

Lecture Notes

(Click on one of the following courses to expand.)

Modern Algorithmic Toolbox (with [Greg Valiant](#)) (CS168, spring 2017)

[Lecture 1: Introduction and Consistent Hashing](#)

[Lecture 2: Approximate Heavy Hitters and the Count-Min Sketch](#)

[Lecture 3: Similarity Metrics and kd-Trees](#)

[Lecture 4: Dimensionality Reduction](#)

[Lecture 5: Generalization \(How Much Data Is Enough?\)](#)

[Lecture 6: Regularization](#)

[Lecture 7: Understanding and Using Principal Component Analysis \(PCA\)](#)

[Lecture 8: How PCA Works](#)

[Lecture 9: The Singular Value Decomposition \(SVD\) and Low-Rank Matrix Approximations](#)

[Lecture 10: Tensors, and Low-Rank Tensor Recovery](#)

[Lectures 11 and 12: Spectral Graph Theory](#)

[Lecture 13: Sampling and Estimation](#)

[Lecture 14: Markov Chain Monte Carlo](#)

[Lectures 15 and 16: The Fourier Transform and Convolution](#)

[Lecture 17: Compressive Sensing](#)

[Lecture 18: Linear and Convex Programming, with Applications to Sparse Recovery](#)

[Lecture 19: Expander Codes](#)

Old notes left on the cutting room floor

A Second Course in Algorithms (CS261, winter 2016)

[Lecture 1: Course Goals and Introduction to Maximum Flow](#)

[Lecture 2: Augmenting Path Algorithms for Maximum Flow](#)

[Lecture 3: The Push-Relabel Algorithm for Maximum Flow](#)

[Lecture 4: Applications of Maximum Flows and Minimum Cuts](#)

[Lecture 5: Minimum-Cost Bipartite Matching](#)

[Lecture 6: Generalizations of Maximum Flow and Bipartite Matching](#)

[Lecture 7: Linear Programming: Introduction and Applications](#)

[Lecture 8: Linear Programming Duality \(Part 1\)](#)

[Lecture 9: Linear Programming Duality \(Part 2\)](#)

[Lecture 10: The Minimax Theorem and Algorithms for Linear Programming](#)

[Lecture 11: Online Learning and the Multiplicative Weights Algorithm](#)

[Lecture 12: Applications of Multiplicative Weights to Games and Linear Programs](#)

[Lecture 13: Online Scheduling and Online Steiner Tree](#)

[Lecture 14: Online Bipartite Matching](#)

[Lecture 15: Introduction to Approximation Algorithms](#)

[Lecture 16: The Traveling Salesman Problem](#)

[Lecture 17: Linear Programming and Approximation Algorithms](#)

[Lecture 18: Five Essential Tools for the Analysis of Randomized Algorithms](#)

[Lecture 19: Beating Brute-Force Search](#)

[Lecture 20: The Maximum Cut Problem and Semidefinite Programming](#)

[Top 10 List](#)

Beyond Worst-Case Analysis (CS264, fall 2014, winter 2017)

Full set of notes from 2014

Additional new lectures in 2017

Older notes left on the cutting-room floor

Incentives in Computer Science (CS269I, fall 2016)

[Lecture 1: The Draw and College Admissions](#)

[Lecture 2: Stable Matching](#)

[Lecture 3: Strategic Voting](#)

[Lecture 4: Voting, Machine Learning, and Participatory Democracy](#)

[Lecture 5: Incentives in Peer-to-Peer Networks](#)

[Lecture 6: Incentivizing Participation](#)

[Lecture 7: Selfish Routing and Network Over-Provisioning](#)

[Lecture 8: Incentives in BGP Routing](#)

[Lecture 9: Incentives in Bitcoin Mining](#)

[Lecture 10: Incentives in Crowdsourcing](#)

[Lecture 12: Asymmetric Information and Reputation Systems](#)

[Lecture 13: Introduction to Auctions](#)

[Lecture 14: First-Price and Sponsored Search Auctions](#)

[Lecture 15: The VCG Mechanism](#)

[Lecture 16: Revenue-Maximizing Auctions](#)

[Lecture 17: Scoring Rules and Peer Prediction \(Incentivizing Honest Forecasts and Feedback\)](#)

[Lecture 18: Prediction Markets](#)

[Lecture 19: Time-Inconsistent Planning](#)

[Lecture 20: Fair Division](#)

Algorithmic Game Theory (CS364A, fall 2013)

The book [Twenty Lectures on Algorithmic Game Theory](#), Cambridge University Press (2016)

[Lecture 1: Introduction and Examples](#)

[Lecture 2: Mechanism Design Basics](#)

[Lecture 3: Myerson's Lemma](#)

[Lecture 4: Algorithmic Mechanism Design](#)

[Lecture 5: Revenue-Maximizing Auctions](#)

[Lecture 6: Simple Near-Optimal Auctions](#)

[Lecture 7: Multi-Parameter Mechanism Design and the VCG Mechanism](#)

[Lecture 8: Combinatorial and Wireless Spectrum Auctions](#)

[Lecture 9: Beyond Quasi-Linearity](#)

[Lecture 10: Kidney Exchange and Stable Matching](#)

[Lecture 11: Selfish Routing and the Price of Anarchy](#)

[Lecture 12: More on Selfish Routing](#)

[Lecture 13: Potential Games and a Hierarchy of Equilibrium Concepts](#)

[Lecture 14: Robust Price-of-Anarchy Bounds in Smooth Games](#)

[Lecture 15: Best-Case and Strong Nash Equilibria](#)

[Lecture 16: Best-Response Dynamics](#)

[Lecture 17: No-Regret Dynamics](#)

[Lecture 18: From External Regret to Swap Regret and the Minimax Theorem](#)

[Lecture 19: Pure Nash equilibria and PLS-Completeness](#)

[Lecture 20: Mixed Nash equilibria and PPAD-Completeness](#)

[Top 10 List](#)

Frontiers in Mechanism Design (CS364B, winter 2014)

[Lecture 1: Ascending and Ex Post Incentive Compatible Mechanisms](#)

[Lecture 2: Unit-Demand Bidders and Walrasian Equilibria](#)

[Lecture 3: The Crawford-Knoer Auction](#)

[Lecture 4: The Clinching Auction](#)

[Lecture 5: The Gross Substitutes Condition](#)

[Lecture 6: Gross Substitutes: Welfare Maximization in Polynomial Time](#)

[Bonus Lecture: Gross Substitutes and Greedy Algorithms](#)

[Lecture 7: Submodular Valuations](#)

[Lecture 8: MIR and MIDR Mechanisms](#)

[Lecture 9: MIDR Mechanisms via Scaling Algorithms](#)

[Lecture 10: Coverage Valuations and Convex Rounding](#)

[Lecture 11: Undominated Implementations and the Shrinking Auction](#)

[Lecture 12: Bayesian Incentive-Compatibility](#)

[Lecture 14: The Price of Anarchy in Simple Auctions](#)

[Lecture 15: The Price of Anarchy of Bayes-Nash Equilibria](#)

[Lecture 16: The Price of Anarchy First-Price Auctions](#)

[Lecture 17: Demand Reduction in Multi-Unit Auctions Revisited](#)

[Lecture 17.5: Beyond Smoothness and XOS Valuations](#)

[Lecture 18: Multi-Parameter Revenue Maximization](#)

[Lecture 19: Interim Rules and Border's Theorem](#)

[Lecture 20: Characterization of Revenue-Maximizing Auctions](#)

Older notes from Fall '05 (out of date)

Communication Complexity (for Algorithm Designers) (CS369E, winter 2015)

[Lecture 1: Data Streams: Algorithms and Lower Bounds](#)

[Lecture 2: Lower Bounds for One-Way Communication Complexity: Disjointness, Index, and Gap-Hamming](#)

[Lecture 3: Lower Bounds for Compressive Sensing](#)

[Lecture 4: Boot Camp on Communication Complexity](#)

[Lecture 5: Lower Bounds for the Extension Complexity of Polytopes](#)

[Lecture 6: Data Structure Lower Bounds](#)

[Lecture 7: Lower Bounds in Algorithmic Game Theory](#)

[Lecture 8: Lower Bounds in Property Testing](#)

[All lectures in one file](#)

[Version for Foundations and Trends in TCS](#)

Miscellaneous Lecture Notes

[Counting Triangles \(Suri-Vassilvitskii\)](#)

[Triangle-Dense Graphs \(Gupta-Roughgarden-Seshadhri\)](#)

[The Algorithmic Lovasz Local Lemma \(Moser\)](#)

[Strongly Connected Components in Linear Time](#)

[Deterministic Linear-Time Selection and Sorting Lower Bounds](#)

[Analysis of QuickSort](#)

Disclaimer: Some of these notes have been edited more than others.

Request for feedback: I always appreciate suggestions and corrections from readers.

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