

11/11/19 : pKa VALUES AND ENERGETICS

EQUILIBRIUM CONSTANT DESCRIBES  $\Delta G^\circ$ : BINDING AT REFERENCE  
CONDITION OF 1 M EVERYTHING

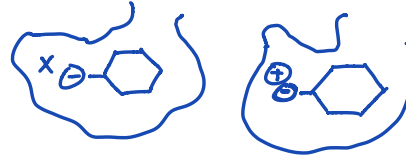
$$\Delta G = \Delta G^\circ + RT \ln \left( \frac{[M][X]}{[MX]} \right)$$

C  $K_D$ ,  $\Delta G = 0$ :

$$0 = \Delta G^\circ + RT \ln \left( \frac{[M][X]}{[MX]} \right)$$

$$-RT \ln \left( \frac{[M][X]}{[MX]} \right) = \Delta G^\circ$$

$$-RT \ln (K_D) = \Delta G^\circ$$



IMPROVED  $\Delta G$ , LOWER  $K_D$ .

LET'S RELATE ENERGETICS TO EQUILIBRIUM  
CONSTANTS

pKa AND pH ARE SPECIAL CASES OF EQUILIBRIUM CONSTANTS

$$pK_a = -\log_{10}(K_a)$$

$\swarrow$   $K_{ACID} \rightarrow K_D, \text{protein}$

$$10^{-pK_a} = K_a$$

$$-RT \ln (10^{-pK_a}) = \Delta G \rightarrow pK_a \cdot RT \cdot \ln(10) = \Delta G$$

A SHIFT IN pKa IS PROPORTIONAL TO A SHIFT IN ENERGY.

A STEP IN pH IS PROPORTIONAL TO CHEMICAL POTENTIAL.

$$\mu_i = RT \ln(C_i) \quad pH = -\log_{10}[H^+] \rightarrow \mu = RT \ln(10) pH$$

$\uparrow$   
ASSUMING IDEALITY

pKa VALUES MEASURE CHANGES IN ENVIRONMENT



$$pK_{a, \text{OBS}} = pK_{a, \text{MODEL}} + \frac{\Delta G_{\text{ENV}}}{RT \ln(10)}$$

$\nwarrow$  COULOMBS

pKa ASP IS 4.0:



YOU OBSERVE pKa IS PROTON OF 2.0.

IS THIS FAVORABLE COULOMB INTERACT OR UNFAVORABLE DEHYDRATION?

$$2 = 4 + \frac{\Delta G_{ENV}}{RT \ln(10)}$$

$$(-2)(RT \ln(10)) = \Delta G_{ENV}$$

$$\frac{-11.4 \text{ kJ}}{\text{mol}} = \Delta G_{ENV}$$