) + 19

w(3)

n=3

Since n ≠ 0 and 1,

return 2w(2) + w(1) ← Return 2(19) + 7

w(2)

n=2

Since n ≠ 0 and 1,

return 2w(1) + w(0) ← Return 2(7) + 5

w(1)

n=1

Since n=1,

return 7

w(2)=19

w(1)=7

Return 7

Based on tracing, w(1)=7, w(2)=19, w(3)=45 and w(4)=109.

