

Database Management Systems

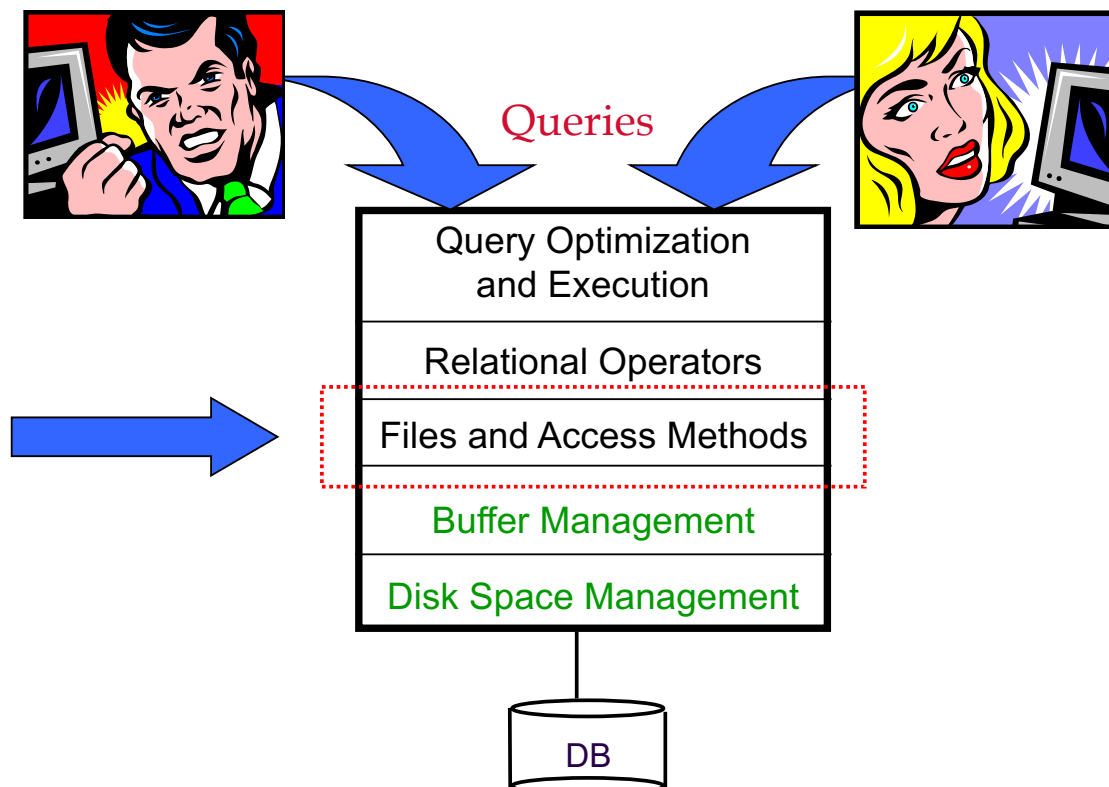
Fall 2019

Indexing

Chapters 8, 10, and 11

"If I had eight hours to chop down a tree,
I'd spend six sharpening my ax."
-- Abraham Lincoln

The BIG Picture



DBMS vs. OS File System

OS does disk space & buffer mgmt: why not let OS manage these tasks?

- **Some limitations, e.g., files can't span disks.**
 - Note, this is changing --- OS File systems are getting smarter (i.e., more like databases!)
- **Buffer management in DBMS requires ability to:**
 - **pin a page** in buffer pool, **force a page** to disk & **order writes** (important for implementing CC & recovery)
 - adjust *replacement policy*, and **pre-fetch pages** based on access patterns in typical DB operations.
- **Q: Compare DBMS Buffer Mgmt to OS Virtual Memory? to Processor Cache?**

Files of Records

- **Blocks interface for I/O, but...**
- **Higher levels of DBMS operate on *records*, and *files of records*.**
- **FILE: A collection of *pages*, each containing a collection of records. Must support:**
 - insert/delete/modify** record
 - fetch** a particular record (specified using *record id*)
 - scan** all records (possibly with some conditions on the records to be retrieved)
- **Note: typically**
page size = block size = frame size.

“MetaData” - System Catalogs

- **How to impose structure on all those bytes??**
 - **MetaData: “Data about Data”**
 - **For each relation:**
 - name, file location, file structure (e.g., Heap file)
 - attribute name and type, for each attribute
 - index name, for each index
 - integrity constraints
 - **For each index:**
 - structure (e.g., B+ tree) and search key fields
 - **For each view:**
 - view name and definition
 - **Plus statistics, authorization, buffer pool size, etc.**
- Q: But how to store the catalogs???*

Catalogs are Stored as Relations!

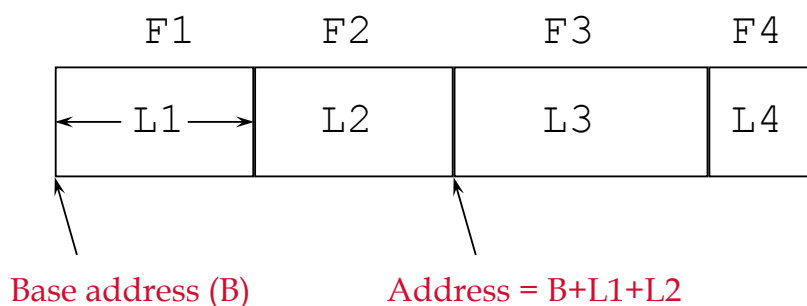
attr_name	rel_name	type	position
attr_name	Attribute_Cat	string	1
rel_name	Attribute_Cat	string	2
type	Attribute_Cat	string	3
position	Attribute_Cat	integer	4
sid	Students	string	1
name	Students	string	2
login	Students	string	3
age	Students	integer	4
gpa	Students	real	5
fid	Faculty	string	1
fname	Faculty	string	2
sal	Faculty	real	3

`Attr_Cat(attr_name, rel_name, type, position)`

It's a bit more complicated...

```
Terminal — psql — 99x28
joeh=# \dt pg_attribute
No matching relations found.
joeh=# \d pg_attribute
Table "pg_catalog.pg_attribute"
  Column      | Type      | Modifiers
-----+-----+-----
attrelid      | oid       | not null
attname       | name      | not null
atttypid      | oid       | not null
attstattarget | integer   | not null
attlen        | smallint  | not null
attnum        | smallint  | not null
attndims      | integer   | not null
attcacheoff   | integer   | not null
atttypmod     | integer   | not null
attbyval      | boolean   | not null
attstorage    | "char"    | not null
attalign      | "char"    | not null
attnotnull    | boolean   | not null
attahasdef    | boolean   | not null
attisdropped  | boolean   | not null
attislocal    | boolean   | not null
attinhcount   | integer   | not null
Indexes:
    "pg_attribute_relid_attnam_index" UNIQUE, btree (attrelid, attname)
    "pg_attribute_relid_attnum_index" UNIQUE, btree (attrelid, attnum)
joeh=#
```

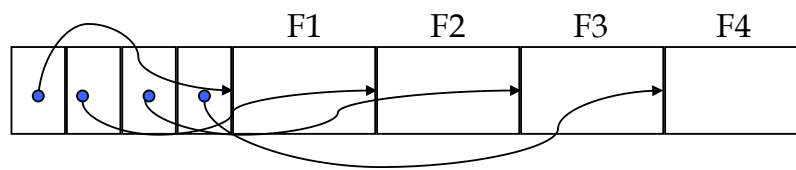
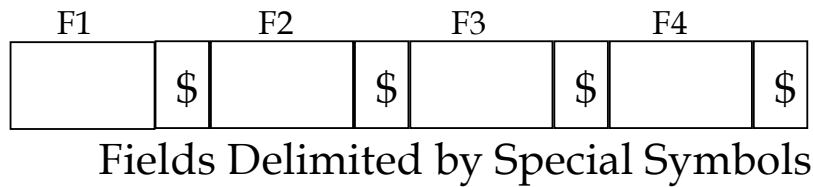
Record Formats: Fixed Length



- Information about field types same for all records in a file; stored in *system catalogs*.
- Finding *i'th* field done via arithmetic.

Record Formats: Variable Length

- **Two alternative formats (# fields is fixed):**

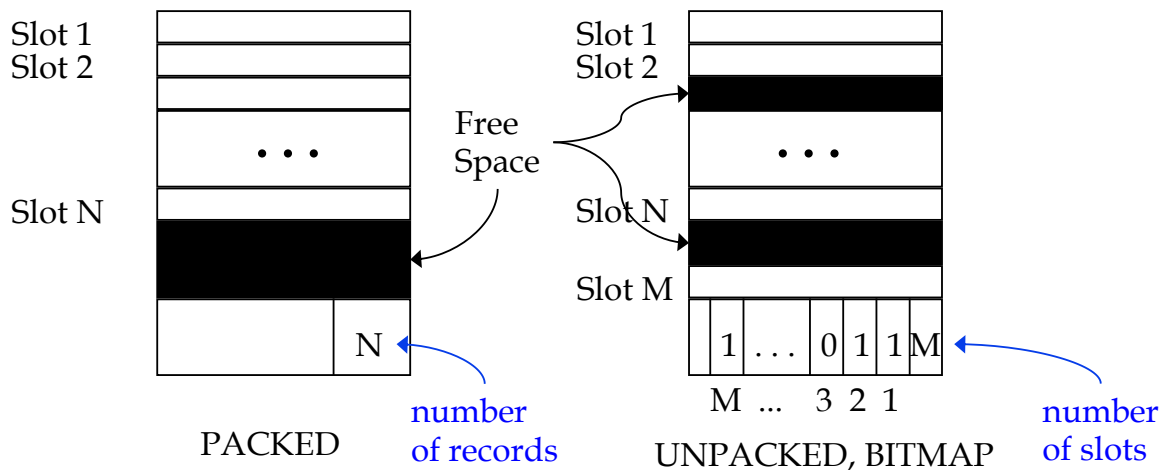


➡ Second offers direct access to *i*'th field, efficient storage of *nulls* (special *don't know* value); small directory overhead.

How to Identify a Record?

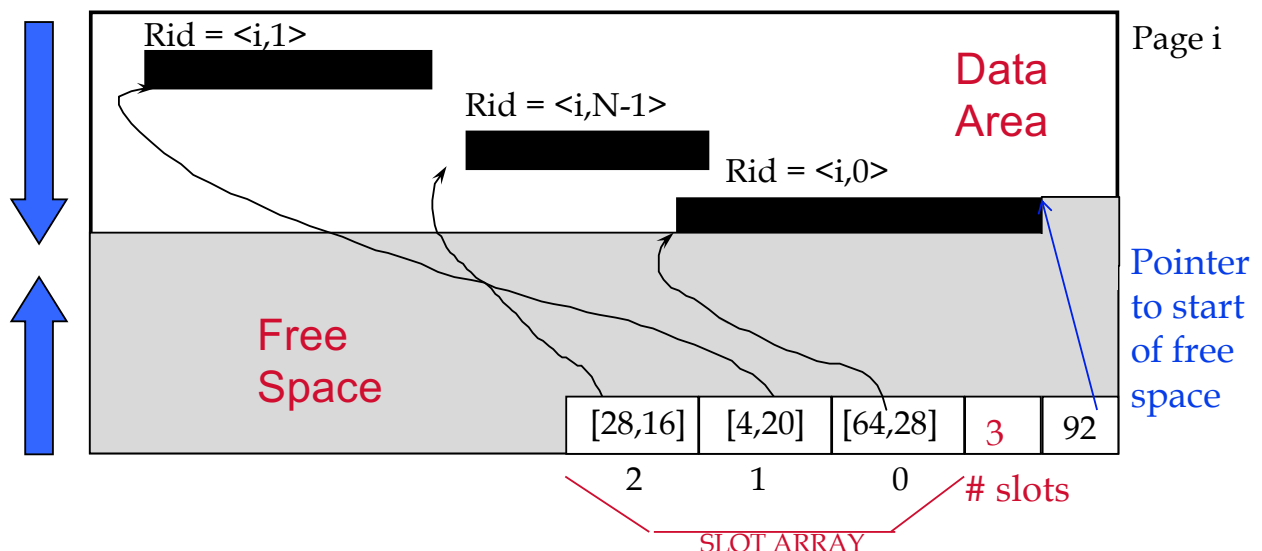
- **The Relational Model doesn't expose "pointers", but that doesn't mean that the DBMS doesn't use them internally.**
- **Q: Can we use memory addresses to "point" to records?**
- **Systems use a "Record ID" or "RecID"**

Page Formats: Fixed Length Records



➤ **Record id = <page id, slot #>.** In first alternative, moving records for free space management changes rid; may not be acceptable.

"Slotted Page" for Variable Length Records



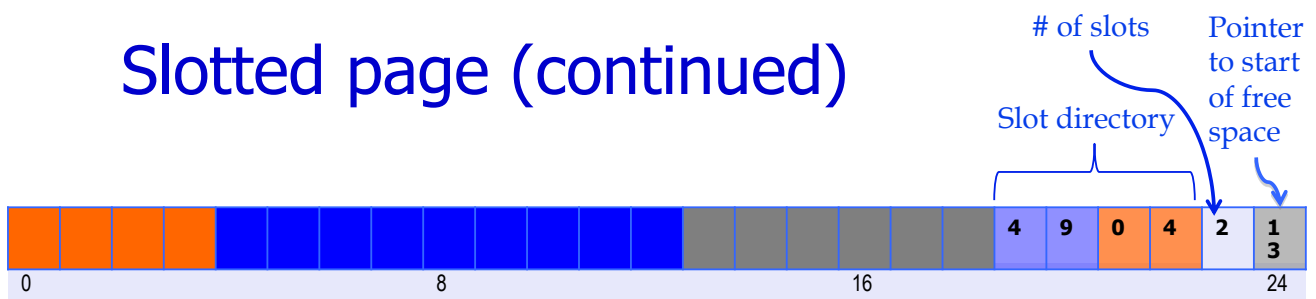
- **Slot contains: [offset (from start of page), length]**
 - in bytes
- **Record id = <page id, slot #>**

- Page is full when data space and slot array

Slotted Page (continued)

- **When need to allocate:**
 - If enough room in free space, use it and update free space pointer.
 - Else, try to compact, if successful, use the freed space.
 - Else, tell caller that page is full.
- **Advantages:**
 - Can move records around in page without changing their record ID
 - Allows lazy space management within the page, with opportunity for clean up later

Slotted page (continued)



- **What's the biggest record you can add to the above page?**
 - Need 2 bytes for slot: [offset, length] plus record.
- **What happens when a record needs to move to a different page?**
 - Leave a "tombstone" behind, pointing to new page and slot.
 - Record id remains unchanged – no more than one hop needed.

So far we've organized:

- **Fields into Records (fixed and variable length)**
- **Records into Pages (fixed and variable length)**

Now we need to organize Pages into Files

Alternative File Organizations

Many alternatives exist, *each good for some situations, and not so good in others:*

Heap files: Unordered. Suitable when typical access is a file scan retrieving all records. Easy to maintain.

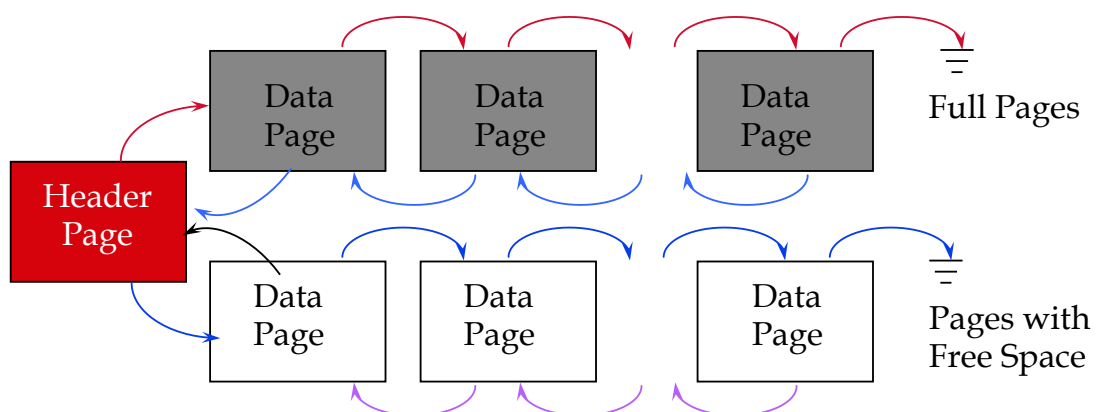
Sorted Files: Best for retrieval in *search key* order, or if only a 'range' of records is needed. Expensive to maintain.

Clustered Files (with Indexes): A compromise between the above two extremes.

Unordered (Heap) Files

- **Simplest file structure contains records **in no particular order**.**
- **As file grows and shrinks, pages are allocated and de-allocated.**
- **To support record level operations, we must:**
 - keep track of the *pages* in a file
 - keep track of *free space* on *pages*
 - keep track of the *records* on a page
- **Can organize as a list, as a directory, a tree, ...**

Heap File Implemented as a List



- **The Heap file name and header page id must be stored persistently.**
The catalog is a good place for this.
- **Each page contains 2 `pointers' plus data.**

Cost Model for Analysis



We ignore CPU costs, for simplicity

- **B:** The number of data blocks
 - **R:** Number of records per block
 - **D:** (Average) time to read or write disk block
- **Measuring number of block I/O's ignores gains of pre-fetching and sequential access; thus, even I/O cost is only loosely approximated.**
 - **Average-case analysis; based on several simplistic assumptions.**
 - Often called a back of the envelope calculation. *Good enough to show the overall trends!*

Some Assumptions in the Analysis

- **Single record insert and delete.**
- **Equality selection - exactly one match (what if more or less???)**.
- **For Heap Files we'll assume:**
 - Insert always appends to end of file.
 - Delete just leaves free space in the page.
 - Empty pages are not deallocated.

Cost of Operations

B: The number of data pages
R: Number of records per page
D: (Average) time to read or write disk page

	Heap File	Sorted File	Clustered File
Scan all records	BD		
Equality Search (unique key)	0.5 BD		
Range Search	BD		
Insert	2D		
Delete	$(0.5B+1)D$		

Sorted Files

- Heap files are **lazy** on **update** - you end up paying on searches.
- Sorted files **eagerly** maintain the file on **update**.
 - The opposite choice in the trade-off
- **Let's consider an extreme version**
 - No gaps allowed, pages fully packed always
 - Q: How might you relax these assumptions?
- **Assumptions for our BotE Analysis:**
 - Files compacted after deletions.
 - Searches are on sort key field(s).

Cost of Operations

B: The number of data pages
R: Number of records per page
D: (Average) time to read or write disk page

	Heap File	Sorted File	Clustered File
Scan all records	BD	BD	
Equality Search (unique key)	0.5 BD	$(\log_2 B) * D$	
Range Search	BD	$[(\log_2 B) + \text{\#match pg}] * D$	
Insert	2D	$((\log_2 B) + B)D$ <i>(because rd,w0.5 File)</i>	
Delete	$(0.5B+1)D$	Same cost as Insert	

The Problem(s) with Sorted Files

1) Expensive to maintain

- Especially if you want to keep the records packed tightly.
- Q: What if you are willing to relax that constraint?

2) Can only sort according to a single **search key**

- File will effectively be a "heap" file for access via any other search key.
- e.g., how to search for a particular student id in a file sorted by major?

Indexes: Introduction

- Sometimes, we want to retrieve records by specifying *values in one or more fields*, e.g.,
 - Find all students in the “CS” department
 - Find all students with a gpa > 3.0
 - Find all students in CS with a gpa > 3.0
- An *index* on a file is a disk-based data structure that speeds up selections on some *search key fields*.
 - Any subset of the fields of a relation can be the search key for an index on the relation.
 - *Search key* is *not* the same as *key*
 - e.g., Search key doesn't have to be unique.

Indexes: Overview

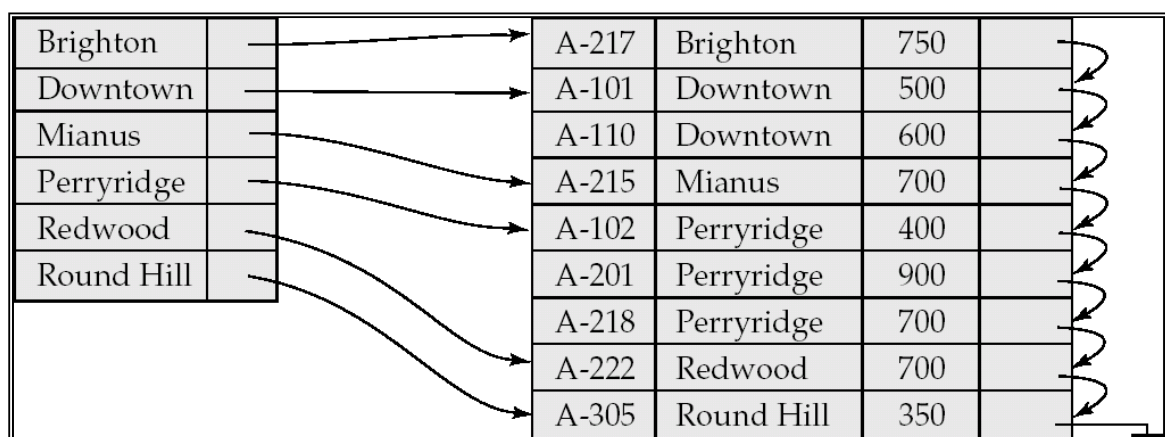
- An index contains a collection of *data entries*, and supports efficient retrieval of all records with a given search key value *k*.
 - Typically, index also contains auxiliary information that directs searches to the desired data entries
- Many indexing techniques exist:
 - B+ trees, hash-based structures, R trees, ...
- Can have multiple (different) indexes per file.
 - E.g. file sorted by *age*, with a hash index on *salary* and a B+tree index on *name*.

Indexes: Overview

- **The index file usually occupies considerably less disk blocks than the data file because its entries are much smaller**
- **A binary search on the index yields a pointer to the file record**
- **Indexes can also be characterized as dense or sparse**

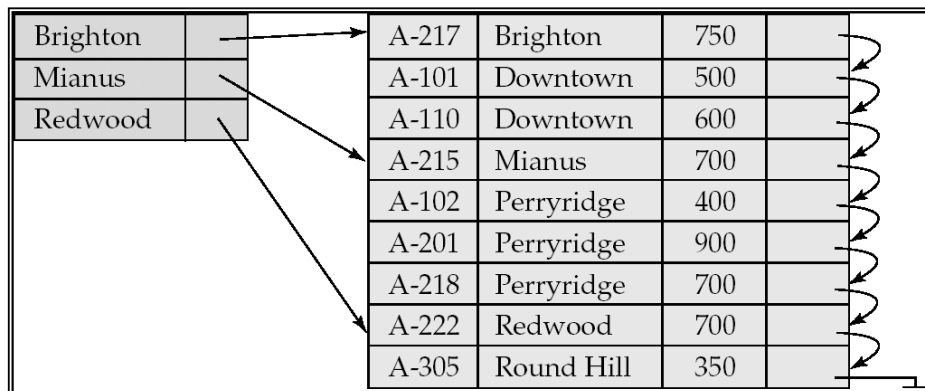
Dense Index Files

- **Dense index — Index record appears for every search-key value in the file.**

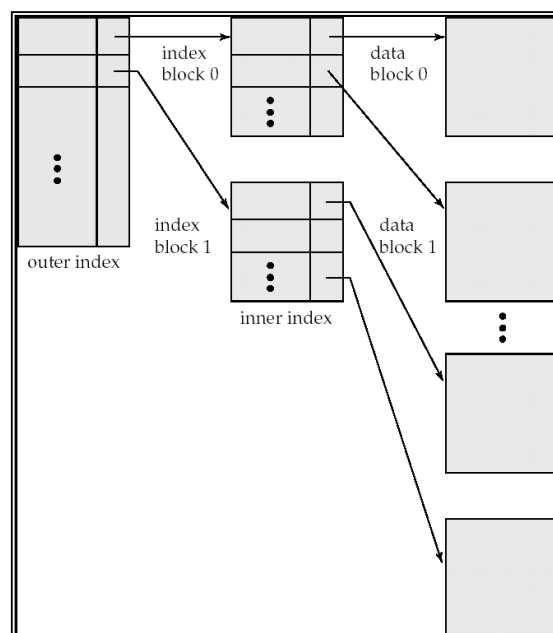


Sparse Index Files

- **Sparse Index: contains index records for only some search-key values.**
 - Applicable when records are sequentially ordered on search-key
- **To locate a record with search-key value K we:**
 - Find index record with largest search-key value $< K$
 - Search file sequentially starting at the record to which the index record points



Multilevel Index (Cont.)



Basic Concepts

- **Indexing mechanisms used to speed up access to desired data.**
 - E.g., author catalog in library
- **Search Key - attribute to set of attributes used to look up records in a file.**
- **An index file consists of records (called index entries) of the form**

search-key	pointer
------------	---------

- **Index files are typically much smaller than the original file**
- **Two basic kinds of indices:**
 - **Ordered indices:** search keys are stored in sorted order
 - **Hash indices:** search keys are distributed uniformly across “buckets” using a “hash function”.

Index Classification

- 1. Selections (lookups) supported**
- 2. Representation of data entries in index**
 - what kind of info is the index actually storing?
 - 3 alternatives here
- 3. Clustered vs. Unclustered Indexes**
- 4. Single Key vs. Composite Indexes**
- 5. Tree-based, hash-based, other**

Indexes: Selections supported

field <op> constant

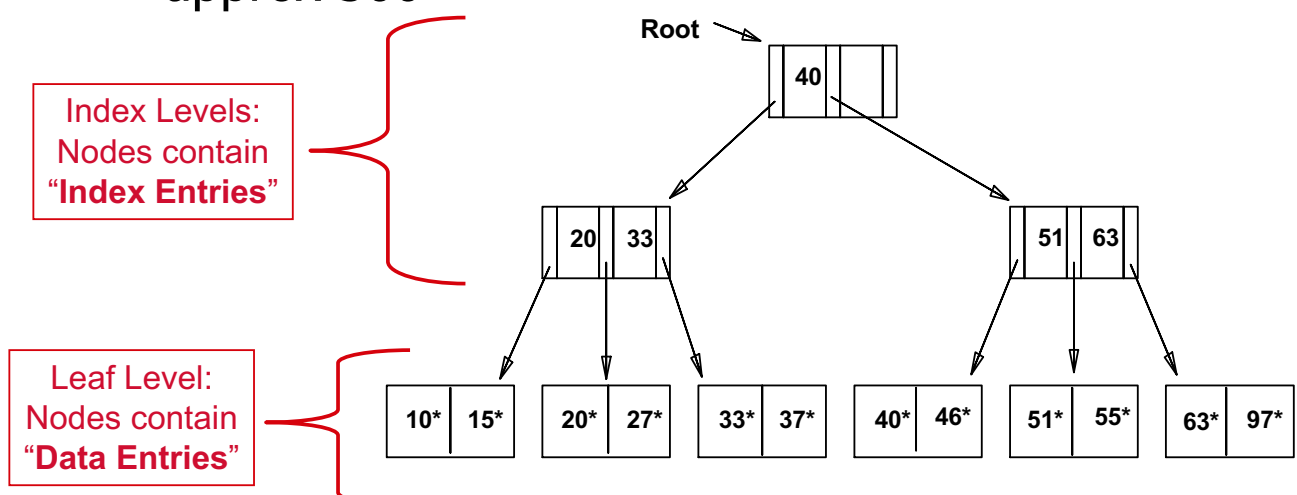
- **Equality** selections (*op* is =)
 - Either "tree" or "hash" indexes help here.
- **Range** selections (*op* is one of <, >, <=, >=, BETWEEN)
 - "Hash" indexes don't work for these.

More exotic selections

- multi-dimensional ranges ("east of Berkeley and west of Truckee and North of Fresno and South of Eureka")
- multi-dimensional **distances** ("within 2 miles of Soda Hall")
- Ranking queries ("10 restaurants closest to Berkeley")
- Regular expression matches, genome string matches, etc.
- Keyword/Web search - includes "importance" of words in documents, link structure, ...

Tree Index: Example

- **Index entries**: <search key value, page id>
they direct search for data entries *in leaves*.
- In example: **Fanout** (F) = 3 (note: unrealistic!)
 - more typical: 16KB page, 67% full, 32Byte entries
= approx 300



What's in a "Data Entry"?

- **Question:** What is actually stored in the leaves of the index for key value "k"? (a data entry for key "k" is denoted "k*" in book and examples)
- **Three alternatives:**
 1. Actual data record(s) with key value **k**
 2. {<**k**, rid of a matching data record>}
 3. <**k**, {rids of all matching data records}>
- **Choice is orthogonal to the indexing technique.**
 - e.g., B+ trees, hash-based structures, R trees, ...

Alt 1= "Index-Organized File"

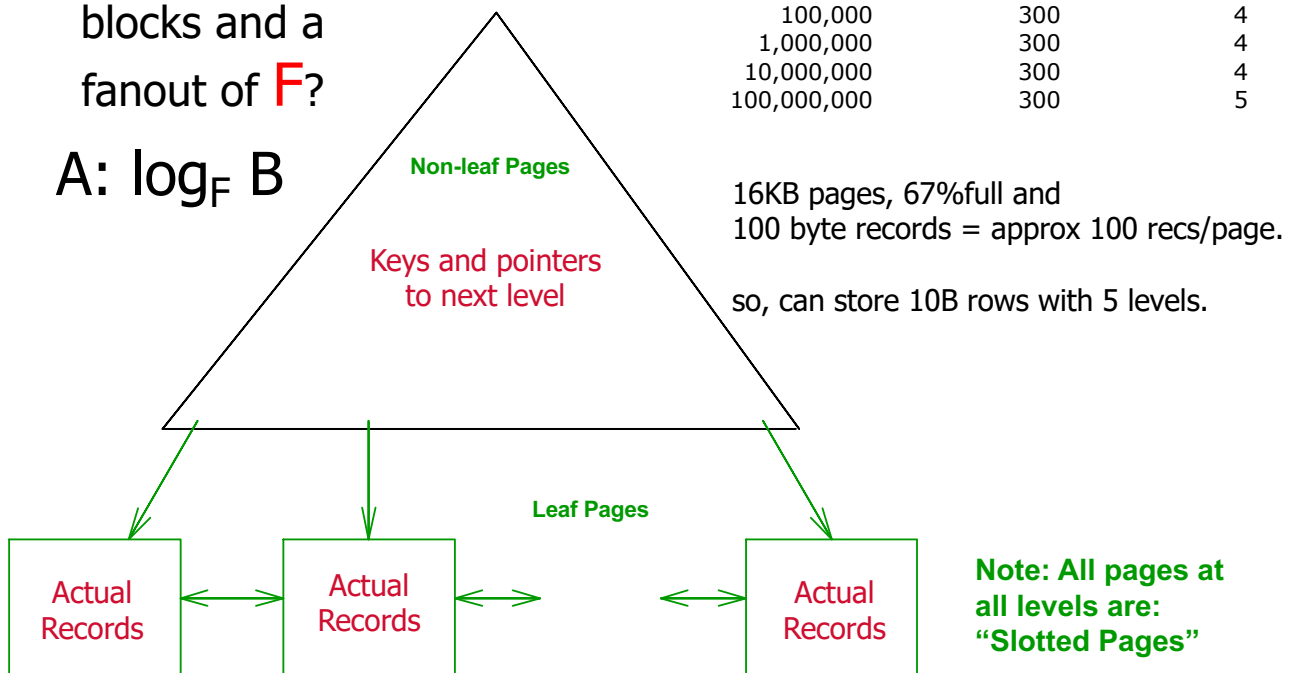
- **Actual data records are stored in leaves.**
 - If this is used, index structure becomes a file organization for data records (e.g., a sorted file).
 - At most one index on a given collection of data records can use Alternative 1.
 - This alternative saves pointer lookups but can be expensive to maintain with insertions and deletions.

Index-Organized File

Q: How many levels if **B** leaf blocks and a fanout of **F**?

A: $\log_F B$

# Leaf Blocks	Fanout	Levels
1,000	300	3
10,000	300	3
100,000	300	4
1,000,000	300	4
10,000,000	300	4
100,000,000	300	5



B: The size of the data (in pages)
R: Number of records per page
D: (Average) time to read or write disk page

Operation Cost

	Heap File	Sorted File (100% Occupancy)	Index-Organized File (67% Occupancy)
Scan all records	BD	BD	1.5 BD (bcos 67% full)
Equality Search <i>unique key</i>	0.5 BD	$(\log_2 B) * D$	$(\log_F 1.5B) * D$
Range Search	BD	$[(\log_2 B) + \text{\#match pg}] * D$	$((\log_F 1.5B) + \text{\#match pg}) * D$
Insert	2D	$((\log_2 B) + B)D$	$((\log_F 1.5B) + 1)D$
Delete	$(0.5B + 1)D$	$((\log_2 B) + B)D$ (because rd, wrt 0.5 file)	$((\log_F 1.5B) + 1)D$

Alternatives for Data Entries (Contd.)

Alternative 2

{<k, rid of a matching data record>}

and Alternative 3

<k, {rids of all matching data records}>

- Easier to maintain than Index-Organized.
 - On the other hand: Index-organized could be faster for reads.
- If more than one index is required on a given file, at most one index can use Alt 1; rest must use 2 or 3.
- Alt 3 more compact than Alt 2, but has *variable sized* data entries even with fixed-length search keys
- Even worse, for large rid lists the data entry would have to span multiple blocks!

Clustered vs. Unclustered Index

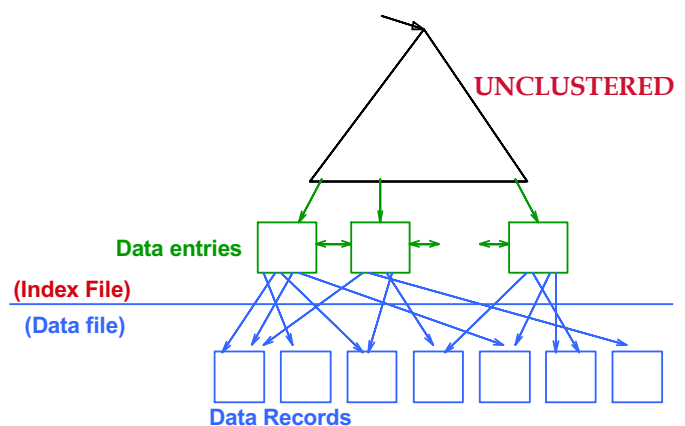
"Clustered" Index: the order of **data records is the same as, or `close to', the order of **index data entries**.**

- A file can be **clustered** on at most one search key.
- Cost of retrieving data records through index varies *greatly* based on whether index is clustered or not!
- Index-organized implies clustered ***but not vice-versa.***
 - In other words, alt-1 is always clustered
 - alt 2 and alt 3 may or may not be clustered.

Example: Alt 2 index for a Heap File

For alts 2 or 3, typically two files – one for data records and one for the index.

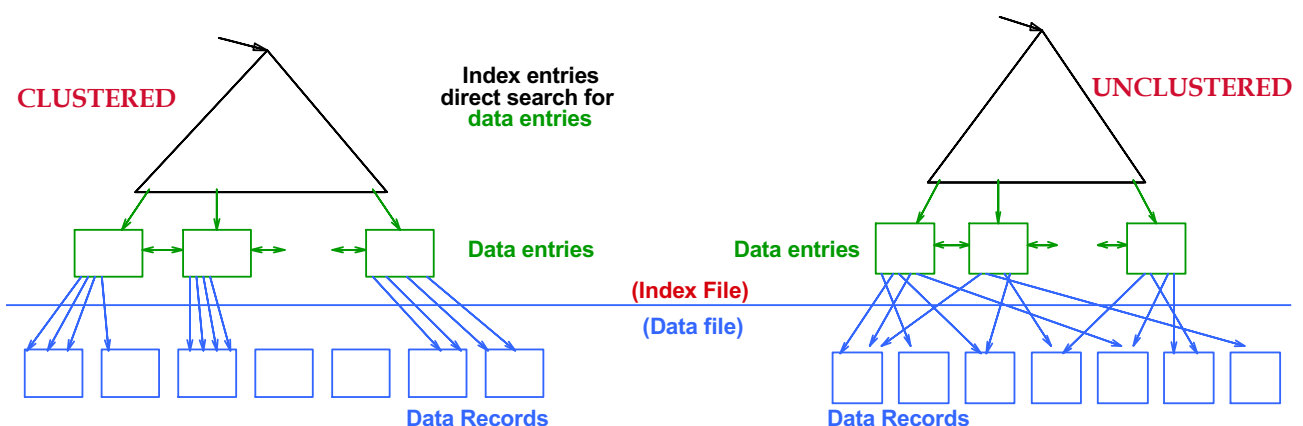
For an unclustered index, the order of data records in the data file is unrelated to the order of the data entries in the leaf level of the index.



Example: Alt 2 index for a Heap File

For a clustered index:

- **Sort the heap file on the search key column(s)**
 - Leave some free space on pages for future inserts
- **Build the index**
- **Use overflow pages in data file if necessary**
 - Thus, clustering is only approximate – data records may not be exactly in sort order (can clean up later)



Unclustered vs. Clustered Indexes

- **What are the tradeoffs????**
- **Clustered Pros**
 - Efficient for range searches
 - May be able to do some types of compression
 - Possible locality benefits (related data?)
 - ???
- **Clustered Cons**
 - Maintenance cost (pay on the fly or be lazy with reorganization)
 - Can only cluster according to a single order

Operation Cost

B: The size of the data (in pages)

D: (Avg) time to read or write disk page

	Unclustered Alt-2 Tree Idx (Index file: 67% occupancy) (Data file: 100% occupancy)	Clustered Alt-2 Tree Idx (Index and Data files: 67% occupancy)
Scan all records	BD (ignore index)	1.5 BD (ignore index)
Equality Search <i>unique key</i>	$(1 + \log_F 0.5 B) * D$ assume an index entry is 1/3 the size of a record so index leaf level = $.33 * 1.5B = 0.5B$	$(1 + \log_F 0.5B) * D$
Range Search	$[(\log_F 0.5B) + \# \text{matching_leaf_pages} - 1 + \# \text{match} \text{ records}] * D$	$((\log_F 0.5B) + \# \text{match} \text{ pages}) * D$
Insert	$((\log_F 0.5B) + 3)D$	$((\log_F 0.5B) + 3)D$
Delete	same as insert	same as insert

Composite Search Keys

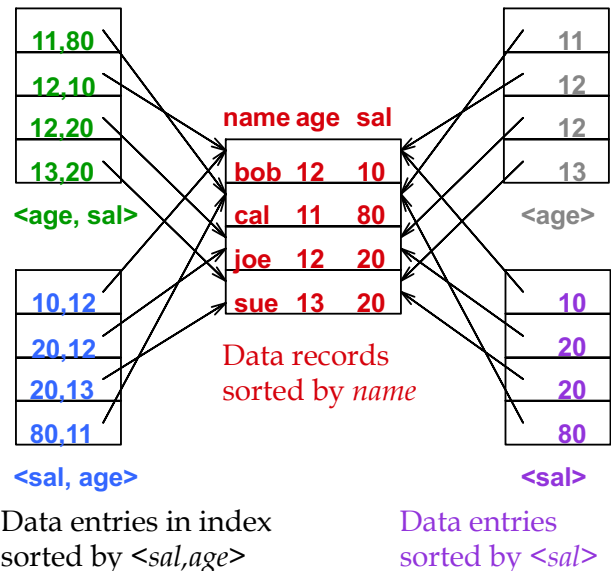
- **Search on a combination of fields.**

- Equality query: Every field value is equal to a constant value. E.g. wrt $\langle \text{age}, \text{sal} \rangle$ index:
 - age=20 and sal =75
- Range query: Some field value is not a constant. E.g.:
 - age > 20; or age=20 and sal > 10

- **Data entries in index sorted by search key to support range queries.**

- **Lexicographic order**
- Like the dictionary, but on fields, not letters!

Examples of composite key indexes using lexicographic order.



Index Classification Revisited

1. Selections (lookups) supported

2. Representation of data entries in index

- what kind of info is the index actually storing?
- 3 alternatives here

3. Clustered vs. Unclustered Indexes

4. Single Key vs. Composite Indexes

5. Tree-based, hash-based, other

Tree-Structured Indexes

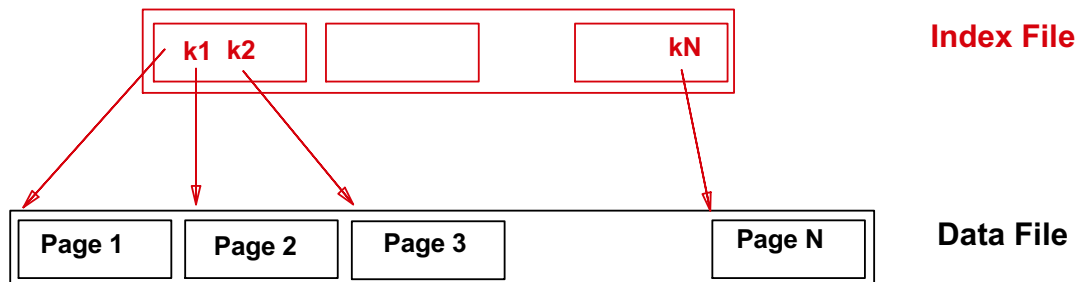
- **Tree-structured indexing techniques support both *range searches* and *equality searches*.**
- **Two examples:**
 - ISAM: static structure; early index technology.
 - B+ tree: dynamic, adjusts gracefully under inserts and deletes.

ISAM = Indexed Sequential Access Method

- **ISAM is an old-fashioned idea**
 - B+ trees are usually better, as we'll see
 - Though not *always*
- **But, it's a good place to start**
 - Simpler than B+ tree, but many of the same ideas
- **Upshot**
 - **Don't** brag about being an ISAM expert on your resume
 - **Do** understand how they work, and tradeoffs with B+ trees

Range Searches

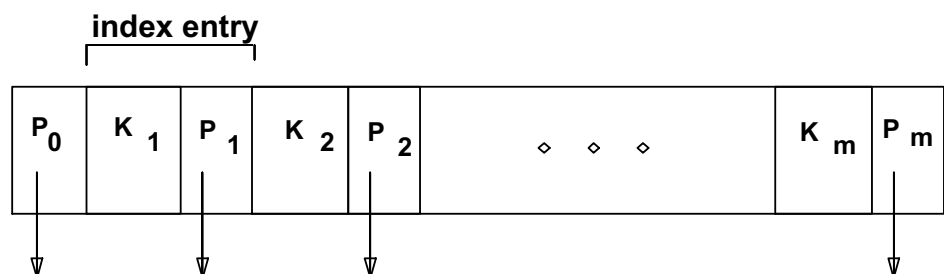
- **Find all students with gpa > 3.0'**
 - If data is in sorted file, do binary search to find first such student, then scan to find others.
 - Cost of binary search on disk is still quite high.
- **Simple idea: Create an 'index' file.**



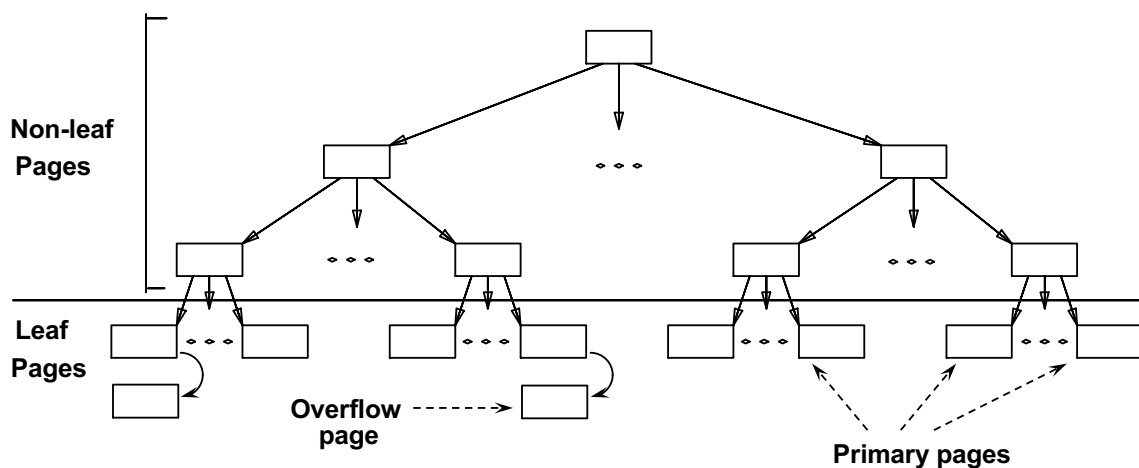
☛ Can do binary search on (smaller) index file!

☛ But what if index doesn't fit easily in memory?

ISAM

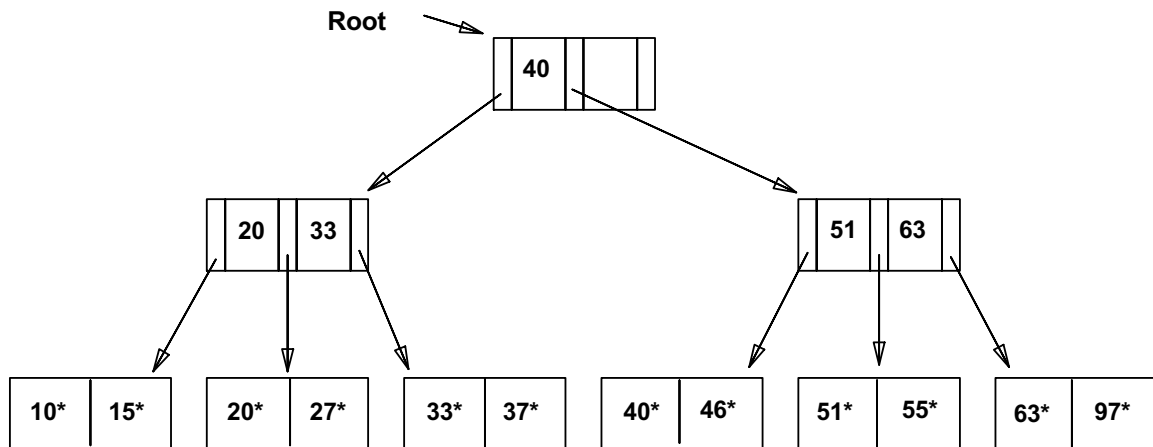


- **We can apply the idea repeatedly!**



Example ISAM Tree

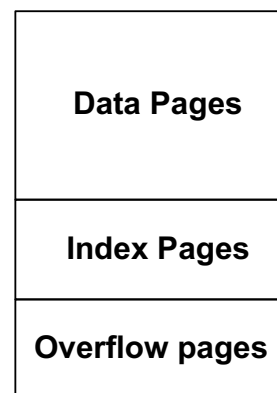
- *Index entries*: <search key value, page id> they direct search for data entries *in leaves*.
- Example where each node can hold 2 entries;



ISAM has a STATIC Index Structure

File creation:

1. Allocate leaf (data) pages sequentially
2. Sort records by search key
3. Allocate index pages
4. Allocate overflow pages



ISAM File Layout

Static tree structure: *inserts/deletes affect only leaf pages.*

ISAM (continued)

Search: Start at root; use key comparisons to navigate to leaf.

$$\text{Cost} = \log_F N$$

$$F = \# \text{ entries/pg (i.e., fanout)}$$

$$N = \# \text{ leaf pgs}$$

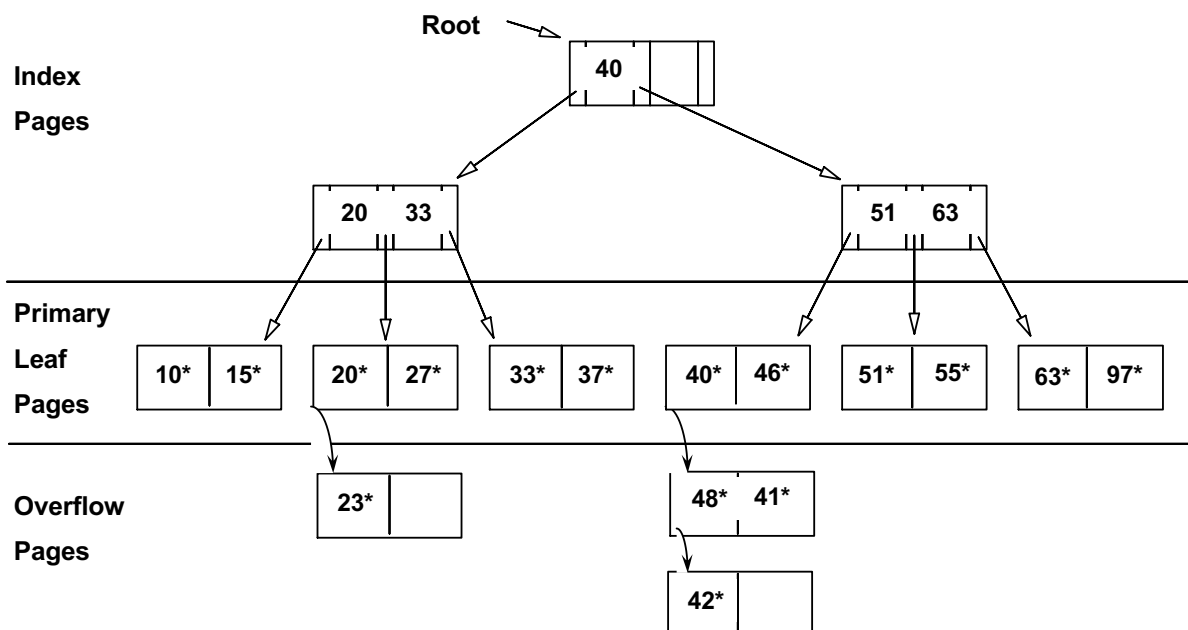
- no need for 'next-leaf-page' pointers. (Why?)

Insert: Find leaf that data entry belongs to, and put it there. Overflow page if necessary.

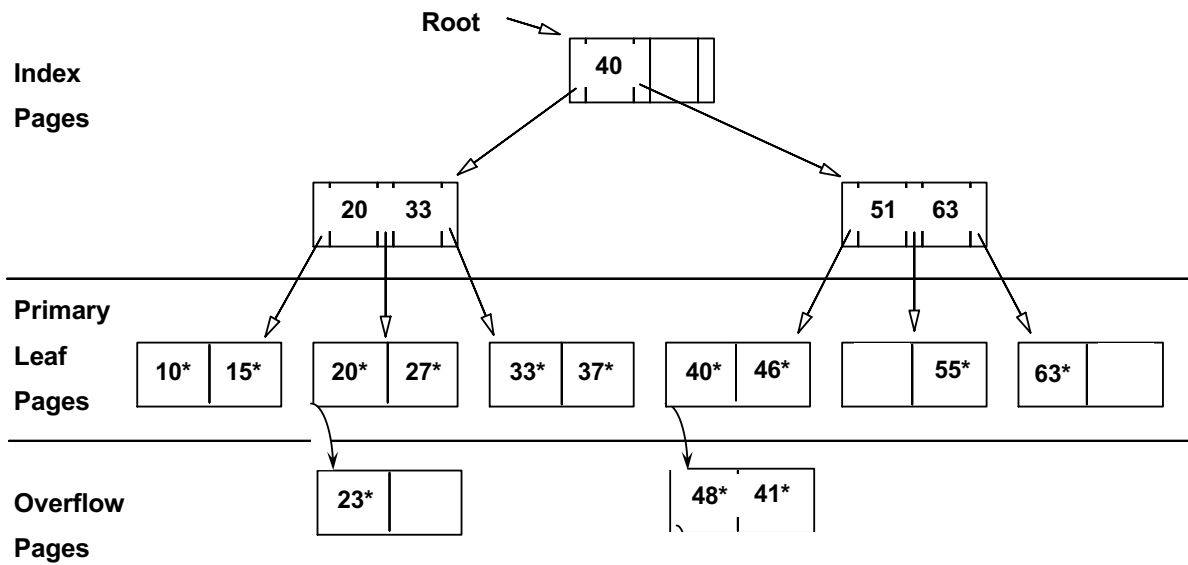
Delete: Find; remove from leaf; if empty de-allocate.

Data Pages
Index Pages
Overflow pages

Example: Insert 23*, 48*, 41*, 42*



... then Deleting 42*, 51*, 97*



☞ Note that 51* appears in index levels, but not in leaf!

ISAM ---- Issues?

- **Pros**

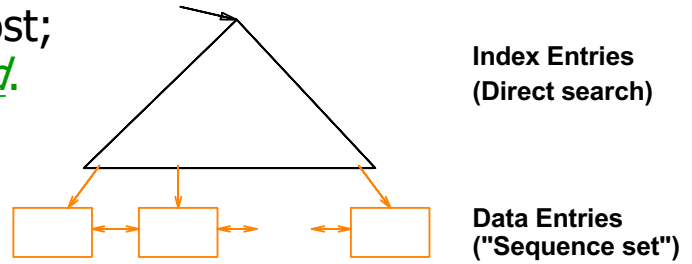
- ????

- **Cons**

- ????

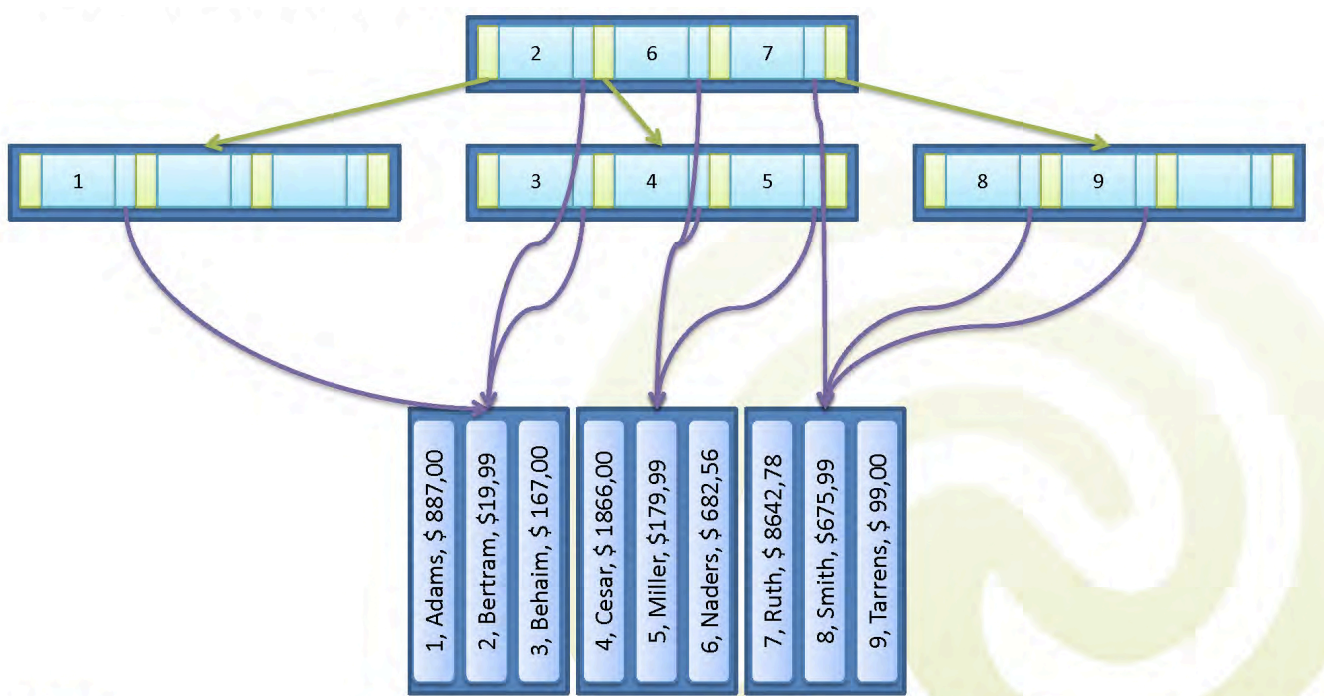
B+ Tree: The Most Widely Used Index

- Insert/delete at $\log_F N$ cost;
keep tree height-balanced.
 $N = \#$ leaf pages



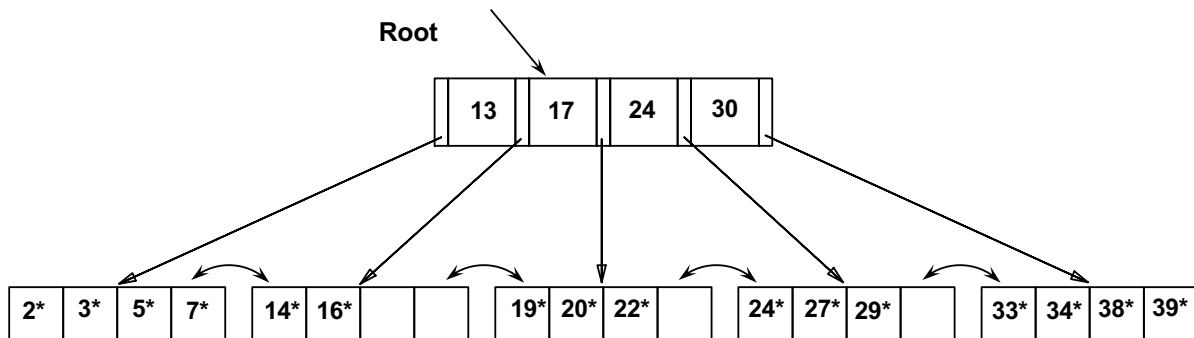
- Each node (**except for root**) contains m entries:
 $d \leq m \leq 2d$ entries.
- " d " is called the order of the tree.
(maintain 50% min occupancy)
- Supports equality and range-searches efficiently.
- As in ISAM, all searches go from root to leaves, but structure is dynamic.

B+ Tree: The Most Widely Used Index



Example B+ Tree

- Search begins at root page, and key comparisons direct it to a leaf (as in ISAM).
- Search for 5*, 15*, all data entries $\geq 24^*$...



A Note on Terminology

- The "+" in B+Tree indicates that it is a special kind of "B Tree" in which **all the data entries reside in leaf pages**.
 - In a vanilla "B Tree", data entries are sprinkled throughout the tree.
- B+Trees are in many ways simpler to implement than B Trees.
 - And since we have a large fanout, the upper levels comprise only a tiny fraction of the total storage space in the tree.
- To confuse matters, most database people call B+Trees "B Trees"!!!

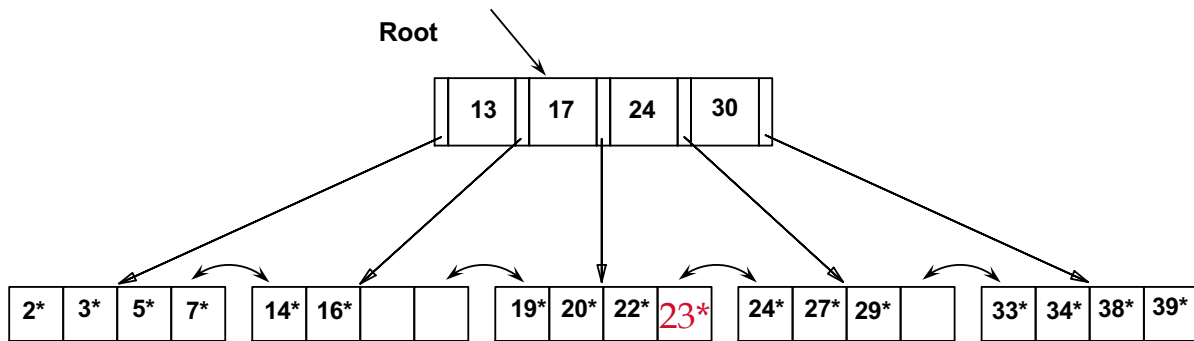
B+ Trees in Practice

- **Remember = Index nodes are disk pages**
 - e.g., fixed length unit of communication with disk
- **Typical order: 100. Typical fill-factor: 67%.**
 - average fanout = 133
- **Typical capacities:**
 - Height 3: $133^3 = 2,352,637$ entries
 - Height 4: $133^4 = 312,900,700$ entries
- **Can often hold top levels in buffer pool:**
 - Level 1 = 1 page = 8 Kbytes
 - Level 2 = 133 pages = 1 Mbyte
 - Level 3 = 17,689 pages = 133 MBytes

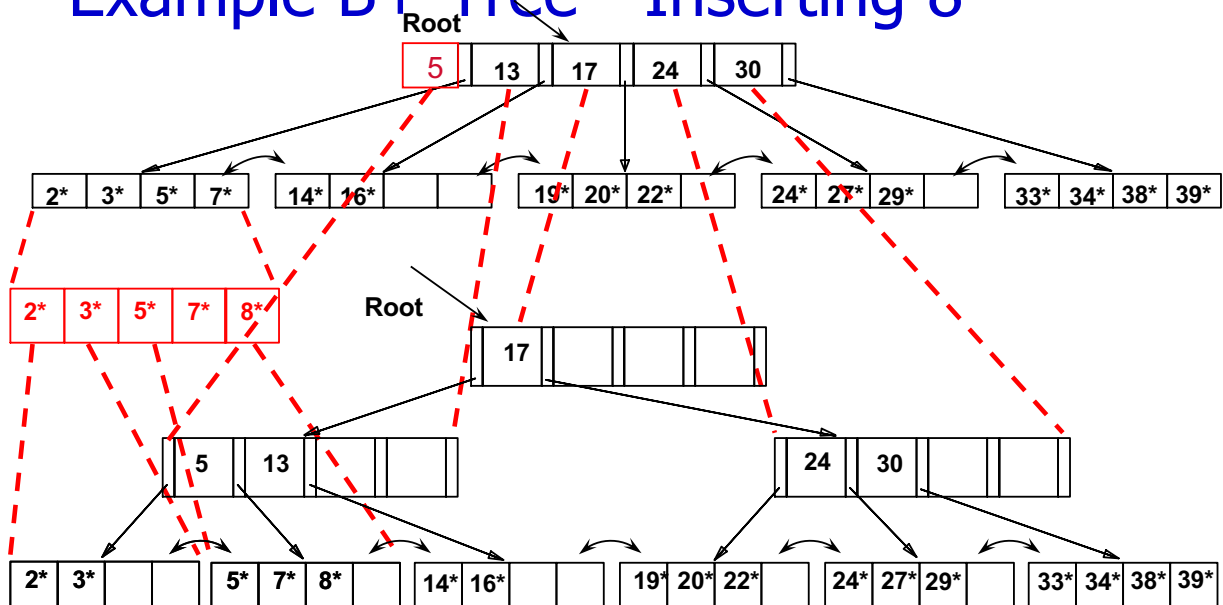
Inserting a Data Entry into a B+ Tree

- **Find correct leaf L .**
- **Put data entry onto L .**
 - If L has enough space, *done!*
 - Else, must split L (into L and a new node $L2$)
 - Redistribute entries evenly, copy up middle key.
 - Insert index entry pointing to $L2$ into parent of L .
- **This can happen recursively**
 - To split index node, redistribute entries evenly, but push up middle key. (Contrast with leaf splits.)
- **Splits “grow” tree; root split increases height.**
 - Tree growth: gets wider or one level taller at top.

Example B+ Tree – Inserting 23*



Example B+ Tree - Inserting 8*

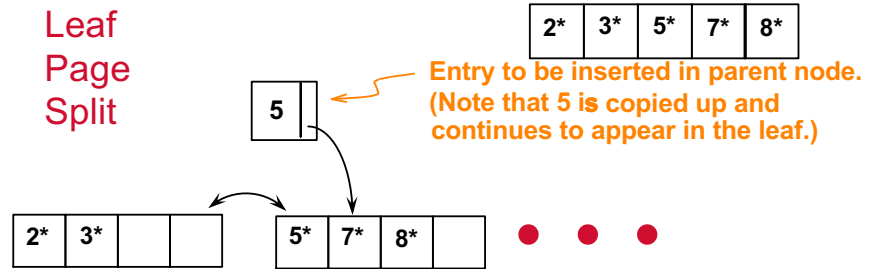


- ❖ Notice that root was split, leading to increase in height.
- ❖ In this example, we could avoid split by re-distributing entries; however, this is not done in practice.

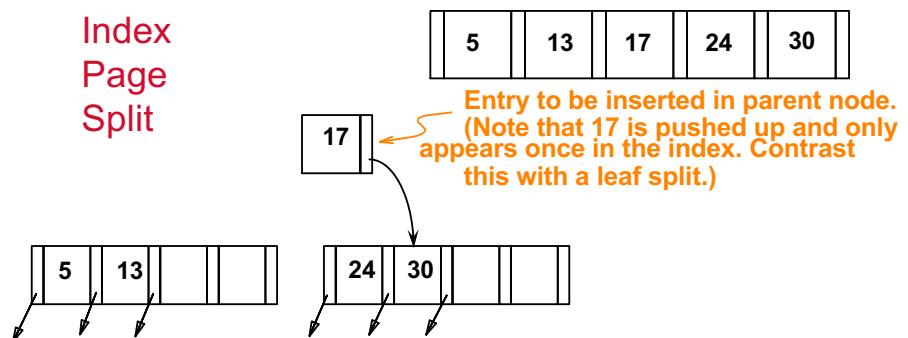
Leaf vs. Index Page Split

(from previous example of inserting "8")

- Observe how minimum occupancy is guaranteed in both leaf and index pg splits.



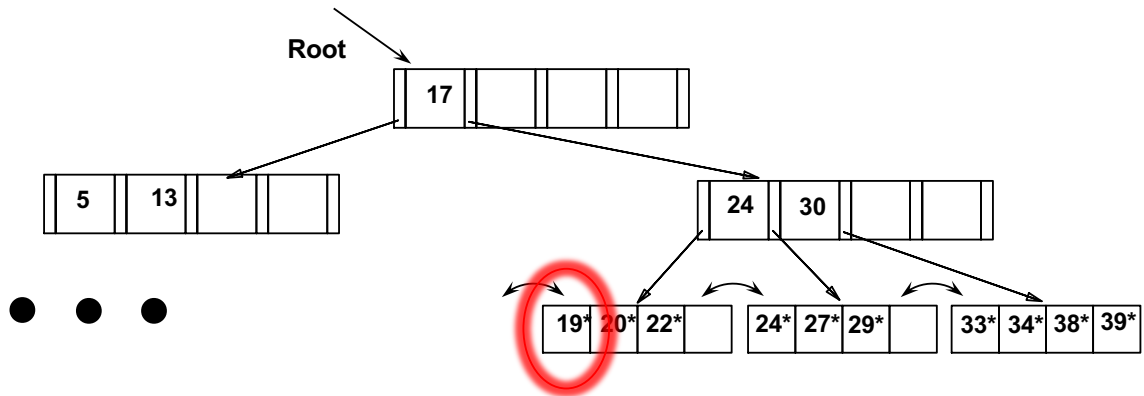
- Note difference between *copy-up* and *push-up*; be sure you understand the reasons for this.



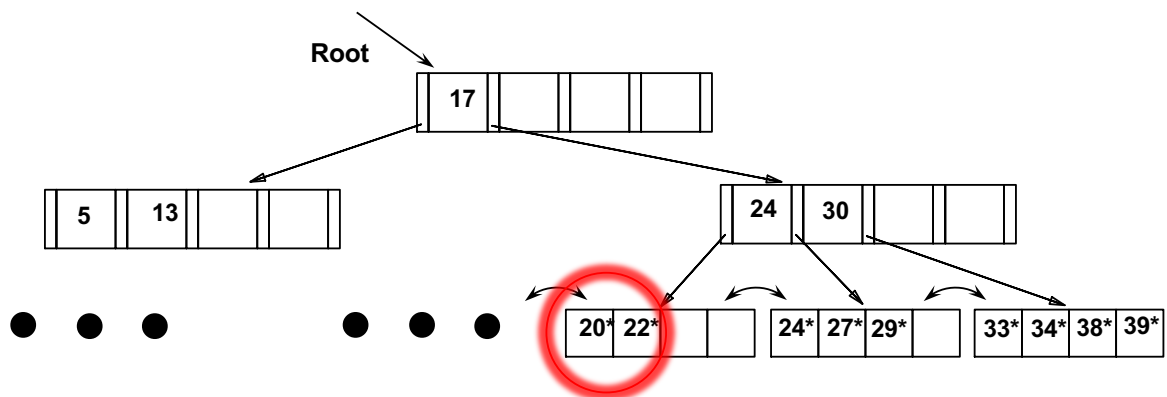
Deleting a Data Entry from a B+ Tree

- Start at root, find leaf L where entry belongs.
- Remove the entry.
 - If L is at least half-full, *done!*
 - If L has only $d-1$ entries,
 - Try to *re-distribute*, borrowing from *sibling* (adjacent node with same parent as L).
 - If re-distribution fails, *merge* L and sibling.
- If merge occurred, must delete entry (pointing to L or sibling) from parent of L .
- Merge could propagate to root, decreasing height.

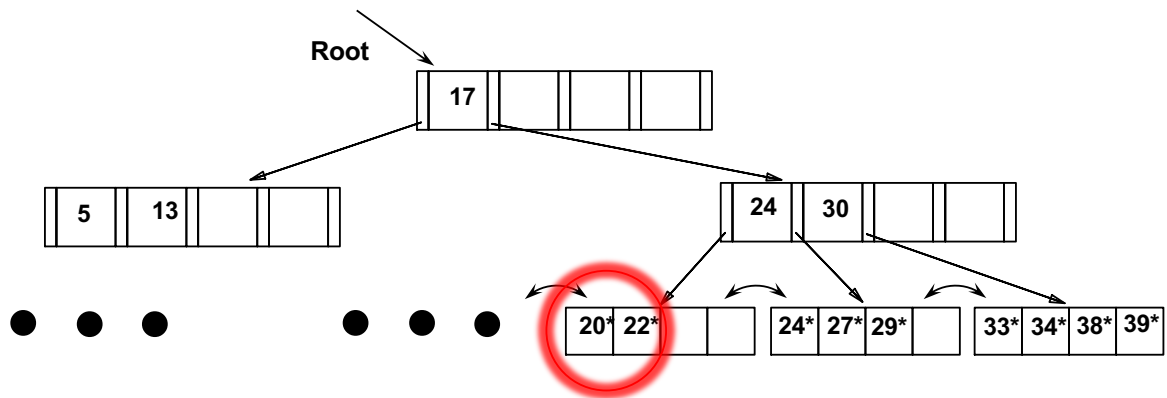
Example Tree - Delete 19*



Example Tree - Delete 19*

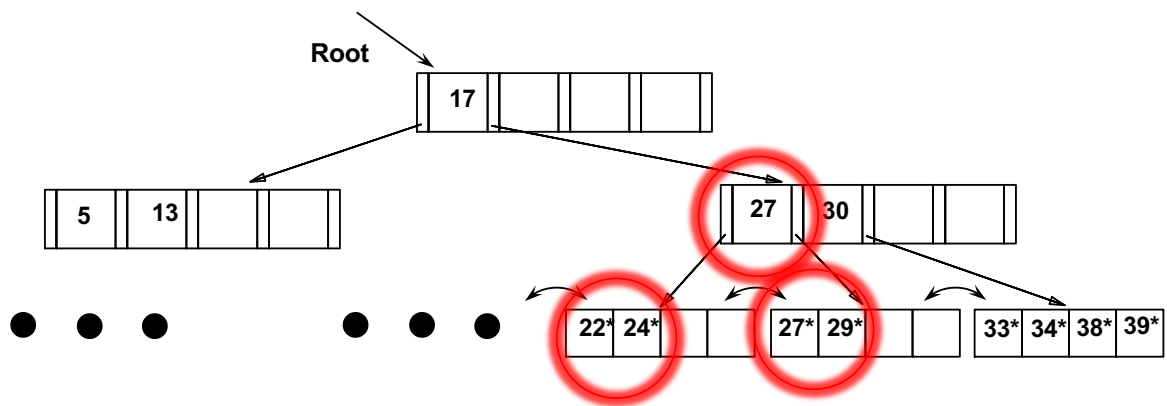


Example Tree – Now, Delete 20*

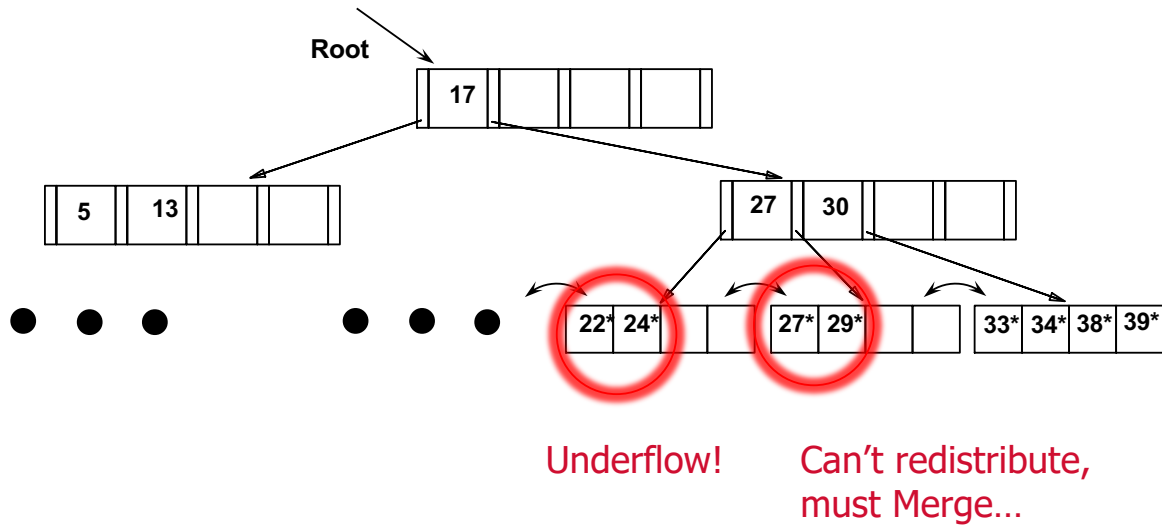


Redistribute

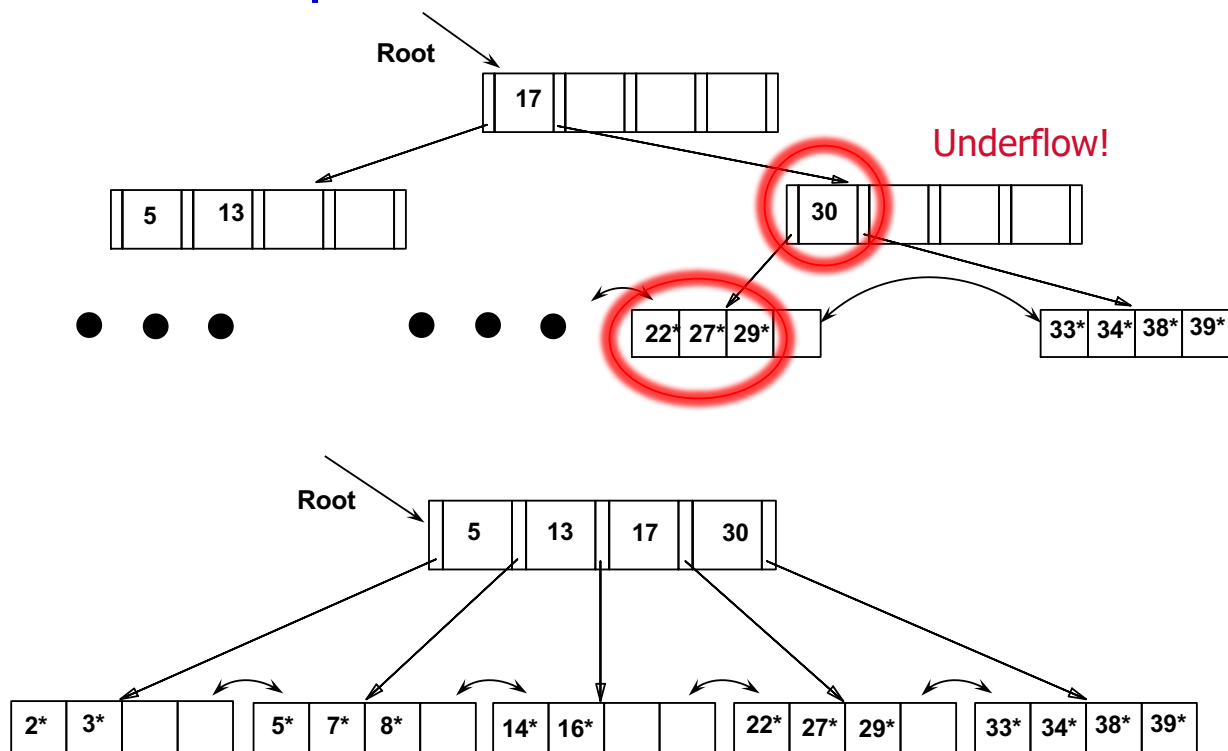
Example Tree – Then Delete 20*



Example Tree – Then Delete 24*

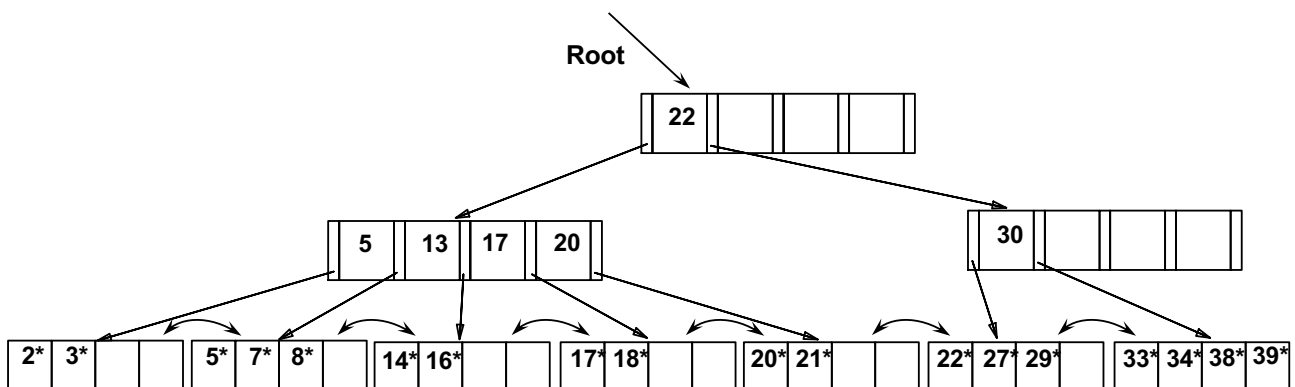


Example Tree – Then Delete 24*



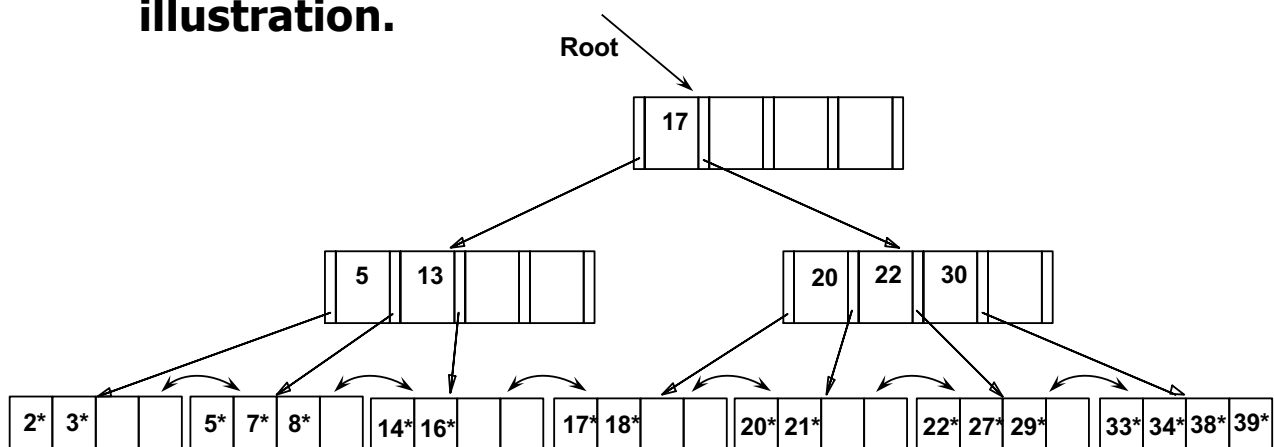
Example of Non-leaf Re-distribution

- Tree is shown below *during deletion* of 24*
- In contrast to previous example, can re-distribute entry from left child of root to right child.



After Re-distribution

- Intuitively, entries are **re-distributed by 'pushing through'** the splitting entry in the parent node.
- It suffices to re-distribute index entry with key 20; we've re-distributed 17 as well for illustration.



A Note on `Order`

- ***Order*** (d) concept replaced by physical space criterion in practice (*`at least half-full`*).
 - Index pages can typically hold many more entries than leaf pages.
 - Variable sized records and search keys mean different nodes will contain different numbers of entries.
 - Even with fixed length fields, multiple records with the same search key value (*duplicates*) can lead to variable-sized data entries (if we use Alternative (3)).
- **Many real systems are even sloppier than this - -- only reclaim space when a page is *completely* empty.**

Introduction to Hash-based Indexes

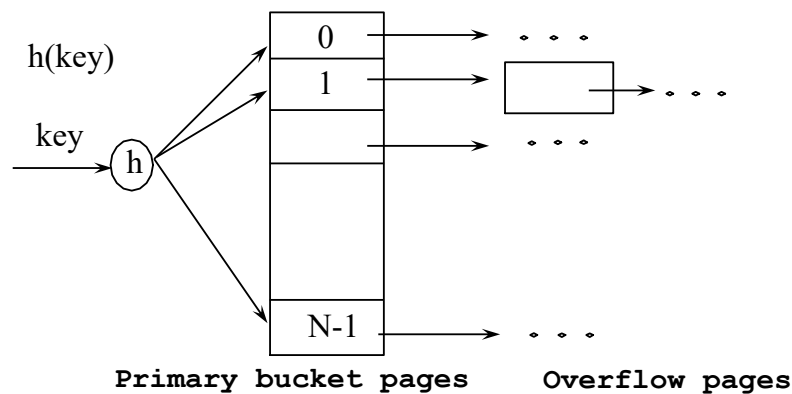
- **Hash-based indexes are best for *equality selections*. Cannot support range searches.**
- **Static and dynamic hashing techniques exist; trade-offs similar to ISAM vs. B+ trees.**

Static Hashing

- **# primary pages fixed, allocated sequentially, never de-allocated; overflow pages if needed.**
- A simple hash function (for N buckets):

$$h(k) = k \text{ MOD } N$$

is bucket # where data entry with key k belongs.



Static Hashing (Contd.)

- Buckets contain *data entries*.
- Hash fn works on *search key* field of record r . Use MOD N to distribute values over range $0 \dots N-1$.
 - $h(\text{key}) = \text{key} \text{ MOD } N$ works well for uniformly distributed data.
 - $h(\text{key}) = (a * \text{key} + b)$.
 - a and b are constants; lots known about how to tune h .
 - various ways to tune h for non-uniform (checksums, crypto, etc.).
- Buckets contain *data entries*.
- As with any static structure: **Long overflow chains** can develop and degrade performance.
 - *Extendible* and *Linear Hashing*: Dynamic techniques to fix this problem.

Extendible Hashing

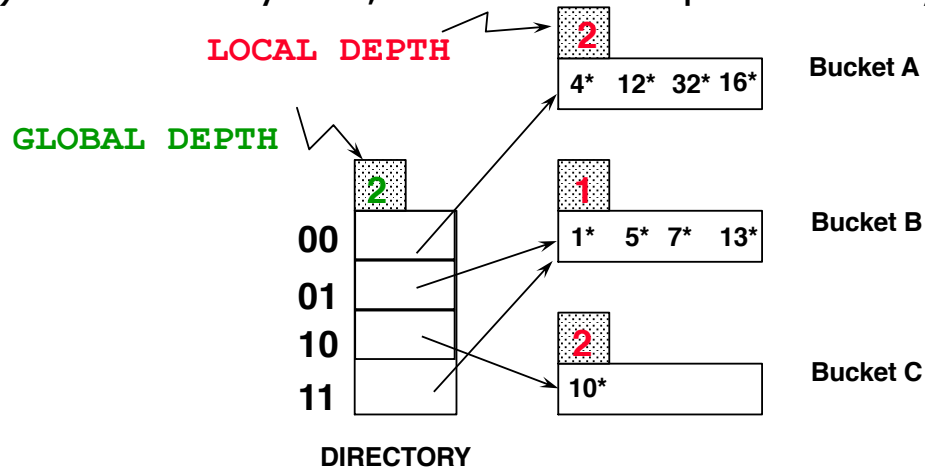
- **Situation: Bucket (primary page) becomes full.**
 - Want to avoid overflow pages
- **How about we add more buckets (i.e., increase "N")?**
 - Okay, but need a new hash function!
- ***Doubling* # of buckets makes this easier**
 - Say N values are powers of 2 – how to do "mod N"?
 - What happens to hash function when you double "N"?
- **Problems with Doubling**
 - Don't want to have to double the size of the file.
 - Don't want to have to move all the data.

Extendible Hashing (continued)

- **Idea: Add a level of indirection!**
- Use ***directory of pointers to buckets***,
- **Double # of buckets by *doubling the directory***
 - Directory much smaller than file, so doubling it is much cheaper.
- **Split only the bucket that just overflowed!**
 - ***No overflow pages!***
 - Trick lies in how hash function is adjusted!

Extendible Hashing – How it Works

- Directory is array of size 4, so 2 bits needed.
- Bucket for record r has entry with index = '*global depth*' least significant bits of $h(r)$;
 - If $h(r) = 5 = \text{binary } 101$, it is in bucket pointed to by 01.
 - If $h(r) = 7 = \text{binary } 111$, it is in bucket pointed to by 11.

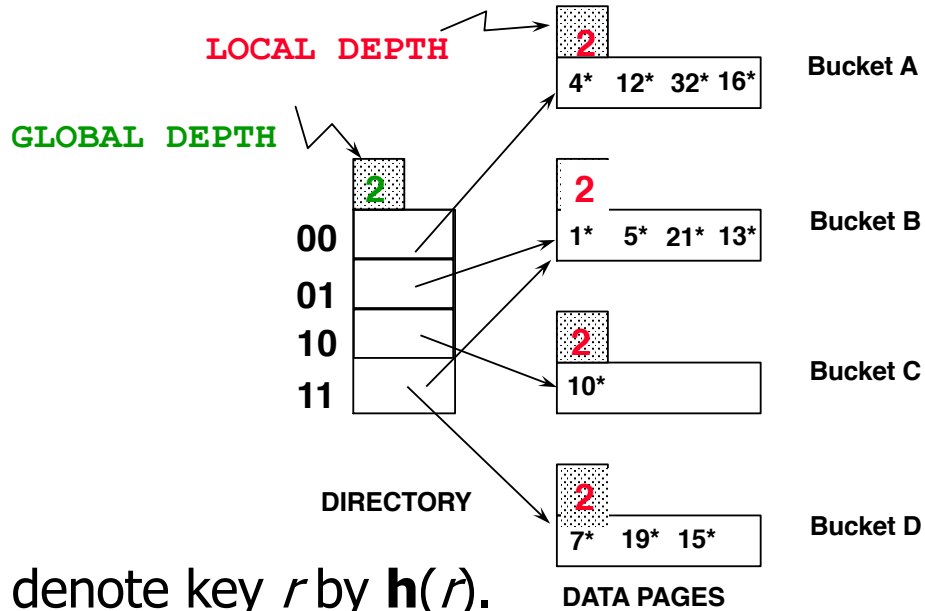


Handling Inserts

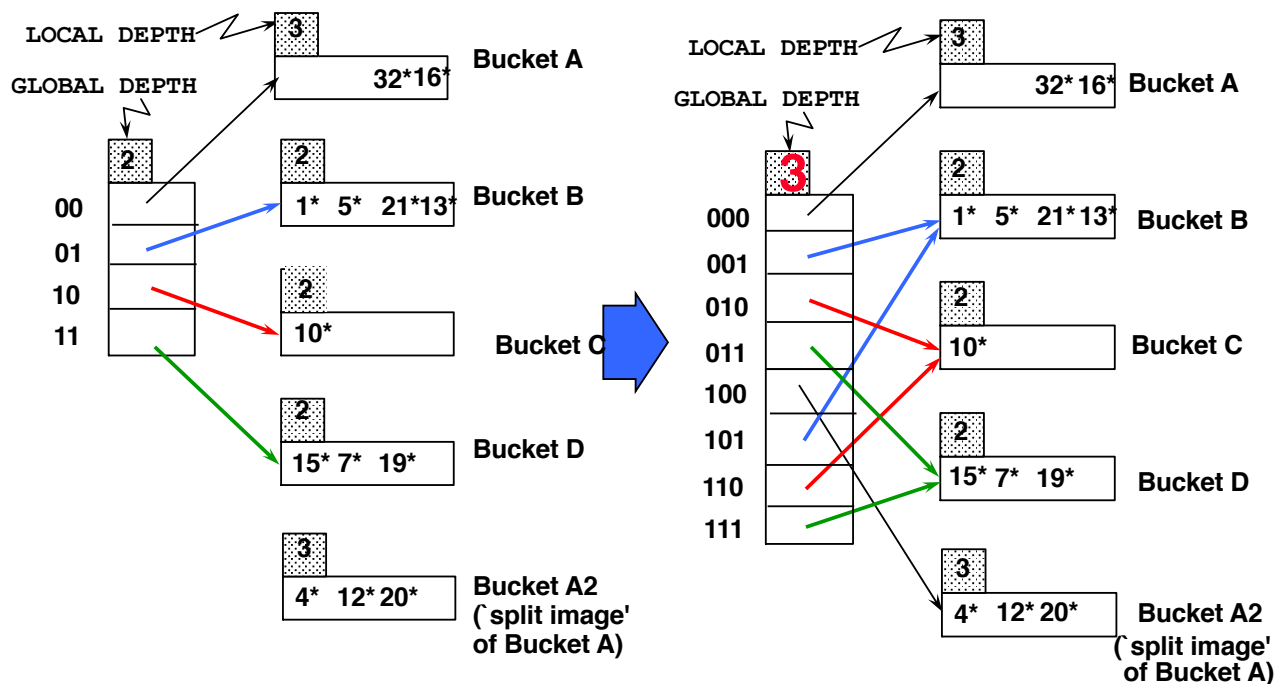
- Find bucket where record belongs.
- If there's room, put it there.
- Else, if bucket is full, *split* it:
 - increment **local depth** of original page
 - allocate new page with new **local depth**
 - re-distribute records from original page.
 - add entry for the new page to the directory

Example: Insert 21, then 19, 15

- **21 = 10101**
- **19 = 10011**
- **15 = 01111**



Insert $\mathbf{h}(r)=20$ (Causes Doubling)

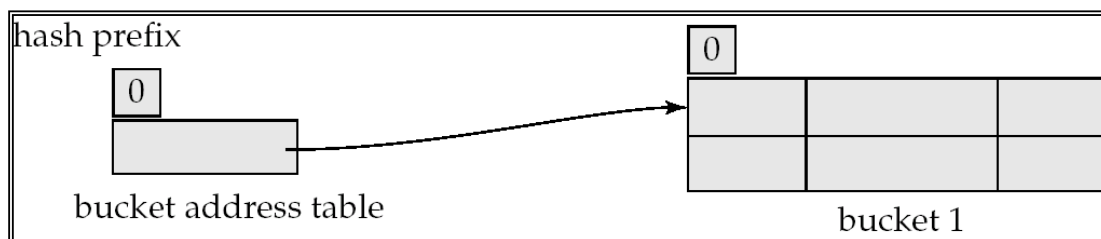


Points to Note

- **20 = binary 10100. Last 2 bits (00) tell us r belongs in either A or A2. Last 3 bits needed to tell which.**
 - *Global depth of directory*: Max # of bits needed to tell which bucket an entry belongs to.
 - *Local depth of a bucket*: # of bits used to determine if an entry belongs to this bucket.
- **When does bucket split cause directory doubling?**
 - Before insert, *local depth* of bucket = *global depth*. Insert causes *local depth* to become > *global depth*; directory is doubled by *copying it over* and 'fixing' pointer to split image page.

Use of Extendible Hash Structure: Example

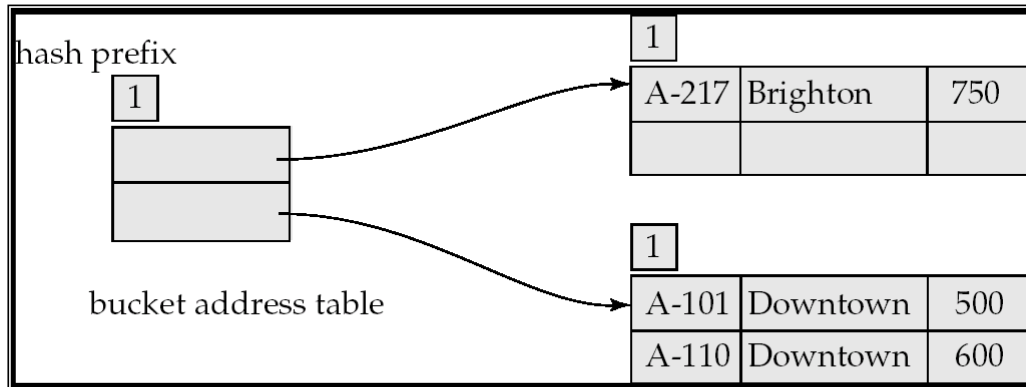
<i>branch_name</i>	<i>h(branch_name)</i>
Brighton	0010 1101 1111 1011 0010 1100 0011 0000
Downtown	1010 0011 1010 0000 1100 0110 1001 1111
Mianus	1100 0111 1110 1101 1011 1111 0011 1010
Perryridge	1111 0001 0010 0100 1001 0011 0110 1101
Redwood	0011 0101 1010 0110 1100 1001 1110 1011
Round Hill	1101 1000 0011 1111 1001 1100 0000 0001



Initial Hash structure, bucket size = 2

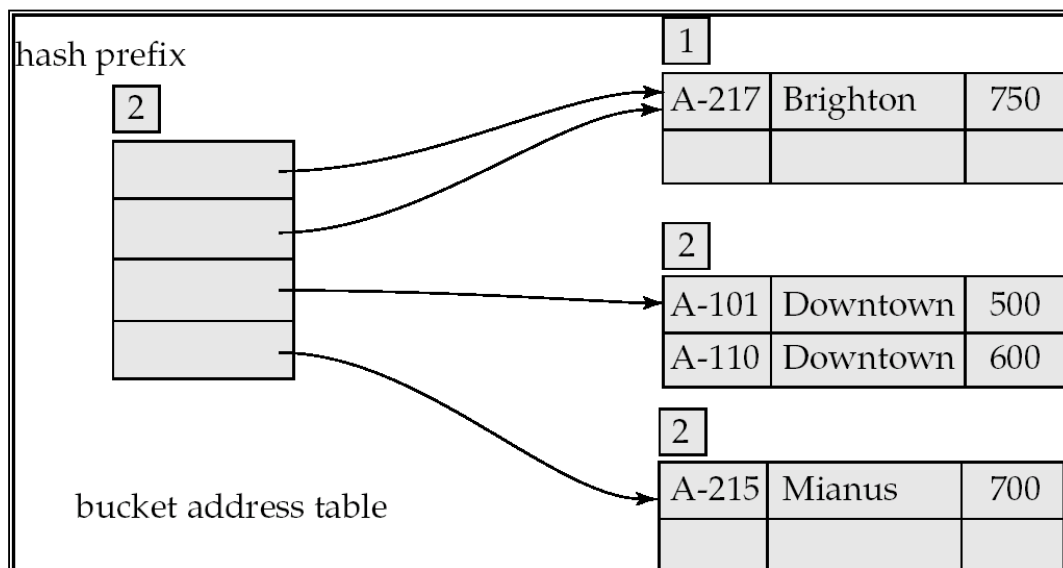
Example (Cont.)

- **Hash structure after insertion of one Brighton and two Downtown records**

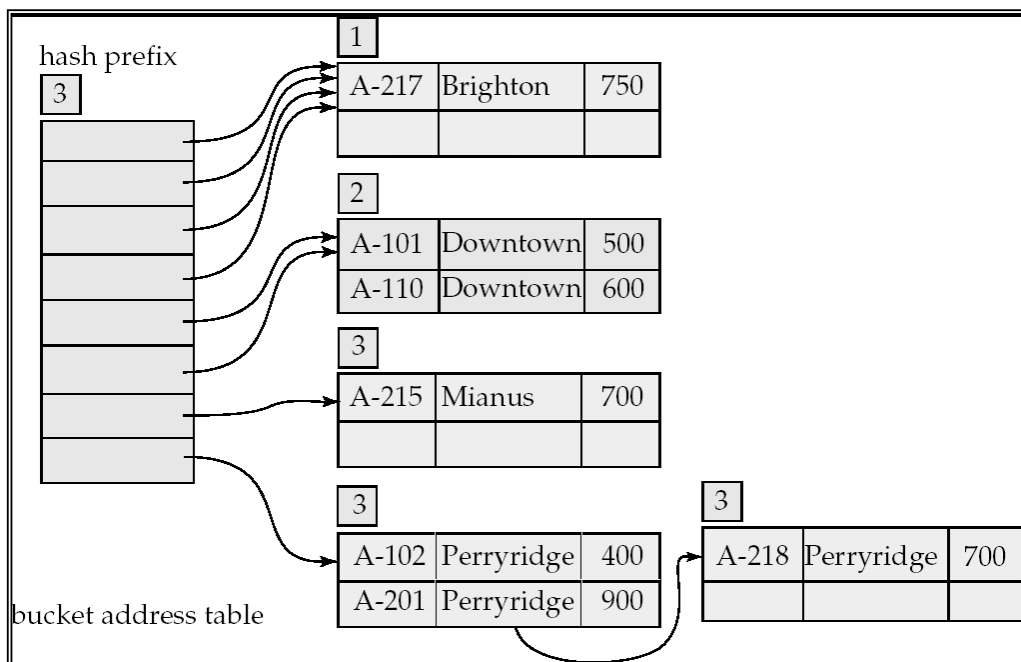


Example (Cont.)

Hash structure after insertion of Mianus record



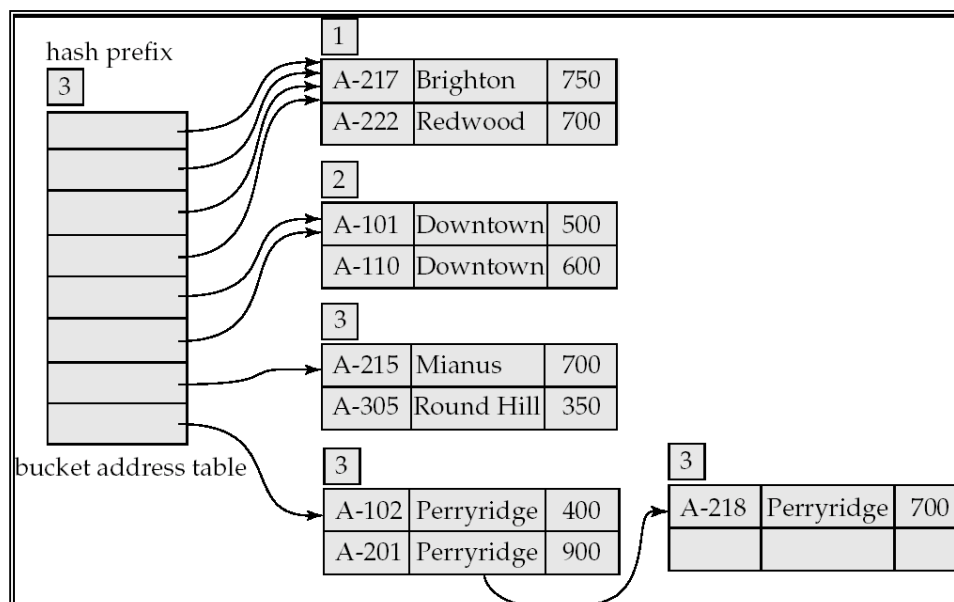
Example (Cont.)



Hash structure after insertion of three Perryridge records

Example (Cont.)

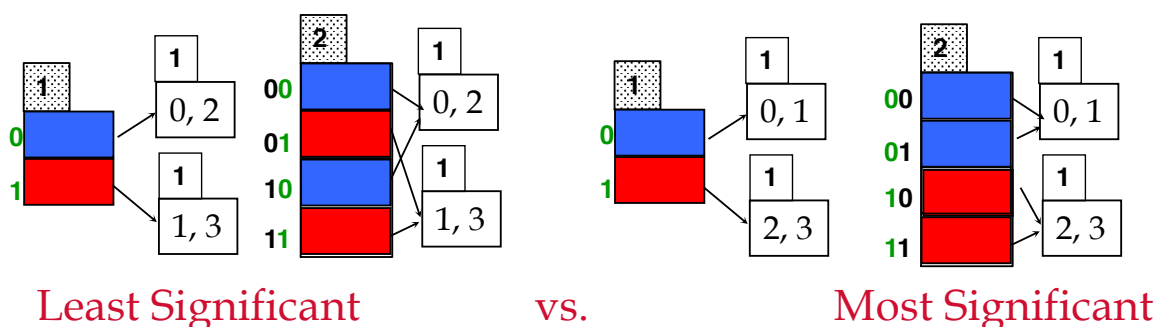
- **Hash structure after insertion of Redwood and Round Hill records**



Directory Doubling

Why use least significant bits in directory (instead of the *most* significant ones)?

Allows for doubling by copying the directory and appending the new copy to the original.



Q: Any other reasons?

Comments on Extendible Hashing

- **If directory fits in memory, equality search answered with one disk access; else two.**
 - 100MB file, 100 bytes/rec, 4K pages contains 1,000,000 records (as data entries) and 25,000 directory elements; chances are high that directory will fit in memory.
 - Directory grows in spurts, and, if the distribution of *hash values* is skewed, directory can grow large.
 - Multiple entries with same hash value cause problems!
- **Delete:** If removal of data entry makes bucket empty, can be merged with 'split image'. If each directory element points to same bucket as its split image, can halve directory.

Summary

- **Tree-structured indexes are ideal for range-searches, also good for equality searches.**
- **ISAM is a static structure.**
 - Only leaf pages modified; overflow pages needed.
 - Overflow chains can degrade performance unless size of data set and data distribution stay constant.
- **B+ tree is a dynamic structure.**
 - Inserts/deletes leave tree height-balanced; $\log_F N$ cost.
 - High fanout (**F**) means depth rarely more than 3 or 4.
 - Almost always better than maintaining a sorted file.

Summary (Contd.)

- Typically, 67% occupancy on average.
- Usually preferable to ISAM, modulo *locking* considerations; adjusts to growth gracefully.
- If data entries are data records, splits can change rids!
- **Other topics:**
 - Key compression increases fanout, reduces height.
 - Bulk loading can be much faster than repeated inserts for creating a B+ tree on a large data set.
- **Most widely used index in database management systems because of its versatility. One of the most optimized components of a DBMS.**

Summary – Hash Indexes

- **Hash-based indexes: best for equality searches, cannot support range searches.**
- **Static Hashing can lead to long overflow chains.**
- **Extendible Hashing avoids overflow pages by splitting a full bucket when a new data entry is to be added to it. (*Duplicates may require overflow pages.*)**
 - Directory to keep track of buckets, doubles periodically.
 - Can get large with skewed data; additional I/O if this does not fit in main memory.
- **“Linear hashing” solves some problems of Extendible hashing – not covered in this course, but check out book section 11.3 – it’s very cool!**

Summary

- **Index Definition in SQL**
- **Create an index**
 - `create index <index-name> on <relation-name> (<attribute-list>)`
 - E.g.: `create index b-index on branch (branch_name)`
- **Use create unique index to indirectly specify and enforce the condition that the search key is a candidate key is a candidate key.**
 - Not really required if SQL unique integrity constraint is supported
- **To drop an index**
 - `drop index <index-name>`
- **Most database systems allow specification of type of index, and clustering.**