

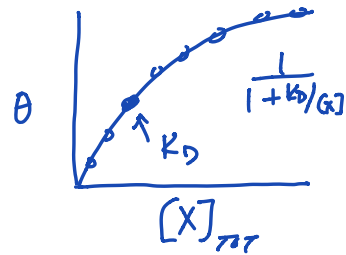
BINDING (11/6/19)

BINDING METHODS?



MEASURE $\theta = \frac{[MX]}{[M]_{TOT}}$

- SPECTROSCOPIC
- PULL DOWN
- ...



KNOW: $[M]_{TOT}$ $[X]_{TOT}$, NOT $[MX]$, $[X]$, OR $[M]$

$$K_D = \frac{[M][X]}{[MX]} = \frac{([M]_{TOT} - [MX])([X]_{TOT} - [MX])}{[MX]}$$

IF $M \ll K_D$, $X \approx X_{TOT}$. ($[MX]$ NEVER DEPLETES X UNDER BINDING CONDITIONS).

$$K_D = \frac{([M]_{TOT} - [MX]) X_{TOT}}{[MX]}$$

$$K_D [MX] = [M]_{TOT} X_{TOT} - [MX] \cdot X_{TOT}$$

$$K_D [MX] + X_{TOT} [MX] = [M]_{TOT} X_{TOT}$$

$$[MX] (K_D + X_{TOT}) = [M]_{TOT} X_{TOT}$$

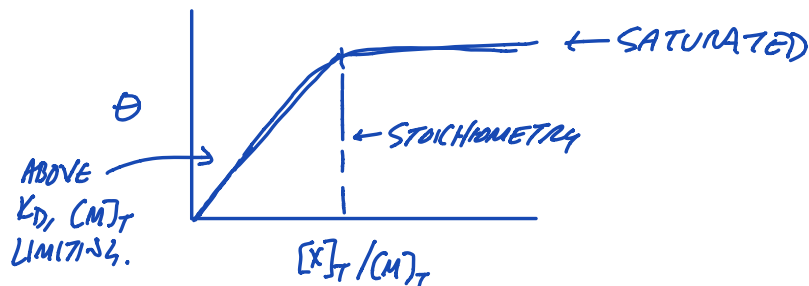
$$[MX] = \frac{[M]_{TOT} X_{TOT}}{K_D + X_{TOT}}$$

$$\theta = \frac{[MX]}{[M]_{TOT}} = \frac{[M]_{TOT} X_{TOT}}{[M]_{TOT} (K_D + X_{TOT})}$$

$$\theta = \frac{X_{TOT}}{K_D + X_{TOT}} = \frac{1}{K_D/X_{TOT} + 1} \leftarrow \text{FIT THIS MODEL TO DATA.}$$

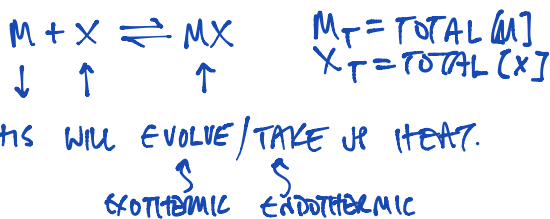
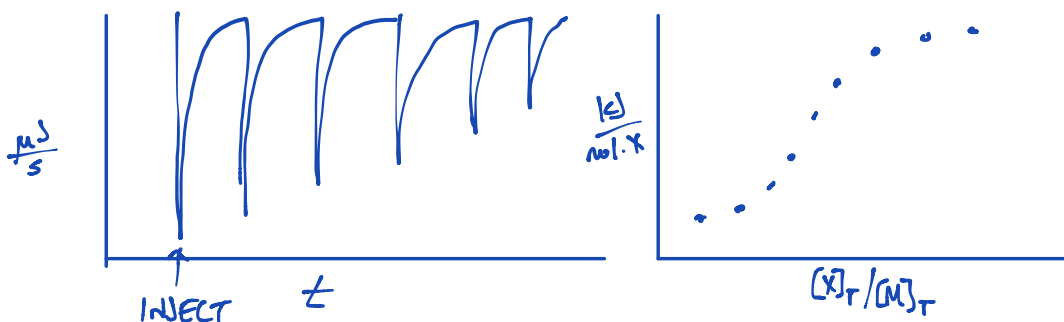
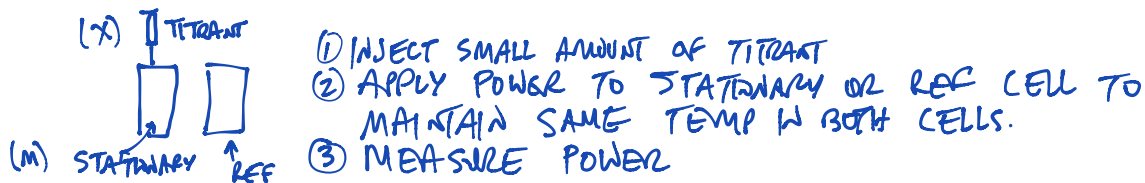
WHAT IF $[M]_{TOT} > K_D$?

- GET MORE COMPLEX FORM (SEE NOTES).
- ENTER STOICHIOMETRIC REGIME.



CAN WE LEARN ABOUT MORE THAN JUST ΔG ?

PROBE BY ISOTHERMAL TITRATION CALORIMETRY.



IF ENTHALPY CHANGE, THIS WILL EVOLVE/TAKE UP HEAT.

$$dH = \delta Q \quad (\text{NO } PdV \text{ WORK})$$

IF WE DUMP A TON OF TITRANT IN, GO TO ALL MX. $\int \delta Q \rightarrow \Delta H$.

WANT MORE INFORMATION.

ADD A LITTLE TITRANT:

$$\begin{array}{c}
 \frac{MX_i}{M_T} \rightarrow \frac{MX_{i+1}}{M_T} \quad (0 \rightarrow) \\
 \\
 q_{i+1} \propto \Delta H \left(\frac{MX_{i+1}}{M_T} - \frac{MX_i}{M_T} \right) \\
 \uparrow \quad \quad \quad \uparrow \\
 \text{ENTHALPY} \quad \quad \text{STEP ON RXN COORD} \\
 \text{FOR RXN}
 \end{array}$$

SO WHAT DETERMINES MX_i ? $[M]_T, [X]_T, K_i$

$$K_D = \frac{[M][X]}{[MX]}$$

$$K_D = \frac{(M_T - MX)(X_T - MX)}{MX}$$

$$K_D M_T = M_T X_T - M_T MX - X_T MX + MX^2$$

$$0 = M_T X_T - K_D MX - M_T MX - X_T MX + MX^2$$

$$0 = M_T X_T - (K_D + M_T + X_T) MX + MX^2$$

$$MX = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$MX = \frac{(K_D + M_T + X_T) - \sqrt{(K_D + M_T + X_T)^2 - 4[M]_T[X]_T}}{2}$$

IF WE KNOW K_D , WE CAN CALCULATE $[M]$. IF WE KNOW ΔH AND M_T , WE CAN CALCULATE q (WHAT WE OBSERVE). **GUESS AND CHECK**

FIT A MODEL WITH SINGLE K_D AND ΔH TO ALL OBSERVED HEATS VS. $[X]_T$.

IF YOU KNOW ΔH AND ΔG ($-RT \ln(K_D)$), YOU CAN FIND ΔS .

HOW CAN WE USE TO LEARN MECHANISM?

$$\Delta H(T) = \Delta H_{\text{ref}} + \Delta C_p (T - T_{\text{ref}}) \quad \text{DO ITC @ MULTIPLE TEMP. IF } \Delta C_p > 0, \text{ LARGE HYDROPHOBIC CONTRIBUTION.}$$