Homework Nine

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5.18a. As the *n* is large, we can use the $\chi^2_{(p)}$ critical value, and reject the null hypothesis if $T^2 > \chi^2_{(p)}(\alpha)$ (Result 5.4). For $\chi^2_{(3)}(0.05)$, the critical value is 7.814. Since the T^2 is larger than $\chi^2_{(3)}(0.001)$ (223.2 > 7.814), we can reject the null hypothesis that the current scores are not different from the past 10 year scores at the 0.05 level.

To use the normal theory test (Statement 5-7) where T^2 is distributed as $((n-1)p/(n-p))^*F_{p, n-p}$, and $F_{3, 87-3}$ (0.05) = 2.27, the critical value for rejecting the null hypothesis is 6.97. Based on Hotelling's T^2 , we can conclude that the current scores are statistically different than those over the last 10 years (reject null hypothesis), since $T^2 > F(223.3 > 6.97)$.

mu0 xbar

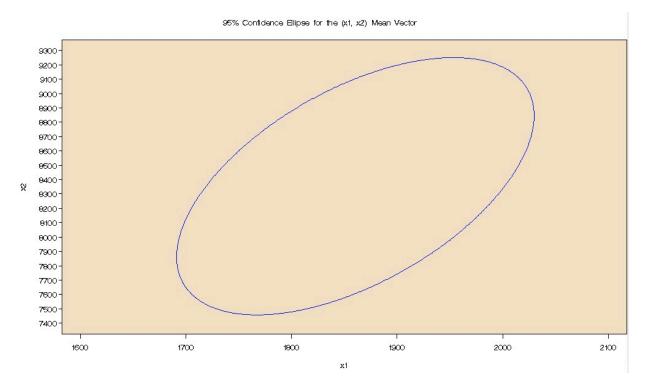
500 526.58621
50 54.689655
30 25.126437

s sinv

5808.0593 597.8352 222.02967 0.0004319 -0.001574 -0.002557
597.8352 126.05373 23.388532 -0.001574 0.0155044 -0.000567
222.02967 23.388532 23.111735 -0.002557 -0.000567 0.0684014

t2 f df1 df2 p
223.31018 72.705639 3 84 <0.0001

5.19a.



Half-length of major and minor axes:

```
x1. 901.65222
x2. 140.51187
```

```
Variable n
              xbar
                      variance
                                  t1
   x1
         30 1860.50
                      124054.67 2.04523
         30 8354.13 3486333.15 2.04523
    x2
     f
              losimultaneousCI
                                 upsimultaneousCI
    3.34039
                   1691.35
                                       2029.65
                                       9250.85
    3.34039
                   7457.41
                         S
                124054.67 361620.45
                361620.45 3486333.2
           EvecS
                         EvalS
    0.1057399 0.9943938 3524786.5
                                       3.3403856
    0.9943938 -0.10574 0 85601.376
/* 18a */
 infile "\\psf\Home\Documents\University\Spring_2012\STA4702\Datasets\T5-2.dat";
  input x1 x2 x3;
run;
proc iml;
  start hotel;
```

```
mu0 = {500, 50, 30};
    one=j(nrow(x), 1, 1);
    ident=i(nrow(x));
    ybar=x`*one/nrow(x);
    s=x * (ident-one*one \ /nrow(x)) *x/(nrow(x)-1.0);
    sinv = inv(s);
    print mu0 ybar;
    print s sinv;
    t2=nrow(x)*(ybar-mu0)`*inv(s)*(ybar-mu0);
    f = (nrow(x) - ncol(x)) *t2/ncol(x)/(nrow(x) -1);
    df1=ncol(x);
    df2=nrow(x)-ncol(x);
    p=1-probf(f,df1,df2);
    print t2 f df1 df2 p;
  finish;
  use t52;
  read all var{x1 x2 x3} into x;
  print x;
  run hotel;
quit;
/* 19a */
data t511;
 infile "\\psf\Home\Documents\University\Spring 2012\STA4702\Datasets\T5-11.dat";
  input x1 x2;
/* Program to graph the confidence ellipse for the mean vector */
%let inputdata = t511; /* this line must be edited */
           = x1 ;
                                /* this line must be edited */
%let var1
               = x2
                                  /* this line must be edited */
%let var2
                                   /* Confidence level desired*/
             = 95
%let conf
proc corr data=&inputdata noprint nocorr cov outp=covout(type=cov);
   var &var1 &var2;
run:
data covonly;
   set covout;
   if _type_='COV';
   keep &var1 &var2;
data meanonly;
   set covout;
   if _type_='MEAN';
   keep &var1 &var2;
run;
data nonly;
  set covout;
   if type ='N';
   keep &var1 &var2;
run:
proc iml;
  use covonly;
  read all into S;
   p = ncol(S);
  use meanonly;
  read all into xbar;
   xbar = xbar`;
  use nonly;
  read all into n; n=n[1,1];
  A = S/n;
  Evec = Eigvec(A);
  Eval = diag(Eigval(A));
  EvecS = Eigvec(S);
  EvalS = diag(Eigval(S));
  try1 = Evec*Eval*Evec`;
  center = xbar;
  F = finv(\&conf/100, p, n-p);
```

```
one = (p*(n-1));
  two = (n*(n-p));
  diff = ((p*(n-1))/(n*(n-p)))*F;
  diffT = sqrt(((p*(n-1))/(n-p))*finv(&conf/100, p, n-p));
  ss = sqrt(diag(S)/n);
  distances = sqrt(diag(EvalS))*sqrt(((p*(n-1))/(n*(n-p)))*finv(&conf/100, p, n-p));
  distance = sqrt((n-1)*p*finv(&conf/100, p, n-p) / (n-p));
  T2distminus = xbar - sqrt(((p*(n-1))/(n-p))*finv(&conf/100, p, n-p))*sqrt(diag(S)/
n);
              = xbar + sqrt((p*(n-1))/(n-p))*finv(&conf/100, p, n-p))*sqrt(diag(S)/
 T2distplus
n);
 print xbar distance distances center EvecS EvalS F one two diff diffT S T2distminus
T2distplus ss;
npoints = 1000;
free xbig;
do r = 1 to npoints;
    angle = 2*3.14159265 * (r/npoints);
    w1 = sin(angle);
    w2 = cos(angle);
    w = w1//w2;
    x = Evec*sqrt(Eval)*distance*w + center;
    xbig = xbig//x;
end:
create plotdata from xbig;
append from xbig;
quit;
goptions ftext=SWISS ctext=BLACK htext=1 cells;
axis1 width=1 offset=(3 pct) label=(a=90 r=0);
axis2 width=1 offset=(3 pct) ;
symbol1 c=BLUE ci=BLUE v=none height=1 cells
        interpol=spline l=1 w=1;
proc gplot data=Work.Plotdata(rename=(Col1=&var1 Col2=&var2)) ;
   title "&conf% Confidence Ellipse for the (&var1, &var2) Mean Vector";
   plot &var2 * &var1
      caxis = BLACK
      ctext = BLACK
      cframe = CXF7E1C2
     href=0
      vref=0
     hminor = 0
     vminor = 0
      vaxis = axis1
      haxis = axis2
      run;
quit;
goptions ftext= ctext= htext=;
symbol1;
axis1; axis2;
title;
options ls=78;
title "Confidence Intervals - t5-11";
%let p=2;
data t511 CI;
  set t511;
  variable="x1"; x=x1; output;
  variable="x2"; x=x2;
                         output;
  keep variable x;
 run:
proc sort;
 by variable;
proc means noprint;
 by variable;
```

```
var x;
output out=a n=n mean=xbar var=s2;
run;
data b;
set a;
t1=tinv(1-0.025,n-1);
tb=tinv(1-0.025/&p,n-1);
f=finv(0.95,&p,n-&p);
loone=xbar-t1*sqrt(s2/n);
upone=xbar+t1*sqrt(s2/n);
losim=xbar-sqrt(&p*(n-1)*f*s2/(n-&p)/n);
upsim=xbar+sqrt(&p*(n-1)*f*s2/(n-&p)/n);
lobon=xbar-tb*sqrt(s2/n);
upbon=xbar+tb*sqrt(s2/n);
run;
proc print;
run;
```