

## Assignment 2

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01.02.2011

STA4202

1.a. Stirring rate does not affect the grain size. The p-value for stirring rate is above 0.05 ( $p = 0.4995$ ), so we can not reject the null hypothesis that stirring rate does not affect grain size. The overall model for grain size is significantly different though ( $p=0.042$ ), indicating that another factor may be responsible for the difference.

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The GLM Procedure

Class Level Information

Class	Levels	Values
Stirring_Rate	4	5 10 15 20
Furnace	4	1 2 3 4

Number of Observations Read	16
Number of Observations Used	16

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The GLM Procedure

Dependent Variable: Grain\_Size

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	6	187.3750000	31.2291667	3.60	<b>0.0420</b>
Error	9	78.0625000	8.6736111		
Corrected Total	15	265.4375000			

R-Square	Coeff Var	Root MSE	Grain_Size Mean
0.705910	38.31024	2.945100	7.687500

Source	DF	Type III SS	Mean Square	F Value	Pr > F
<b>Stirring_Rate</b>	<b>3</b>	<b>22.1875000</b>	<b>7.3958333</b>	<b>0.85</b>	<b>0.4995</b>
Furnace	3	165.1875000	55.0625000	6.35	0.0133

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The GLM Procedure

Tukey's Studentized Range (HSD) Test for Grain\_Size

NOTE: This test controls the Type I experimentwise error rate, but it generally has a higher Type II error rate than REGWQ.

Alpha	0.05
Error Degrees of Freedom	9

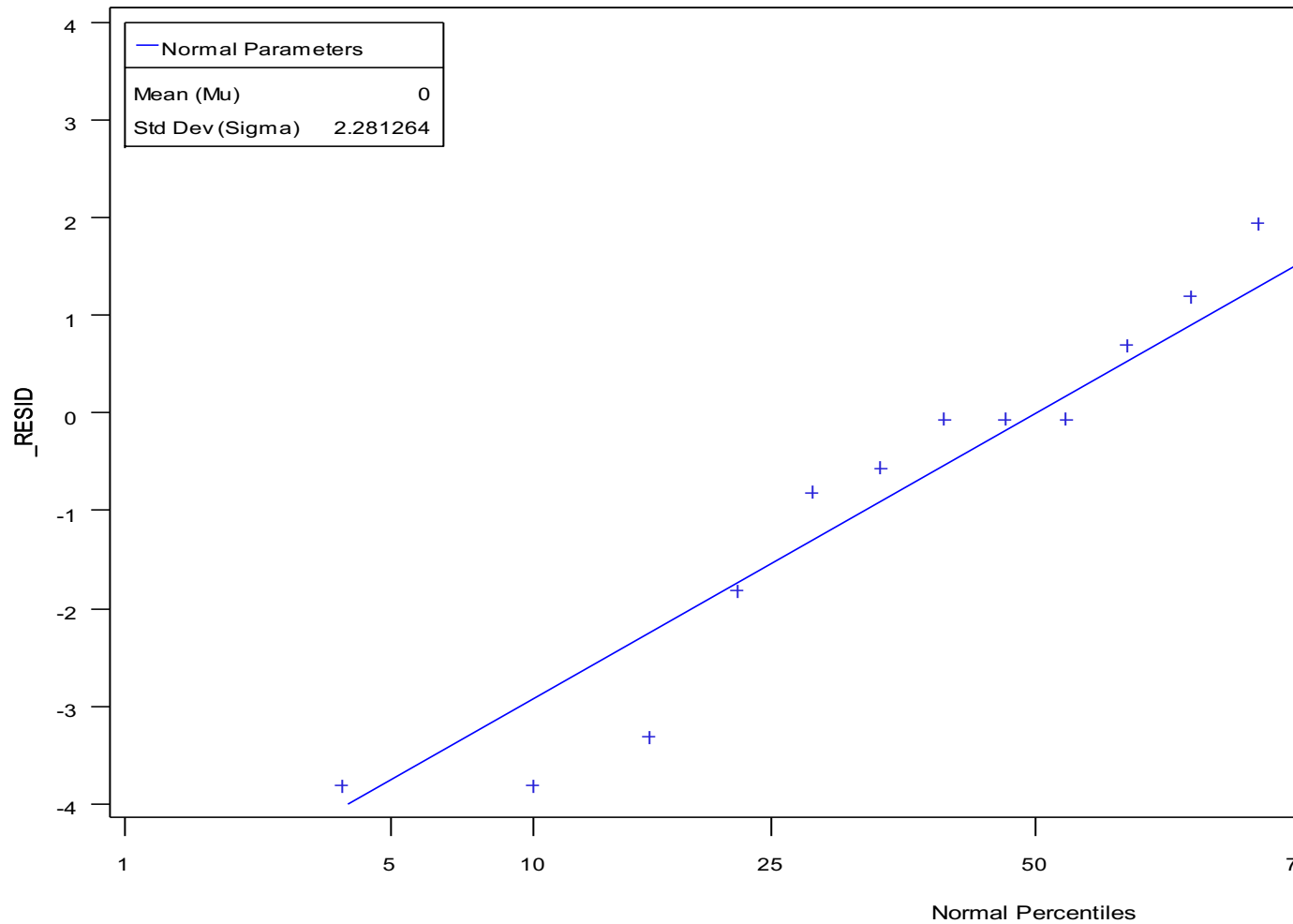
Error Mean Square	8.673611
Critical Value of Studentized Range	4.41489
Minimum Significant Difference	6.5011

Means with the same letter are not significantly different.

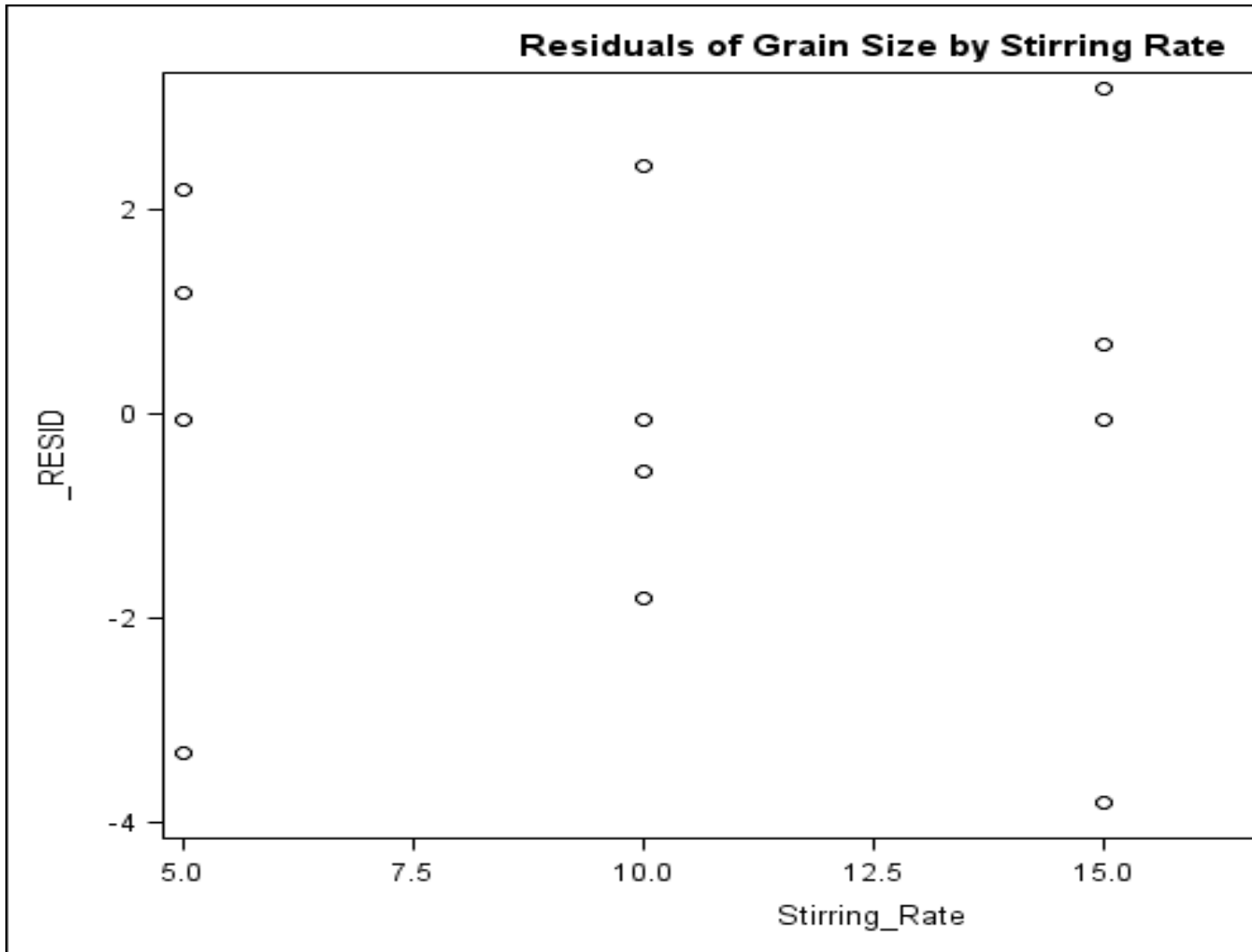
		<b>Stirring_</b>		
Tukey Grouping	Mean	N	Rate	
A	8.750	4	20	
A				
A	8.500	4	10	
A				
A	7.750	4	15	
A				
A	5.750	4	5	

1.b. The plot has a sine-wave pattern to it, indicating that there is systematic deviation from the model. It shows a non-linear pattern, and I would say that the model used is not a good fit.

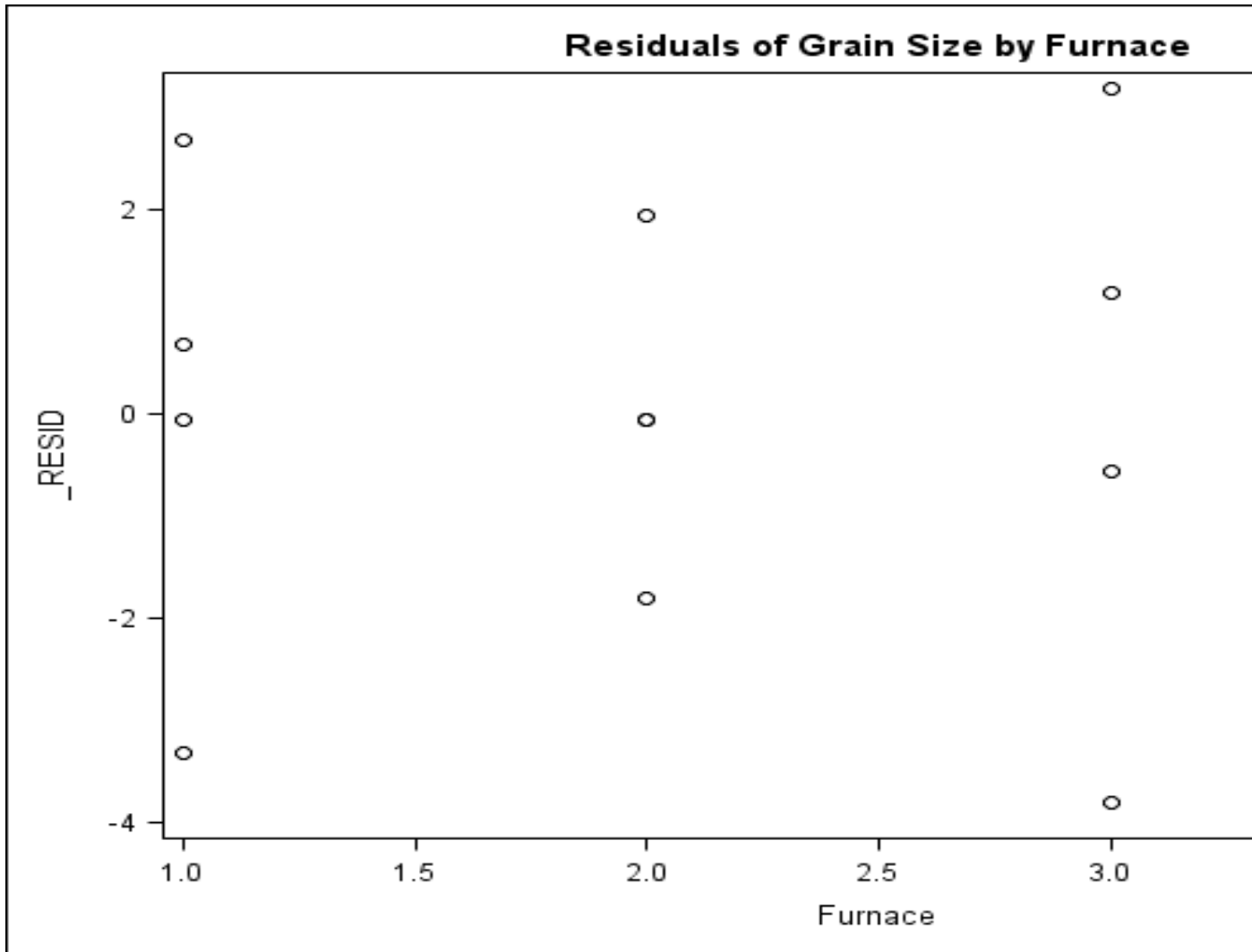
## Normal Probability Plot of Residuals



1.c. In this plot, the data looks distributed randomly, so we can assume independent error and constant variance assumptions among stirring rates.



In this plot, the data looks distributed randomly, so we can assume independent error and constant variance assumptions among furnaces.



1.d. Stirring rate is not that important (since the ANOVA proved it to be non-significant) in producing grain size, but a rate of 5 produces smaller (albeit non-significantly) grain size. They should avoid using furnace 1 because the mean grain size for that furnace (evidenced by performing a Tukey test on the block means) is significantly larger (13.25) than any other furnaces. In the end, they should use a stirring rate of 5 and either furnace 3 or 4.

The GLM Procedure

Tukey's Studentized Range (HSD) Test for Grain\_Size

NOTE: This test controls the Type I experimentwise error rate, but it generally has a higher Type II error rate than REGWQ.

Alpha	0.05
Error Degrees of Freedom	9
Error Mean Square	8.673611
Critical Value of Studentized Range	4.41489
Minimum Significant Difference	6.5011

Means with the same letter are not significantly different.

Tukey Grouping	Mean	N	Furnace
A	13.250	4	1
B	6.000	4	2
B			
B	5.750	4	3
B			
B	5.750	4	4

2. One can see that the blocking (day and batch) are not significant, but the type of catalyst used is significant ( $p = 0.0005$ ). We can conclude that the difference in reactions times in this sample is due to the catalyst. From the Tukey test, we can conclude that catalyst B is not different from any other catalysts, but catalysts C and A are significantly different from D and E. If the researcher wants to reduce reaction time, she should use catalysts D or E, but if she wishes to increase it, she should use C or A.

Class Level Information

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The GLM Procedure

Class Level Information

Class	Levels	Values
Batch	5	1 2 3 4 5
Day	5	1 2 3 4 5
Catalyst	5	A B C D E

Number of Observations Read 25

Number of Observations Used 25

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The GLM Procedure

Dependent Variable: Time Time

Source	Sum of		Mean Square	F Value	Pr > F
	DF	Squares			
Model	12	169.1200000	14.0933333	4.51	0.0072
Error	12	37.5200000	3.1266667		
Corrected Total	24	206.6400000			

R-Square	Coeff Var	Root MSE	Time Mean
0.818428	30.07208	1.768238	5.880000

Source	DF	Type III SS	Mean Square	F Value	Pr > F
Batch	4	15.4400000	3.8600000	1.23	0.3476
Day	4	12.2400000	3.0600000	0.98	0.4550
<b>Catalyst</b>	<b>4</b>	<b>141.4400000</b>	<b>35.3600000</b>	<b>11.31</b>	<b>0.0005</b>

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The GLM Procedure

Tukey's Studentized Range (HSD) Test for Time

NOTE: This test controls the Type I experimentwise error rate, but it generally has a higher Type II error rate than REGWQ.

Alpha	0.05
Error Degrees of Freedom	12
Error Mean Square	3.126667
Critical Value of Studentized Range	4.50771
Minimum Significant Difference	3.5646

Means with the same letter are not significantly different.

Tukey Grouping	Mean	N	Catalyst
A	8.800	5	<b>C</b>
A			
A	8.400	5	<b>A</b>
A			
B A	5.600	5	<b>B</b>
B			
B	3.400	5	<b>D</b>
B			
B	3.200	5	<b>E</b>

3.a. The p-value for additive is well below alpha ( $p = 0.0012$ ), so we can reject the null hypothesis that additive does not have an effect on mileage. The p-value for the blocks (i.e. car) is also significant, indicating that the type of car also affected mileage.

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The GLM Procedure

Class Level Information

Class	Levels	Values
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Car	5	1 2 3 4 5
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Additive	5	1 2 3 4 5
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Number of Observations Read	20
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Number of Observations Used	20
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The GLM Procedure

Dependent Variable: Mileage Mileage

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
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Model	8	66.93333333	8.36666667	9.19	<b>0.0007</b>
Error	11	10.01666667	0.91060606		
Corrected Total	19	76.95000000			

R-Square	Coeff Var	Root MSE	Mileage Mean
0.869829	7.919144	0.954257	12.05000

Source	DF	Type III SS	Mean Square	F Value	Pr > F
Car	4	35.23333333	8.80833333	9.67	0.0013
Additive	4	35.73333333	8.93333333	9.81	<b>0.0012</b>

3.b. From the Tukey test, one can see that the only differences are between 1-3, 1-4, 1-5, and 2-5. The best mileage is attained by using additive 1 or 2 (although since 2 is not different from 3 or 4, one might choose additive 1 for the best results). When performing a Tukey test on the blocks, you discover that car 5 is significantly lower in mileage than the other cars, so the investigator may choose to omit this car in the next experiment to eliminate unnecessary variation between blocks.

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The GLM Procedure

Tukey's Studentized Range (HSD) Test for Mileage

NOTE: This test controls the Type I experimentwise error rate, but it generally has a higher Type II error rate than REGWQ.

Alpha	0.05
Error Degrees of Freedom	11
Error Mean Square	0.910606
Critical Value of Studentized Range	4.57360
Minimum Significant Difference	2.1822

Means with the same letter are not significantly different.

Tukey Grouping	Mean	N	Additive
<b>A</b>	<b>14.0000</b>	<b>4</b>	<b>1</b>
A			
B A	12.7500	4	2
B			
B C	11.7500	4	4
B C			
B C	11.5000	4	3
C			
C	10.2500	4	5

Tukey's Studentized Range (HSD) Test for Mileage

NOTE: This test controls the Type I experimentwise error rate, but it generally has a higher Type II



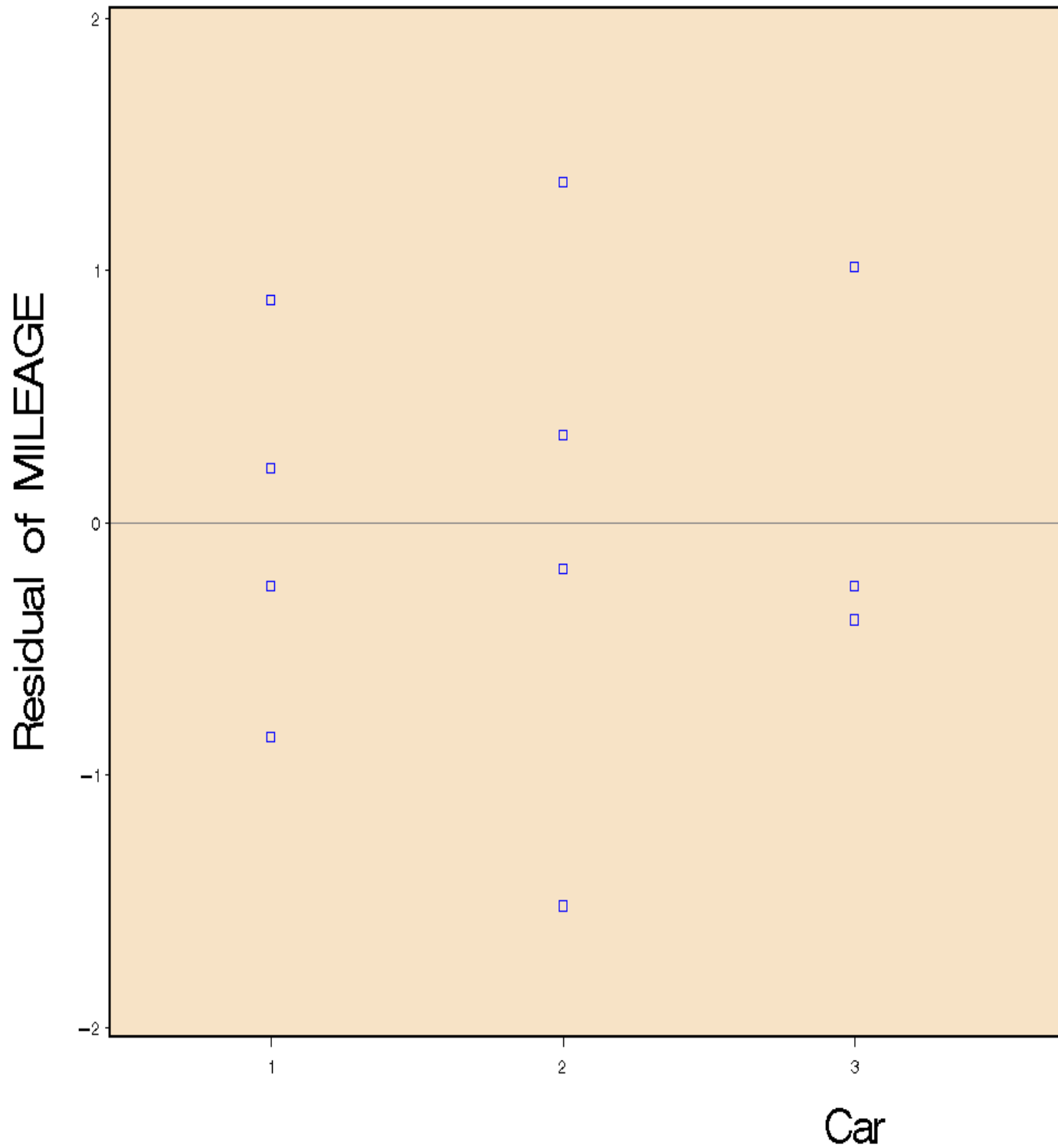
error rate than REGWQ.

Alpha	0.05
Error Degrees of Freedom	11
Error Mean Square	0.910606
Critical Value of Studentized Range	4.57360
Minimum Significant Difference	2.1822

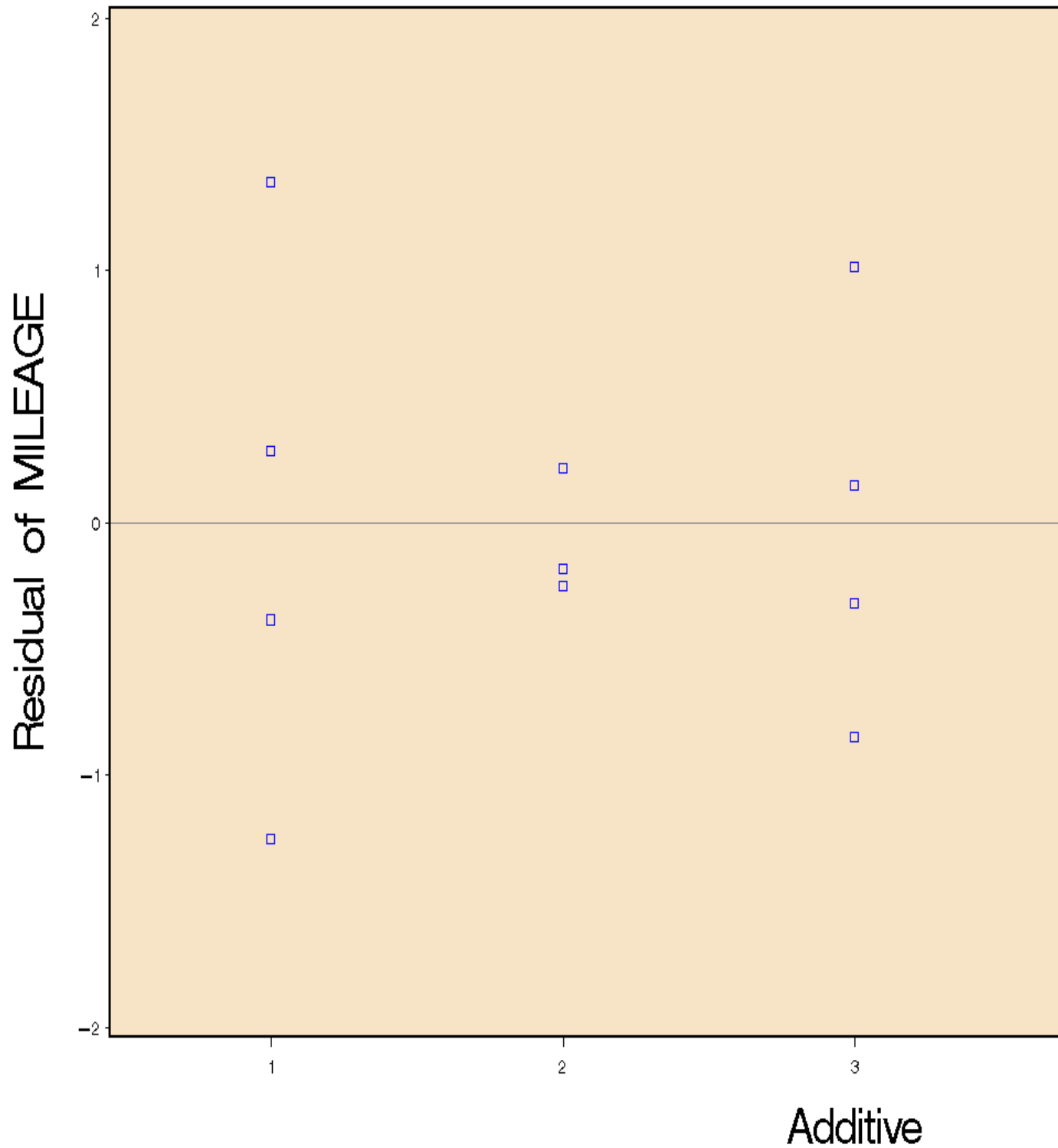
Means with the same letter are not significantly different.

Tukey Grouping	Mean	N	Car
A	13.5000	4	2
A			
A	12.5000	4	1
A			
A	12.5000	4	4
A			
A	12.0000	4	3
<b>B</b>	<b>9.7500</b>	<b>4</b>	<b>5</b>

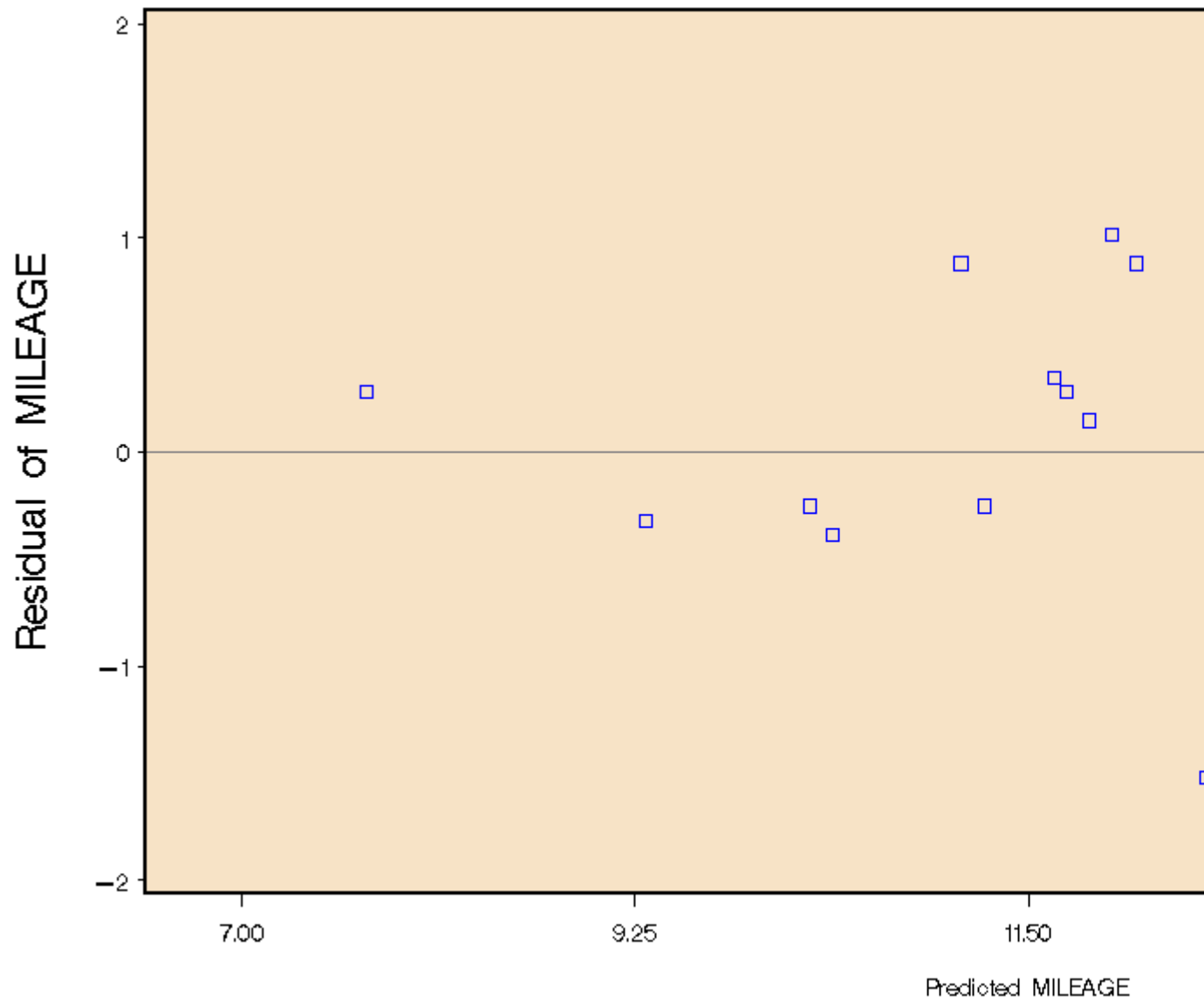
The plot of mileage residuals by car looks to satisfy the ANOVA assumptions (even though there might be a slight megaphone effect, since the blocks are categorical we could rearrange the plot with no penalty).



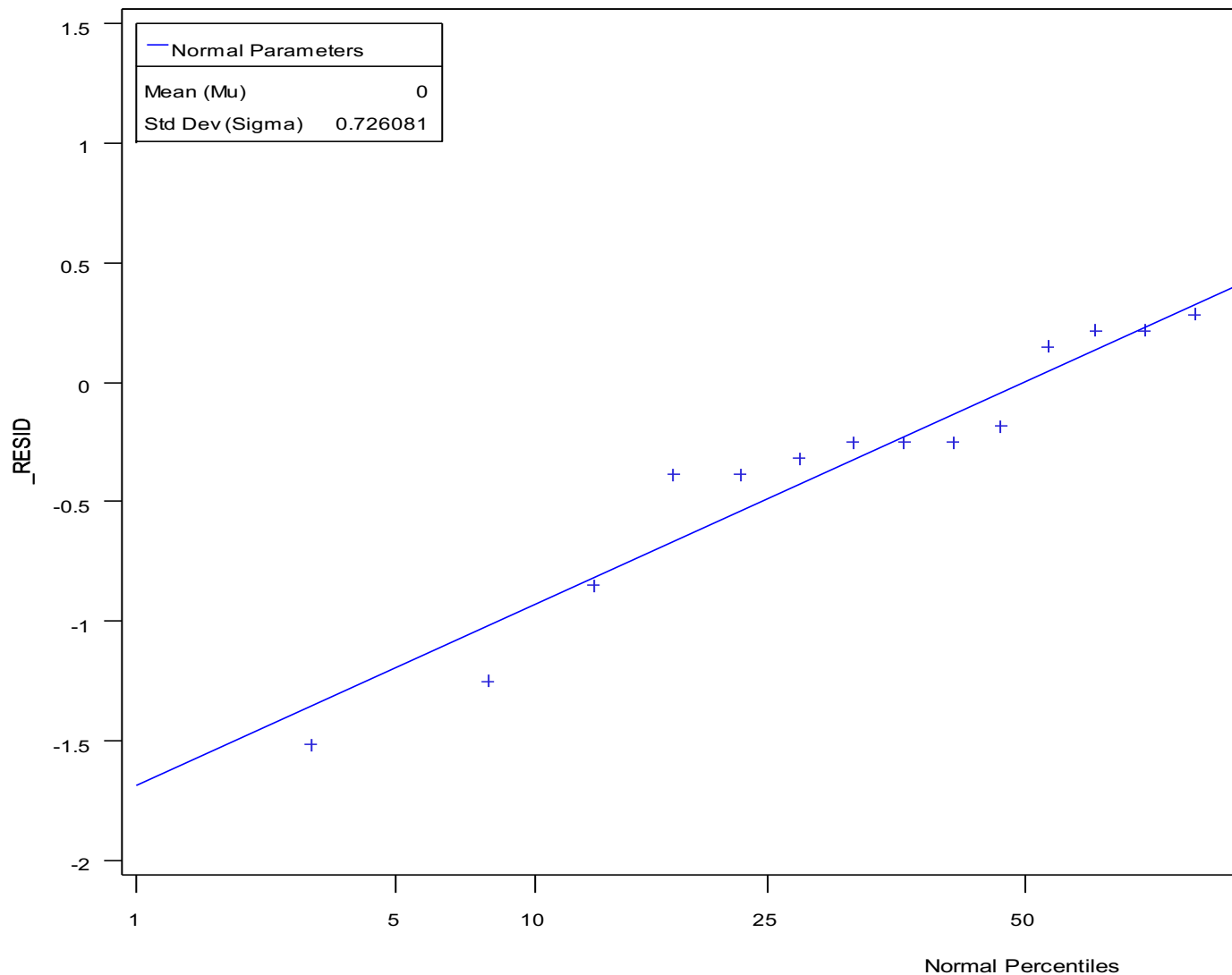
The plot of mileage residual by additive shows a slight megaphone effect, although again since the data is categorical we could rearrange it and eliminate this effect. Thus, the ANOVA assumptions are met.



The plot of mileage residuals by predicted mileage has a slight megaphone effect, which may caution us that the ANOVA assumptions are not met. Since the two prior plots look OK, I think we can trust the model.



The normal probability plot looks like there is non-linearity in the data since the middle data points are horizontally aligned rather than diagonally. The model may not be a good fit.



3.c. From the orthogonal contrasts, we can conclude that additive 3 is not different from the rest, but groups 1-2 and 4-5 are significantly different ( $p = 0.0001$ ). The comparison of additives 1 and 2 almost meets significance criteria ( $p = 0.0591$ ), but additives 4 and 5 do not ( $p = 0.2395$ ). This confirms the findings from the Tukey test above.

Contrast	DF	Contrast SS	Mean Square	F Value	Pr > F
Additive 3 vs. Others	1	0.18750000	0.18750000	0.21	0.6588
Additives 1 and 2 vs. Additives 4 and 5	1	30.10416667	30.10416667	33.06	<b>0.0001</b>
Additives 1 vs. Additive 2	1	4.03333333	4.03333333	4.43	0.0591
Additives 4 vs. Additive 5	1	1.40833333	1.40833333	1.55	0.2395

```
proc glm data=Work.P_03;
  class ADDITIVE CAR;
  model MILEAGE = ADDITIVE CAR / SS3;
```

```

contrast 'Additive 3 vs. Others' additive          1 1 -4 1
1;
contrast 'Additives 1 and 2 vs. Additives 4 and 5' additive 1 1 0 -1
-1;
contrast 'Additives 1 vs. Additive 2' additive      -1 1 0 0
0;
contrast 'Additives 4 vs. Additive 5' additive      0 0 0 -1
1;
run; quit;

```

4.a. The overall model is significant ( $p < 0.0001$ ), and all three variables (cooking\_time, pressure, and hardwood) are all significant, thus they affect the strength of paper. In terms of interactions, the only significant one is hardwood x pressure (cookingtime x pressure is trend level [ $p = 0.07$ ], but not significant). After removing the non-significant interactions, the results are basically the same, but the p-values for the interaction and hardwood got higher. From the Tukey test, one can see that the 4 hour cooking time produces stronger paper, hardwood concentration 2 produces stronger paper, and pressure of 650 also produces stronger paper (all of these are significantly different from the other conditions).

#### The GLM Procedure

##### Class Level Information

Class	Levels	Values
Hardwood	3	2 4 8
Cooking_Time	2	3 4
Pressure	3	400 500 650

Number of Observations Read	36
Number of Observations Used	36
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#### The GLM Procedure

Dependent Variable: Strength Strength

Source	DF	Sum of		Mean Square	F Value	Pr > F
		Squares				
Model	17	59.72888889		3.51346405	9.61	<.0001
Error	18	6.58000000		0.36555556		
Corrected Total	35	66.30888889				

R-Square	Coeff Var	Root MSE	Strength Mean
0.900767	0.305274	0.604612	198.0556

Source	DF	Type III SS	Mean Square	F Value	Pr > F
Cooking_Time	1	20.25000000	20.25000000	55.40	<.0001

Hardwood	2	7.76388889	3.88194444	10.62	0.0009
Pressure	2	19.37388889	9.68694444	26.50	<.0001
Hardwood*Cooking_Tim	2	2.08166667	1.04083333	2.85	0.0843
Cooking_Tim*Pressure	2	2.19500000	1.09750000	3.00	0.0750
Hardwood*Pressure	4	6.09111111	1.52277778	4.17	0.0146
Hardwo*Cookin*Pressu	4	1.97333333	0.49333333	1.35	0.2903

#### AFTER REMOVING NON-SIGNIFICANT INTERACTIONS

Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
<b>Model</b>	<b>9</b>	<b>53.47888889</b>	<b>5.94209877</b>	<b>12.04</b>	<b>&lt;.0001</b>
<b>Error</b>	<b>26</b>	<b>12.83000000</b>	<b>0.49346154</b>		
<b>Corrected Total</b>	<b>35</b>	<b>66.30888889</b>			

R-Square	Coeff Var	Root MSE	Strength Mean
<b>0.806512</b>	<b>0.354682</b>	<b>0.702468</b>	<b>198.0556</b>

Source	DF	Type III SS	Mean Square	F Value	Pr > F
<b>Cooking_Time</b>	<b>1</b>	<b>20.25000000</b>	<b>20.25000000</b>	<b>41.04</b>	<b>&lt;.0001</b>
<b>Hardwood</b>	<b>2</b>	<b>7.76388889</b>	<b>3.88194444</b>	<b>7.87</b>	<b>0.0021</b>
<b>Pressure</b>	<b>2</b>	<b>19.37388889</b>	<b>9.68694444</b>	<b>19.63</b>	<b>&lt;.0001</b>
<b>Hardwood*Pressure</b>	<b>4</b>	<b>6.09111111</b>	<b>1.52277778</b>	<b>3.09</b>	<b>0.0332</b>

Tukey's Studentized Range (HSD) Test for Strength

NOTE: This test controls the Type I experimentwise error rate, but it generally has a higher Type II error rate than REGWQ.

Alpha	0.05
Error Degrees of Freedom	18
Error Mean Square	0.365556
Critical Value of Studentized Range	2.97115
Minimum Significant Difference	0.4234

Means with the same letter are not significantly different.

Tukey Grouping	Mean	N	Cooking_ Time
A	198.8056	18	4
B	197.3056	18	3

Alpha	0.05
Error Degrees of Freedom	18
Error Mean Square	0.365556
Critical Value of Studentized Range	3.60930
Minimum Significant Difference	0.63

Means with the same letter are not significantly different.

Tukey Grouping	Mean	N	Hardwood
A	198.6667	12	2

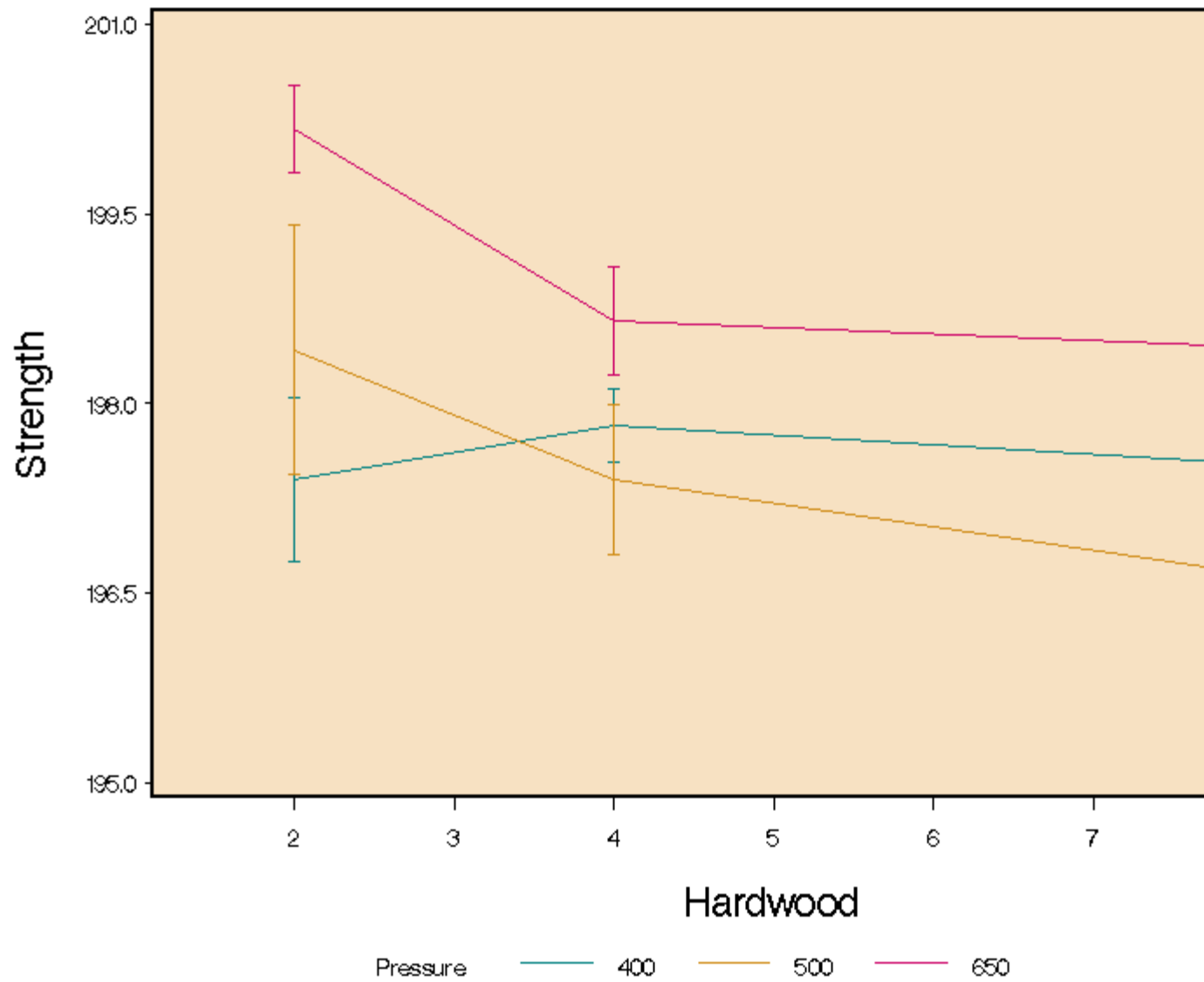
A				
B	A	197.9583	12	4
B				
B		197.5417	12	8
Alpha 0.05				
Error Degrees of Freedom		18		
Error Mean Square		0.365556		
Critical Value of Studentized Range		3.60930		
Minimum Significant Difference		0.63		

Means with the same letter are not significantly different.

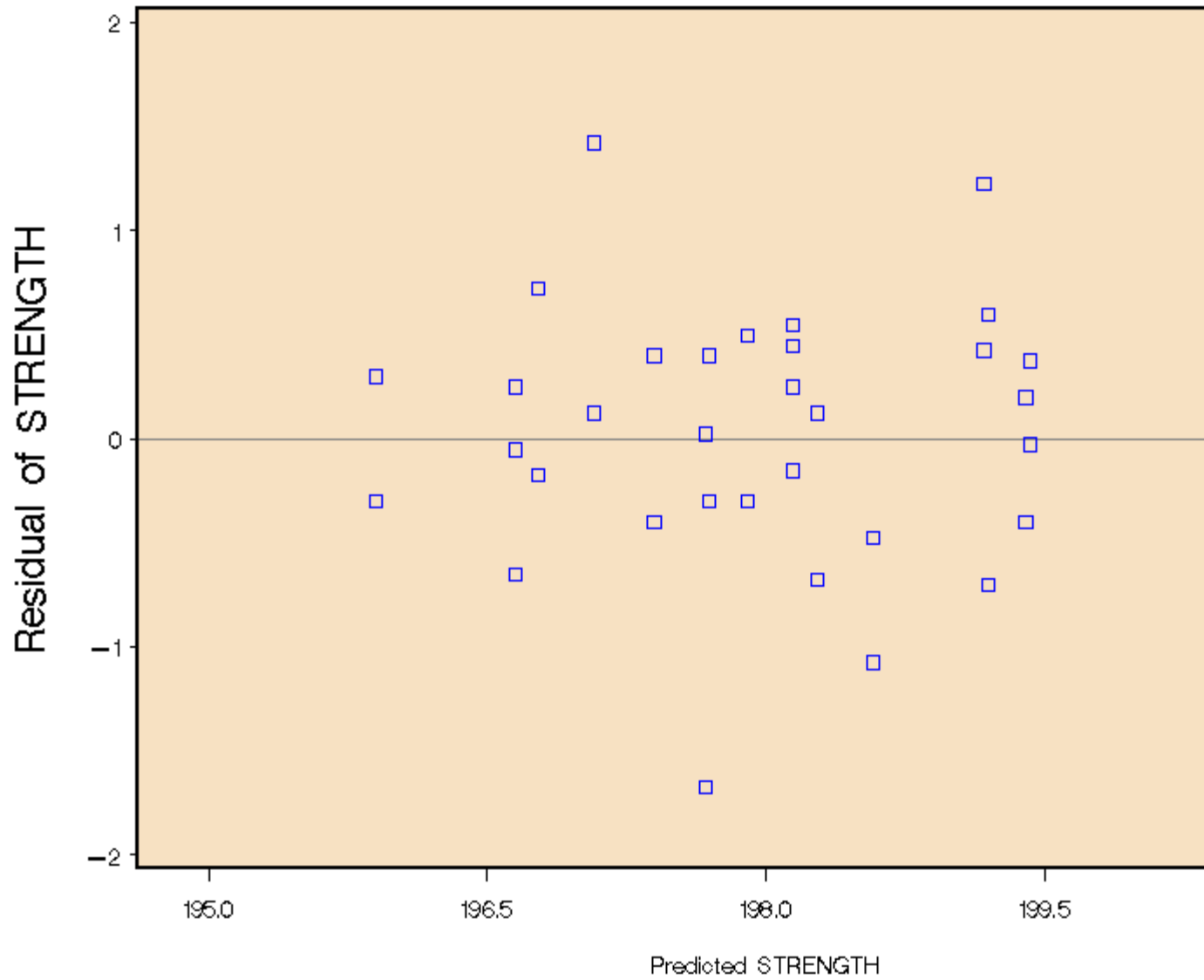
Tukey Grouping	Mean	N	Pressure
	A	199.0917	12 650
B	197.5833	12	400
B			
B	197.4917	12	500

In the interaction plot, you can see that the strongest paper is made by hardwood 2 and pressure 650, and that the pressure of 650 produces stronger paper than any other combination. The weakest paper is made by hardwood 2 and 400 pressure, but the other two hardwood concentrations with 400 pressure make stronger paper than 500 or 650 pressure, indicating some interaction between hardwood 2 and pressure 400.

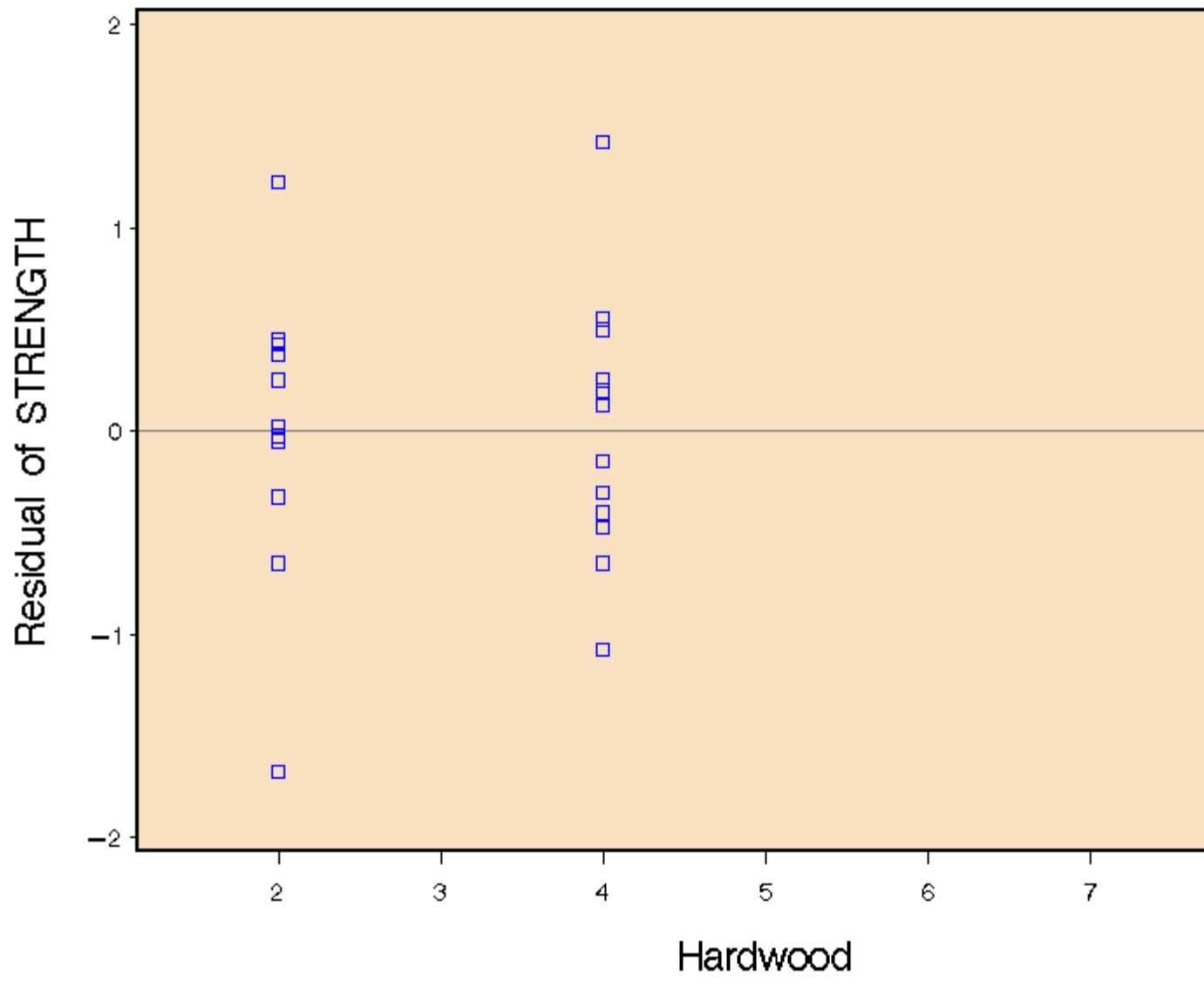




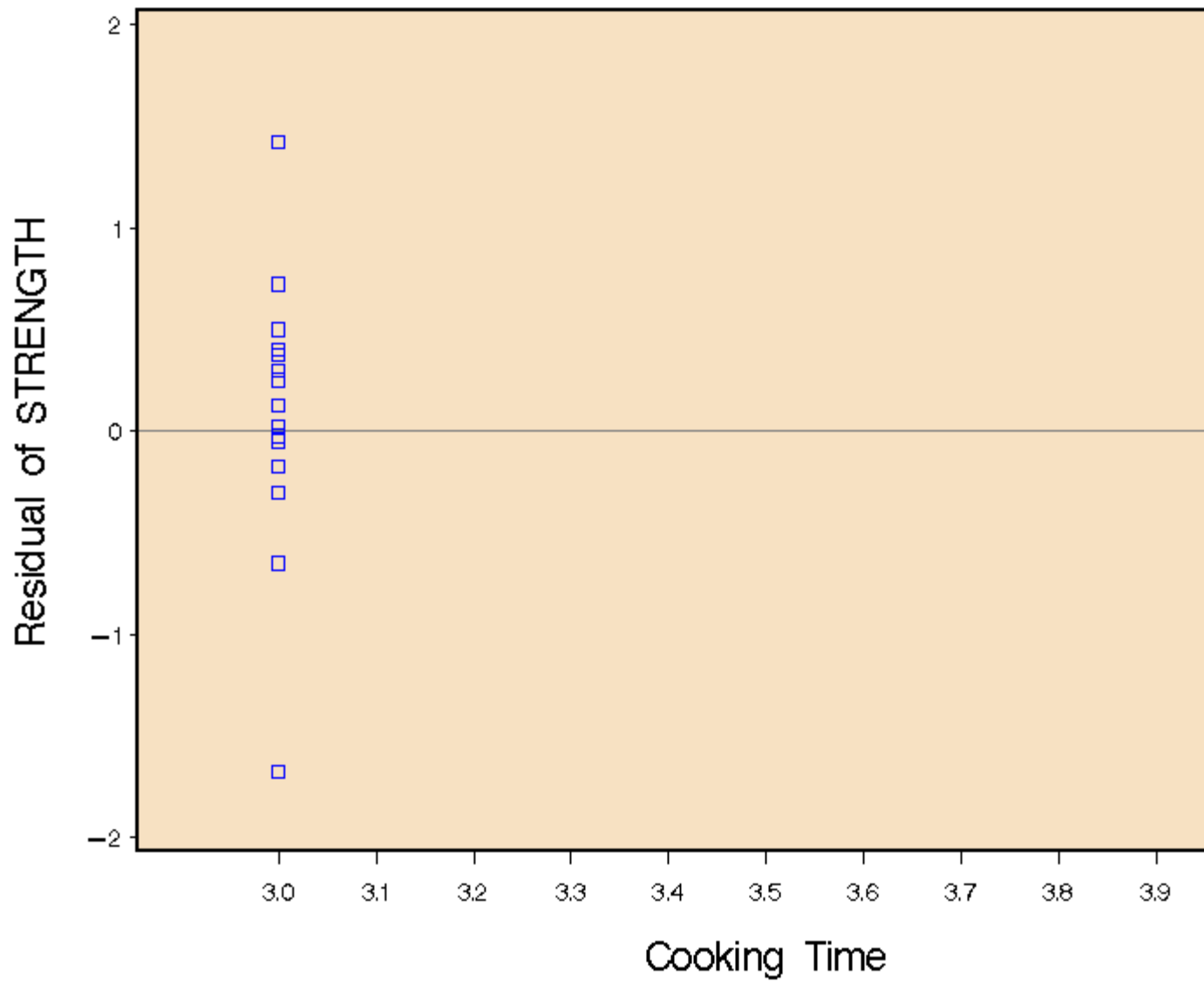
4.b. The residuals of strength by predicted strength are distributed randomly and appear to have independent and constant variance. There are a few outliers, but generally the plot looks to satisfy the ANOVA assumptions.



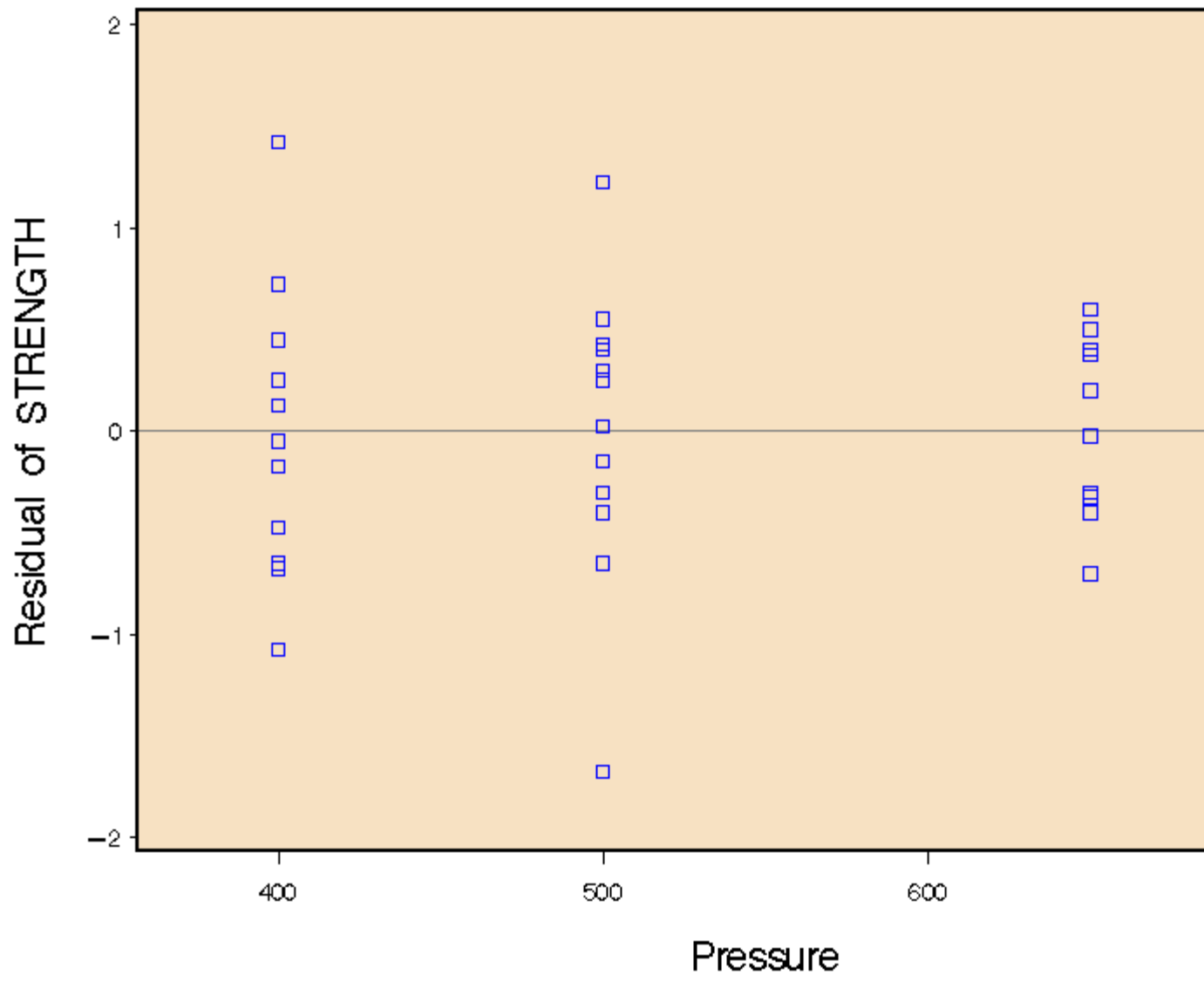
The plot of strength residuals by hardwood appears to have random distribution and constant and independent variance. There may be a slight megaphone effect, but overall the plot looks OK.



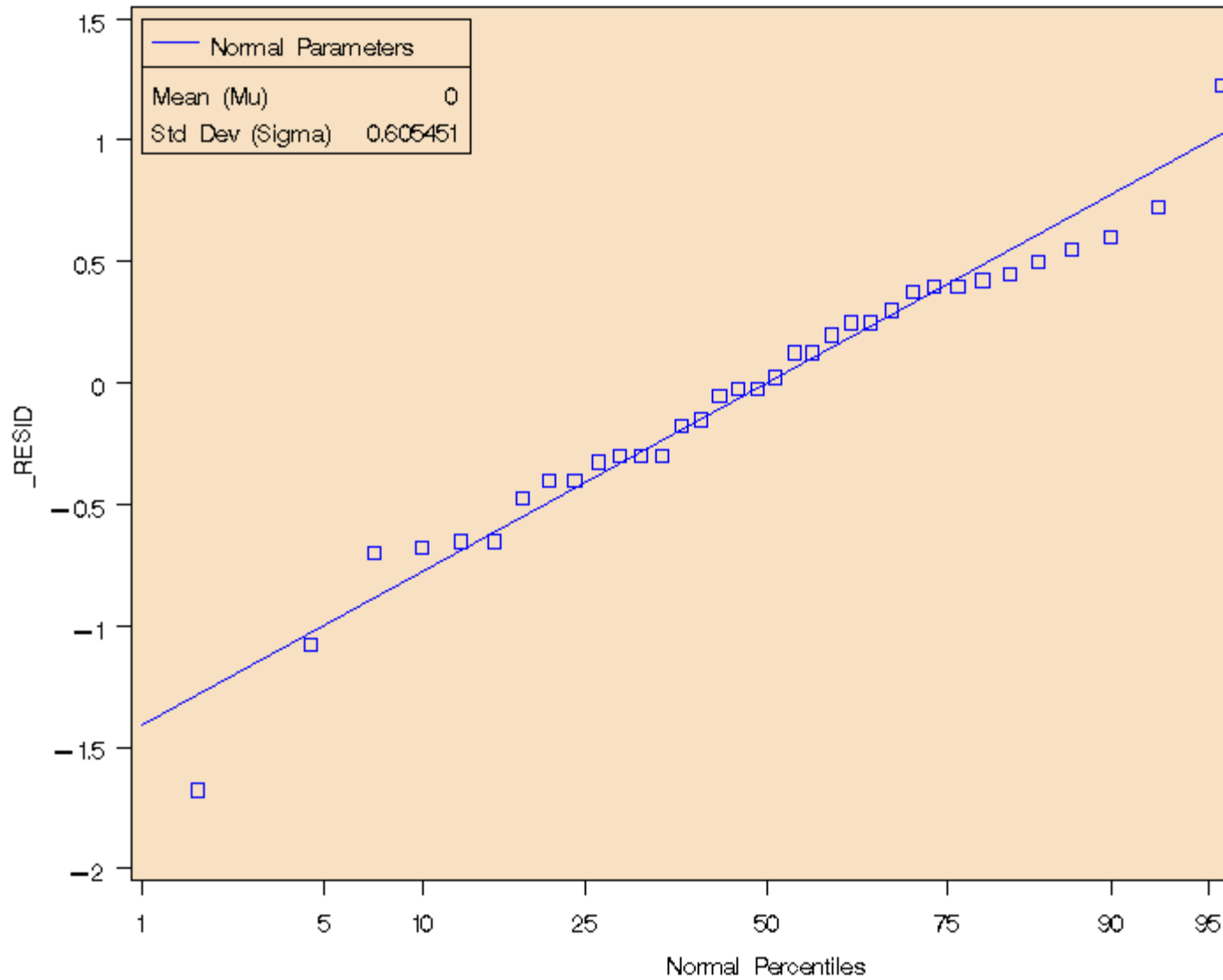
The plot of strength residuals by cooking time appears to have random distribution and constant and independent variance.



The plot of strength residuals by pressure appear to have a megaphone effect with less variation for 650.



The normal probability plot of strength residuals does look to be OK; there are a few visible outliers, but it looks OK



4.c. I would run the process with 4 hour cooking time, percentage hardwood concentration of 2, and pressure of 650 to get the strongest paper.