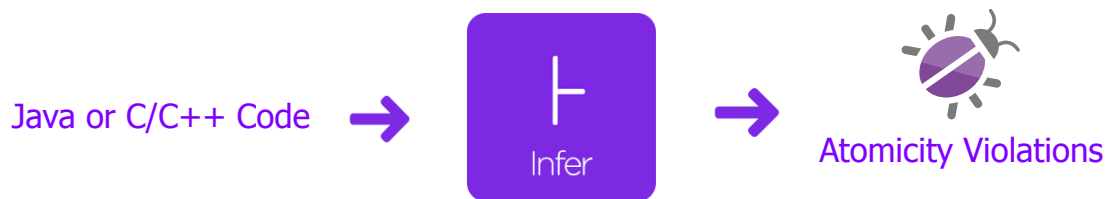


# Advanced Static Analysis of Atomicity in Concurrent Programs through Facebook Infer

Dominik Harmim\*



## Abstract

This work aims to improve and extend *Atomer*. A further goal is to perform new experiments with it. *Atomer* is a *static analyser* that detects *atomicity violations* created within the bachelor's thesis of the author as a module of *Facebook Infer* — an open-source static analysis framework that promotes efficient analysis. The original analysis assumes that sequences of function calls executed *atomically once* should probably be executed *always atomically*, and it naturally works with sequences. In this work, to improve *scalability*, the use of sequences was approximated by sets. Further, several new features were implemented, notably: support for *C++ and Java languages*; more advanced and precise manipulation with locks; and the analysis's parametrization. The new extensions were verified and evaluated on programs created for testing purposes. Furthermore, new experiments on extensive real-life programs were made, and already fixed and reported real bugs were rediscovered. The experiments revealed a significant increase of precision of the new version of *Atomer*.

**Keywords:** Facebook Infer — Static Analysis — Abstract Interpretation — Atomicity Violation — Contracts for Concurrency — Concurrent Programs — Program Analysis — Atomicity — *Atomer* — Incremental Analysis — Modular Analysis — Compositional Analysis — Interprocedural Analysis

**Supplementary Material:** [Atomer Repository](#) — [Atomer Wiki](#) — [Facebook Infer Repository](#)

\*[xharmi00@stud.fit.vutbr.cz](mailto:xharmi00@stud.fit.vutbr.cz), Faculty of Information Technology, Brno University of Technology

## 1. Introduction

Bugs are an integral part of computer programs ever since the inception of the programming discipline. Unfortunately, they are often hidden in unexpected places, and they can lead to unexpected behaviour, which may cause significant damage. Nowadays, developers have many possibilities of catching bugs in the early development process. *Dynamic analysers* or tools for *automated testing* are often used, and they are satisfactory in many cases. Nevertheless, they can still leave too many bugs undetected because they can analyse only *particular program flows* dependent on the

input data. An alternative solution is *static analysis* that has its shortcomings as well, such as the *scalability* on large codebases or a considerably high rate of incorrectly reported errors (so-called *false positives* or *false alarms*). Several efficient tools for static analysis were implemented, e.g., Coverity or CodeSonar. However, they are often proprietary and difficult to openly evaluate and extend.

Recently, Facebook introduced *Facebook Infer*: an open-source tool for creating highly scalable, compositional, incremental, and interprocedural static analysers. Facebook Infer has grown considerably, but

it is still under active development by many teams across the globe. It is employed every day not only in Facebook itself, but also in other companies, such as Spotify, Uber, Mozilla, or Amazon. Currently, Facebook Infer provides several analysers that check for various types of bugs, such as buffer overflows, data races and some forms of deadlocks and starvation, null-dereferencing, or memory leaks. However, most importantly, Facebook Infer is a *framework* for building new analysers quickly and easily. Unfortunately, the current version of Facebook Infer still lacks better support for *concurrency bugs*. While it provides an *reasonably advanced data race analyser*, it is limited to Java and C++ programs only and fails for C programs, which use a *lower-level lock manipulation*.

In *concurrent programs*, there are often *atomicity requirements* for the execution of specific sequences of instructions. Violating these requirements may cause many kinds of problems, such as unexpected behaviour, exceptions, segmentation faults, or other failures. *Atomicity violations* are usually not verified by compilers, unlike syntactic or some sorts of semantic rules. Moreover, atomicity requirements, in most cases, are not even documented at all. Therefore, in the end, programmers themselves must abide by these requirements and usually lack any tool support. Furthermore, in general, it is difficult to avoid errors in *atomicity-dependent programs*, especially in large projects, and even more laborious and time-consuming is finding and fixing them.

Within the author's bachelor's thesis [1], *Atomer*<sup>1</sup> was proposed — a *static analyser* for finding some forms of *atomicity violations* implemented as a Facebook Infer's module. In particular, the stress is put on the *atomic execution of sequences of function calls*, which is often required, e.g., when using specific library calls. It is based on the assumption that sequences of function calls executed *atomically once* should probably be executed *always atomically*, and it naturally works with sequences. In fact, the idea of checking the atomicity of certain sequences of function calls is inspired by the work of *contracts for concurrency* [2]. In the terminology of [2], the atomicity of specific sequences of calls is the most straightforward (yet very useful in practice) kind of contracts for concurrency. The implementation of the first version of *Atomer* *mainly targets C programs that use POSIX thread, i.e., PThread locks*.

<sup>1</sup>The implementation of *Atomer* is available on GitHub as an *open-source* repository. The link can be found among the supplementary materials of this paper.

Within this work, *Atomer* was improved and extended. Further, *other* experiments were performed. In particular, to improve *scalability*, working with sequences of function calls was *approximated* by working with *sets of function calls*. Furthermore, several new features were implemented, notably: support for *C++ and Java languages*, *more advanced and precise manipulation with locks*, and the analysis's *parameterisation*.

The development of *Atomer* and its extensions have been discussed with the developers of Facebook Infer, and it was supported under the H2020 ECSEL project Aquas. Currently, it is a part of the H2020 ECSEL project Arrowhead Tools. Parts of the paper are taken from the thesis [1].

The rest of the article is organised as follows. In Section 2, there is introduced the *Facebook Infer* framework. *Atomer* is described in Section 3. This is followed by Section 4, which considers all the extensions and improvements proposed within this work. The implementation of these extensions, together with the experimental evaluation of the new *Atomer*'s features and other experiments performed within this work, are discussed in Section 5. Finally, the paper is concluded in Section 6.

## 2. Facebook Infer

This section describes the principles and features of *Facebook Infer*. The description is based on information provided at the Facebook Infer's website<sup>2</sup> and in [3]. Parts of this section are taken from [1].

Facebook Infer is an *open-source*<sup>3</sup> *static analysis framework*<sup>4</sup>, which can discover various kinds of software bugs of a given program, emphasising *scalability*. A more detailed explanation of Facebook Infer architecture is given in Section 2.2. Facebook Infer is implemented in *OCaml*<sup>5</sup> — a *functional programming language*, also supporting *imperative* and *object-oriented* paradigms. Facebook Infer was originally a *standalone* tool focused on *sound verification* of the absence of *memory safety violations*, which was first published in the well-known paper [7].

Facebook Infer can analyse programs written in several languages. In particular, it supports the following languages: C, C++, Java, and Objective-C (and C#, see [8]). Moreover, it is possible to extend Facebook Infer's *frontend* for supporting other languages.

<sup>2</sup>Facebook Infer's website: <https://fbinfer.com>.

<sup>3</sup>A link to the Facebook Infer's open-source repository is in the supplementary materials of the paper.

<sup>4</sup>A brief explanation of *static analysis* itself can be found in [1] — Section 2.1. In more detail, it is then explained in [4, 5, 6].

<sup>5</sup>OCaml's website: <https://ocaml.org>.

Currently, Facebook Infer contains many analyses focusing on various kinds of bugs, e.g., *Inferbo* (buffer overruns); *RacerD* (data races) [9, 10]; and other analyses that check for buffer overflows, some forms of deadlocks and starvation, null-dereferencing, memory leaks, resource leaks, etc.

## 125 2.1 Abstract Interpretation in Facebook Infer

Facebook Infer is a general framework for static analysis of programs, and it is based on *abstract interpretation*<sup>6</sup>. Despite the original approach taken from [7], Facebook Infer aims to find bugs rather than *formal verification*. It can be used to develop new sorts of *compositional* and *incremental* analysers quickly (*traprocedural* or *interprocedural* [5]) based on the concept of function *summaries*. In general, a *summary* represents *preconditions* and *postconditions* of a function [13]. However, in practice, a summary is a custom data structure that may be used for storing any information resulting from the analysis of particular functions. Facebook Infer generally does not compute the summaries during the analysis along the *Control Flow Graph (CFG)* [14]) as it is done in classical analyses based on the concepts from [15, 16]. Instead, Facebook Infer performs the analysis of a program *function-by-function along the call tree*, starting from its leaves (demonstrated in Example 2.1) therefore, a function is analysed, and a summary is computed without knowledge of the call context. Then, the summary of a function is used at all of its call sites. Since the summaries do not differ for different contexts, the analysis becomes more scalable, but it can lead to a loss of accuracy.

151 In order to create a new intraprocedural analyser  
152 in Facebook Infer, it is needed to define the following  
153 (the listed items are described in more detail in [1]—  
154 Section 2.1.1):

1. The *abstract domain*  $\mathcal{Q}$ , i.e., a type of an *abstract state*.
2. The *ordering operator*  $\sqsubseteq$ , i.e., an ordering of abstract states.
3. The *join operator*  $\sqcup$ , i.e., the way of joining two abstract states.
4. The *widening operator*  $\nabla$ , i.e., the way how to enforce the termination of the computation.
5. The *Transfer functions*  $\tau$ , i.e., a transformer that takes an abstract state as an input and produces an abstract state as an output.

166 Further, to create an interprocedural analyser, it is  
167 required to define additionally:

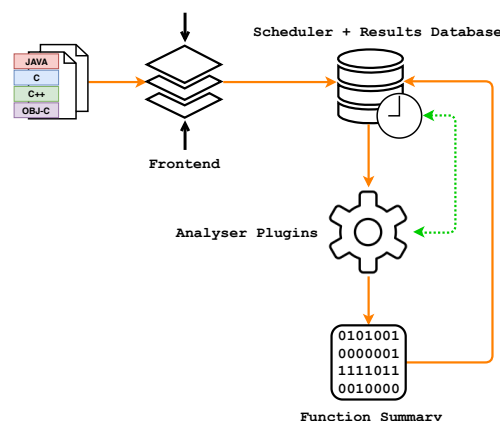
<sup>6</sup>~~Abstract interpretation is explained and formally defined in [11].~~ Section 2.1.1. Additional description can be found in [11, 12, 5, 6, 4].

1. A type of function summaries  $\chi$ . 168
2. The logic for using summaries in transfer functions and the logic for transforming an intraprocedural abstract state to a summary. 169  
170  
171

An important feature of Facebook Infer improving its scalability is the *incrementality* of the analysis. It allows one to analyse separate code changes only, instead of analysing the whole codebase. It is more suitable for extensive and variable projects where ordinary analysis is not feasible. The incrementality is based on *reusing summaries* of functions for which there is no change in them neither in the functions transitively invoked from them, as shown in Example 2.1.

## 2.2 Architecture of the Abstract Interpretation Framework in Facebook Infer 181

The architecture of the abstract interpretation framework of Facebook Infer (**Infer.AI**) may be split into three major parts, as demonstrated in Figure 1: a *frontend*, an *analysis scheduler* (and a *results database*), and a set of *analyser plugins*.



**Figure 1.** The architecture of Facebook Infer’s abstract interpretation framework [1]

The frontend compiles input programs into the *Smallfoot Intermediate Language* (SIL) and represents them as a CFG. There is a separate CFG representation for each analysed function. Nodes of this CFG are formed as SIL instructions (the individual instructions are outlined in [1]). The frontend allows one to propose *language-independent* analyses (to a certain extent) because it supports input programs to be written in multiple languages.

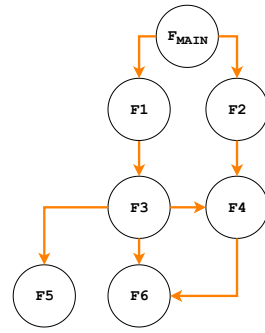
The next part of the architecture is the scheduler, which defines the order of the analysis of single functions according to the appropriate *call graph*<sup>7</sup>. The scheduler also checks if it is possible to simultaneously analyse some functions, allowing Facebook Infer to run the analysis in parallel.

<sup>7</sup>A **call graph** is a *directed graph* describing call dependencies among functions.

### 203 Example 2.1.

204 For demonstrating the order  
 205 of the analysis in Facebook  
 206 Infer and its incrementality,  
 207 assume a call graph given  
 208 in Figure 2. At first, leaf  
 209 functions F5 and F6 are ana-  
 210 lysed. Further, the analysis  
 211 goes on towards the root  
 212 of the call graph— $F_{MAIN}$ ,  
 213 while considering the de-  
 214 pendencies denoted by the  
 215 edges. This order ensures  
 216 that a summary is available  
 217 once a nested function call  
 218 is abstractly interpreted within the analysis. When  
 219 there is a subsequent code change, only directly  
 220 changed functions and all the functions up the call  
 221 path are re-analysed. For instance, if there is a change  
 222 of source code of function F4, Facebook Infer triggers  
 223 reanalysis of functions F4, F2, and  $F_{MAIN}$  only.

224 The last part of the architecture consists of a set  
 225 of analyser plugins. Each plugin performs some ana-  
 226 lysis by interpreting SIL instructions. The result of  
 227 the analysis of each function (function summary) is  
 228 stored in the results database. The interpretation of  
 229 SIL instructions (*commands*) is made using the *ab-*  
 230 *stract interpreter* (also called the *control interpreter*)  
 231 and *transfer functions* (also called the *command in-*  
 232 *terpreter*). The transfer functions take a previously  
 233 generated *abstract state* of an analysed function as  
 234 an input, and by applying the interpreting command,  
 235 produce a new abstract state. The abstract interpreter  
 236 interprets the command in an *abstract domain* accord-  
 237 ing to the CFG. This workflow is shown in a simplified  
 238 form in Figure 3.



**Figure 2.** A call graph for an illustration of Facebook Infer's analysis process [1]

### 3. Atomer: Atomicity Violations Detector 239

This section introduces the principles of the *static ana-*  
*lyser Atomer* proposed as a module of *Facebook Infer*  
 for finding some forms of *atomicity violations*. Atomer  
 was proposed and in detail described in the bachelor's  
 thesis of the author of this paper [1]. Therefore, natu-  
 rally, the following description is based on the men-  
 tioned thesis.

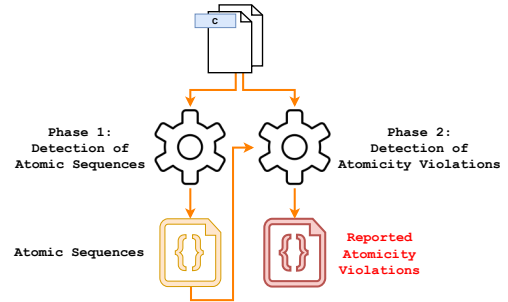
Atomer concentrates on checking the *atomicity of*  
*the execution of certain sequences of function calls*,  
 which is often required for *concurrent programs'* cor-  
 rect behaviour. Atomer's principle is based on the  
 assumption that sequences of function calls executed  
*atomically once* should probably be executed *always*  
*atomically*.

The proposal of Atomer is based on *basic con-*  
*tracts for concurrency* [1, 2]. These allow one to define  
*sequences of functions* required to be *executed atomic-*  
*ally*. Atomer can automatically derive candidates for  
 such contracts and then verify whether the contracts  
 are fulfilled. Both of these steps are done statically.  
 The proposed analysis is divided into two parts (*phases*  
*of the analysis*):

**Phase 1:** Detection of (likely) *atomic sequences*.

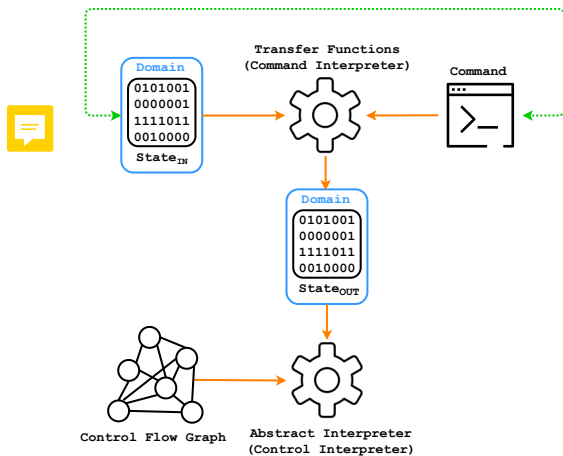
**Phase 2:** Detection of *atomicity violations* (violations  
 of the atomic sequences).

The phases are in depth described in the sections be-  
 low. Moreover, these phases of the analysis and its  
 workflow are illustrated in Figure 4.



**Figure 4.** Phases of the Atomer's analysis and the analysis high-level process illustration

This section describes the proposal of Atomer in  
 general. The concrete types of the *abstract states* (i.e.,  
 elements of the *abstract domain*  $\mathcal{Q}$ ) and the *summar-*  
*ies*  $\chi$ , along with the implementation of all necessary  
*abstract interpretation operators*, are stated in [1].  
 However, actually, the abstract states  $s \in \mathcal{Q}$  of both  
 phases of the analysis are proposed as *sets*. So, in fact,  
 the *ordering operator*  $\sqsubseteq$  is implemented using testing  
 for a *subset* (i.e.,  $s \sqsubseteq s' \Leftrightarrow s \subseteq s'$ , where  $s, s' \in \mathcal{Q}$ ), the  
*join operator*  $\sqcup$  is implemented as the *set union* (i.e.,  
 $s \sqcup s' \Leftrightarrow s \cup s'$ ), and the *widening operator*  $\nabla$  is imple-  
 mented using the join operator (i.e.,  $s \nabla s' \Leftrightarrow s \sqcup s'$ ).



**Figure 3.** Facebook Infer's abstract interpretation process [1]



### 280 3.1 Phase 1: Detection of Atomic Sequences

281 **Phase 1** of Atomer detects *sequences of functions* that  
282 should be *executed atomically*. Intuitively, the detec-  
283 tion is based on looking for sequences of functions  
284 executed atomically on some path through a program.

285 The detection of sequences of calls to be executed  
286 atomically is based on analysing all paths through the  
287 CFG of a function and generating all pairs  $(A, B) \in$   
288  $\Sigma^* \times \Sigma^*$  (where  $\Sigma^*$  is a set of all possible sequences  
289 of functions from  $\Sigma$  in a given program) of *reduced*  
290 *sequences* [1] of function calls for each path such that:  
291 Here,  $A$  is a reduced sequence of function calls that  
292 appear between the beginning of the function being  
293 analysed and the first lock; between an unlock and  
294 a subsequent lock; or between an unlock and the end of  
295 the function being analysed.  $B$  is a reduced sequence of  
296 function calls that follow the calls from  $A$  and that ap-  
297 pear between a lock and an unlock (or between a lock  
298 and the end of the function being analysed). Thus, the  
299 *abstract state*  $s \in \mathcal{Q}$  is defined as  $2^{\Sigma^* \times \Sigma^*}$  (because there  
300 is a set of the  $(A, B)$  pairs for each program path).

301 The *summary*  $\chi_f \in 2^{\Sigma^* \times \Sigma^*}$  of a function  $f$  is then  
302 defined as  $\chi_f = (B, AB)$ , where:

- 303 •  $B$  is a set constructed that contains all the  $B$  se-  
304 quences that appear on program paths through  $f$ .  
305 In other words, this component of the summary  
306 is a set of sequences of atomic function calls  
307 appearing in an analysed function.
- 308 •  $AB$  is a *concatenation* of all the  $A$  and  $B$  se-  
309 quences with removed duplicates of function  
310 calls. In particular, assume that there is the fol-  
311 lowing computed set of  $(A, B)$  pairs:  $\{(A_1, B_1),$   
312  $(A_2, B_2), \dots, (A_n, B_n)\}$ , then the result is concat-  
313 enated sequence  $A_1 \cdot B_1 \cdot A_2 \cdot B_2 \cdot \dots \cdot A_n \cdot B_n$  with  
314 removed duplicates. Intuitively, in this compon-  
315 ent of the summary, it is gathered occurrences of  
316 all called functions within an analysed function  
317 obtained by concatenation of all the  $A$  and  $B$   
318 sequences.  $AB$  is recorded to analyse functions  
319 higher in the *call hierarchy* since locks/unlocks  
320 can appear in such a *higher-level* function.

**Example 3.1.** For instance, the analysis of the func-  
tion  $f$  from Listing 1 produces the following sequences:

$$\overbrace{x, \cancel{x}, y}^A \quad \overbrace{[a, b, \cancel{b}]}^B$$

321 The strikethrough of the functions  $x$  and  $b$  denotes  
322 removing already recorded function calls in the  $A$   
323 and  $B$  sequences. For the above, the abstract state  
324 at the end of an interpretation of the function  $f$  is  
325  $s_f = \{\{((x, y), (a, b))\}\}$ . The derived summary  $\chi_f$  for  
326 the function  $f$  is  $\chi_f = (\{(a, b)\}, (x, y, a, b))$ .

```
1 void f() {
2     x(); x(); y();
3     lock(&L); // (a, b)
4     a(); b(); b();
5     unlock(&L);
6 }
```

**Listing 1.** A code snippet used for an illustration of  
the derivation of *sequences of functions called*  
*atomically*

The derived sequences of calls assumed to execute  
atomically — the  $B$  sequences — from the summaries  
of all analysed functions are stored into a file used  
during **Phase 2**, which is described below.

### 327 3.2 Phase 2: Detection of Atomicity Violations 331

328 In the second phase of the analysis, i.e., when *detect-*  
329 *ing violations* of the atomic sequences obtained from  
330 **Phase 1**, the analysis looks for *pairs of functions* that  
331 *should be called atomically* (or just for single func-  
332 tions if there is only one function call in an atomic  
333 sequence) while this is not the case on some path  
334 through the CFG. The pairs of function calls to be  
335 checked for atomicity are obtained as follows: For  
336 each function  $f$  with the *summary*  $\chi_f = (B, AB)$  in  
337 a given program, it is taken the first component  $B$   
338 of the summary  $\chi_f$ , i.e.,  $B = \{B_1, B_2, \dots, B_n\}$ , and it  
339 is taken *every pair*  $(x, y) \in \Sigma \times \Sigma$  of functions that ap-  
340 pear as a *substring* in some of the  $B_i$  sequences, i.e.,  
341  $B_i = w \cdot x \cdot y \cdot w'$  for some sequences  $w, w'$ . Note that  $x$   
342 could be  $\epsilon$  (an empty sequence) if some  $B_i$  consists of  
343 a single function. All these “atomic pairs” are put into  
344 the set  $\Omega \in 2^{\Sigma \times \Sigma}$ .

345 An element of this phase’s *abstract state* is a triple  
346  $(x, y, \Delta) \in \Sigma \times \Sigma \times 2^{\Sigma \times \Sigma}$ , where  $(x, y)$  is a pair of the  
347 most recent function calls, and  $\Delta$  is a *set of pairs that*  
348 *violate atomicity*. Thus, the abstract state  $s \in \mathcal{Q}$  is  
349 defined as  $2^{\Sigma \times \Sigma \times 2^{\Sigma \times \Sigma}}$ . Whenever a function  $f$  is called,  
350 it is created a new pair  $(x', y')$  of the most recent func-  
351 tion calls from the previous pair  $(x, y)$  (i.e.,  $(x', y') =$   
352  $(y, f)$ ). Further, when the current program state is not  
353 inside an *atomic block*, it is checked whether the new  
354 pair (or just the last call) violates the atomicity (i.e.,  
355  $(x', y') \in \Omega \vee (\epsilon, y') \in \Omega$ ). When it does, it is added to  
356 the set  $\Delta$  of pairs that violate atomicity.

**Example 3.2.** To demonstrate the detection of an  
atomicity violation, assume the functions  $f$  and  $g$   
from Listing 2. The set of atomic sequences of  
the function  $f$  with the summary  $\chi_f = (B, AB)$  is  
 $B = \{(a, b, c)\}$ , thus  $\Omega = \{(a, b), (b, c)\}$ . In the func-

tion g, an atomicity violation is detected because the pair of functions b and c is not called atomically.

```

1 void f() {
2     lock(&L); // (a, b, c)
3     a(); b(); c();
4     unlock(&L);
5 }
6 void g() {
7     // ATOMICITY_VIOLATION: (b, c)
8     x(); b(); c(); y();
9 }

```

**Listing 2.** Example of an *atomicity violation*

The sets of atomicity violations  $\Delta$  from individual functions are the final reported atomicity violations seen by a user.

## 4. Proposal of Enhancements for Atomer

## 5. Implementation and Experiments

## 6. Conclusions

## Acknowledgements

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