Summary of formulas and constants used in biochemistry

Constants

$$R = 0.008314 \ kJ \cdot mol^{-1} \cdot K^{-1}$$
$$T \ in \ K = T \ in \ ^{\circ}C + 273.15$$

Free energy

$$\Delta G = \Delta H - T\Delta S$$

Free energy and concentration:

$$aA + bB \rightleftharpoons cC + dD$$

$$\Delta G^{\circ\prime} = -RT \ln \left(K_{eq} \right) = -RT \ln \left(\frac{[C]_{eq}^{c}[D]_{eq}^{d}}{[A]_{eq}^{a}[B]_{eq}^{b}} \right)$$

$$\Delta G = \Delta G^{\circ\prime} + RT \ln \left(\frac{[C]^{c}[D]^{d}}{[A]^{a}[B]^{b}} \right)$$

The standard state condition is defined as all products and reactants at 1 M, 25C, 1 atm pressure, pH 7.0.

Binding

For the reaction:

$$M + X \rightleftharpoons M \cdot X$$

$$K_{eq} = K_{association} = K_a = \frac{[M \cdot X]}{[M][X]}$$

You can write this reaction as a dissociation reaction as well (generally preferred by biochemists)

$$M \cdot X \rightleftharpoons M + X$$

$$K_{eq} = K_{dissociation} = K_D = \frac{[M][X]}{[M \cdot X]}$$

Written this way, K_D has units of concentration and thus measures the concentration at which the reaction will be 50% bound and 50% unbound.

$$\theta = \frac{[MX]}{[M] + [MX]} = \frac{1}{1 + K_D/[X]}$$

pH:

$$M \cdot H \stackrel{K_a}{\rightleftharpoons} M + H^+$$

$$K_a = \frac{[M][H^+]}{[M \cdot H]}$$

$$pH = -log_{10} ([H^+]); \ pK_a = -log_{10} (K_a)$$

$$\theta = \frac{[M \cdot H]}{[M] + [M \cdot H]} = \frac{1}{1 + K_a/[H^+]} = \frac{1}{1 + 10^{(pH - pK_a)}}$$

Cooperative binding

For the cooperative binding reaction:

$$MX_n \rightleftharpoons [M] + n[X]$$

$$\theta_n = \frac{[MX_n]}{[M] + \sum_{i=1}^{i=n} [MX_i]}$$

$$\theta = \frac{1}{1 + \left(\frac{K_D}{[X]}\right)^n}$$

where n is the number of cooperating sites.