

(i) Printed Pages : 4

Roll No. May-2016

(ii) Questions : 7

Sub. Code :

6	6	6	8
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Exam. Code :

0	9	0	6
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B.Engg. 1st Year 2nd Semester

1046

(Mechanical) - QUANTUM AND STATISTICAL PHYSICS

(Common with ECE, IT and EEE)

Paper : APH - 203 (Common with ECE, IT & EEE)

Time Allowed : Three Hours]

[Maximum Marks : 50

Note : Attempt five questions in all, including Question No. I which is compulsory and selecting two questions from each section.

I. Answer the following briefly :

- (a) Mention the postulates of Special theory of relativity.
- (b) Explain the terms observable and operator. What is a Hermitian operator?
- (c) Define orbital angular momentum and orbital quantum number.
- (d) Explain the relation between the zero-point energy and the uncertainty principle.
- (e) How is Doppler effect different for sound and light waves?
- (f) Distinguish between Bose-Einstein and Fermi-Dirac Statistics.
- (g) Why $\Phi = ax^2$ is not acceptable wavefunction in quantum mechanics?

6668/BIK-565

1

[Turn over

on VIII Solve the one-dimensional wave equation $\frac{\partial^2 y}{\partial x^2} = \frac{\partial^2 y}{\partial t^2}$
 $y(x, 0) = f(x)$, $\frac{\partial y}{\partial t}(x, 0) = g(x)$
initial velocity. Here $y = y(x, t)$.

- (h) Explain the importance of Fermi energy.
- (i) Mention the significance of the Schwarzschild radius.
- (j) Is it possible to observe the Compton effect with visible light? Why? 10×1=10

SECTION-A

- II. (a) Discuss the Doppler effect in light. Derive an expression of change in wavelength when a source of light is receding away from the observer. Give one example to explain the relevance of this effect. 5
- (b) Describe Michelson's Morely experiment. What is the aim and conclusion of the experiment? 5
- III. (a) Calculate the wavelength of incident X-ray photon which produces recoil electron of energy 4 keV in Compton effect. The electron recoils in the direction of incident photon and photon is scattered at an angle of 180° . 3
- (b) State the postulates of quantum mechanics. 3
- (c) Show that the expression for de-Broglie wavelength of a particle with rest mass m_0 , and kinetic energy K in eV can be written as $\lambda = hc/[K(2m_0c^2 + K)]^{1/2}$ 4
- IV. (a) Two rockets of rest length L_0 are approaching the earth from opposite directions at velocities $c/2$. How long does one of them appear to the other? 3

- (b) Assume that the uncertainty in the position of a particle is equal to its de-Broglie wavelength. Show that the uncertainty in its velocity is equal to or greater than $(1/4\pi)$ times its velocity. 3

- (c) Derive Schrodinger time independent wave equation. What do you mean by stationary states? 4

SECTION-B

- V. (a) Describe Stern-Gerlach experiment with necessary theory. What was the aim of the experiment? Discuss its significance. 4

- (b) What are orthogonal wavefunctions? For a particle in one dimensional box, show that the wavefunctions for two different states are orthogonal. 4

- (c) Explain the physical significance of quantum numbers n , ℓ and m_l . How are they interrelated? 2

- VI. (a) Write a short account of the distribution of energy in the spectrum of a black body. Indicate graphically the energy distribution of black body radiation with wavelength at different temperatures. Discuss the important results with reference to Wien's and Rayleigh Jeans law. 5

- (b) State and explain Pauli's exclusion principle. How does knowledge of symmetric and anti-symmetric wave functions lead to this principle? 2

- (c) Show that the average energy of a Planck's oscillator is given by $h\nu/(e^{h\nu/kt}-1)$. 3

- VII. (a) Evaluate the transmission coefficient for an electron of total energy 2 eV incident upon a rectangular potential barrier of height 4 eV and thickness 10^{-10} m. 3
- (b) What is spin-orbit interaction ? How does it lead to the observed fine-structure splitting of the spectral lines of the hydrogen atom ? 4
- (c) Compare the probability for three bosons to be in a particular state with the three classical particles to be in the same state. 3

Printed Pages : 3

Roll No.

Questions : 8

Sub. Code :

6	6	4	5
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Exam. Code :

9	0	5
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B.Engg. 1st Semester

1125

QUANTUM AND STATISTICAL PHYSICS

Paper-APH-103

Time Allowed : Three Hours]

[Maximum Marks : 50

Note : (i) All questions carry equal marks.

(ii) Question I is compulsory.

(iii) Attempt five questions in all selecting **two** questions from each Part.

I. Attempt any **five** parts :

- (a) What is ultraviolet catastrophe ?
- (b) Why Doppler effect in light is termed as symmetric phenomenon ?
- (c) Give two distinguishing features between three kinds of statistics obeyed by different physical systems.
- (d) What are the postulates of special theory of relativity ?
- (e) What are space like events ? Do they obey principle of causality ?

(f) What are the basic requisites for wave function to represent the state of a physical system ? 3 (a)

(g) Why a particle can't be at rest in the infinitely deep one-dimensional potential well ? 2×5=10 (b)

PART-A

II. (a) Discuss Michelson-Morley experiment clearly giving its objective and results. 7

(b) Using Lorentz transformation, obtain the relation for length contraction. 3

III. (a) Derive the Lorentz transformations for different components of particles velocity. 5

(b) Show that $(E/c)^2 - p^2$ is invariant under Lorentz transformations. 5

IV. (a) Arrive at steady state form of Schrodinger's equation and show that the energy quantization is natural consequence of this equation. 6

(b) An X-ray photon is found to have its wavelength doubled on being scattered through 90° . Find the wavelength and energy of the incident photon. 4

PART-B

V. (a) A particle of mass m and kinetic energy E is incident on a one-dimensional potential step of height V_0 , such that $E < V_0$. Solve Schrodinger's equation for this particle and list the observations. How do these observations differ from the expectations of classical mechanics ? 7

(b) Prove the identity that $[x^2, p_x] = 2i\hbar x$. 3

represent (a) Discuss Stern Gerlach experiment emphasizing on its objective and outcome. 5

deep on (b) Write a brief note on Zeeman effect. 5

$\times 5 = 10$ VII. What is thermionic emission ? Using appropriate formalism of statistical physics, derive expression for Richardson Dushman equation. 10

ing VIII. Giving basic elements of Maxwell-Boltzmann distribution, derive the distribution for molecular energies in a gas. 10

Printed Pages : 3

Roll No.

Questions : 7

Sub. Code :

6	6	5	7
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Exam. Code :

9	0	5
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B.E. Computer Science & Engg. 1st Semester

1124

QUANTUM AND STATISTICAL PHYSICS

Paper : APH-103

Time Allowed : Three Hours]

[Maximum Marks : 50

Note :- Attempt five questions in all including the compulsory question no. 1. All questions carry equal marks.

1. (a) State the two postulates of Special Theory of Relativity. 2
(b) What are the postulates of Quantum Mechanics ? 2
(c) Construct normalized, completely anti-symmetric two particle wavefunction. 2
(d) What is :
(i) Compton Effect 2
(ii) Photoelectric Effect ? 2
(e) What is Black Body Radiation ? Explain. 2
2. (a) Write a note on Lorentz transformations. 5
(b) In the reference frame of a star, the light emitted has frequency 5.55×10^{13} Hz, whereas an observer measured it as 6.66×10^{14} Hz. At what speed the star is moving towards / away from the observer ? 3

6657/BDF-24750

1

[Turn over

O6. i) Explain the difference between structures and union
input and output functions in C.

- (c) How do two velocities add up in :
 (i) Galilean frame
 (ii) Lorentz frame ?
3. (a) A typical atomic nucleus radius is about 5×10^{-15} meters. Argue using uncertainty principle that it is not possible for it to contain electron. 4
 (b) What is Bragg's Law ? How does it help in finding structure of a crystal ? 3
 (c) What is de Broglie Hypothesis ? What is the typical value of de Broglie wave length of electron ? 3
4. (a) Use the ground state linear harmonic oscillator wavefunction to show by direct integration that expectation value of momentum operator P , $(\langle \Psi_0 | P | \Psi_0 \rangle)$ is zero. 4
 (b) Explain qualitatively what happens when a quantum particle comes across a :
 (i) Potential well
 (ii) Potential barrier. 6
5. (a) Discuss qualitatively the Hydrogen Atom Spectrum. 5
 (b) What happens when a Hydrogen atom is placed in magnetic field ? 3
 (c) What does Stern-Gerlach experiment reveal ? 2
6. (a) Give a qualitative description of Kronig-Penney model. 5

(b) How does one distinguish conductors, semiconductors and insulators ? 5

(a) Briefly describe :

(i) Maxwell-Boltzman statistics

(ii) Bose-Einstein statistics and

(iii) Fermi-Dirac statistics. 6

(b) Why the electrons in a metal do not contribute to its specific heat except at very high and very low temperatures ? 4

1127
B.E. (Biotechnology)
First Semester
APH-103: Quantum and Statistical Physics
(Common with IT and CSE)

Time allowed: 3 Hours

Max. Marks: 50

NOTE: Attempt five questions in all, including Question No. 1 which is compulsory and selecting two questions from each Section.

x-x-x

I Attempt any five parts (2 x 5=10)

- (a) Draw and discuss the working of a Ferry's black body.
- (b) What were the conclusions of Davison Germer experiment.
- (c) Distinguish between macrostate and microstate of a statistical system.
- (d) Show that Lorentz transformations of coordinates of a moving particle reduces to Galilean transformation when speed of particle is negligible as compared to the speed of light.
- (e) Qualitatively argue that Heisenberg's uncertainty principle is natural consequence of wave nature of a particle.
- (f) Why a particle of mass m trapped in an infinitely deep one dimensional potential well can never be at rest.
- (g) How is the performance of PIN diode improves due to tunneling effect.

Section A

- II (a) What was the objective of Michelson Morley experiment. Describe the working of interferometer used in this experiment. Giving observations, discuss the inferences drawn from this experiment. (7)
- (b) Derive the energy-momentum relation $E^2 = p^2 c^2 + m^2 c^4$. (3)
- III (a) How was meson decay problem explained through the concept of special theory of relativity. (5)
- (b) Show that $(x^2 + y^2 + z^2 - c^2 t^2)$ is invariant under Lorentz transformations. (5)
- IV (a) What is photoelectric effect. How does quantum theory explains this phenomenon. (6)

- (b) An x-ray photon is found to have its wavelength doubled on being scattered through 90° . Find the wavelength and energy of the incident photon. (4)

Section B

- V (a) A particle of mass m and kinetic energy E is trapped in one dimensional potential well of infinite depth. Solve Schrodinger's equation for this particle to obtain permissible states of trapped particle. Further show that energy quantization is a natural consequence. (7)
- (b) Prove the identity that $[x^2, p_x] = 2i\hbar x$ (3)
- VI.(a) Derive the expression for radiative transitions in the hydrogen atom. What are its guiding selection rules. (5)
- (b) Discuss objective, working and inferences of Stern-Gerlach experiment. (5)
- VII What is black body radiation? Using appropriate formalism of statistical physics, derive expression for Planck's radiation formula. (10)

Exam. Code: 0905
Sub. Code: 6645

1128
B.E. (Bio-Technology) First Semester
APH-103: Quantum and Statistical Physics
(Common with IT and CSE)

Max. Marks: 50

Time allowed: 3 Hours

NOTE: Attempt five questions in all, including Question No. 1 which is compulsory and selecting two questions from each Part.

x-x-x

I. Attempt any five of the following:-

- What is paradoxical about twin paradox?
- Why pair production cannot occur in free space?
- Why gravitational red shift is not apparent for most of the stars?
- What are the angles between L and the z axis for $l = 1$? For $l = 2$?
- Why is it not possible for Stern-Gerlach-experiment to be performed in a uniform magnetic field?
- Distinguish between macrostate and microstate of a statistical system.
- Under what condition do B-E and F-D statistics yield Classical statistics? (5x2)

UNIT - I

- What was the aim and conclusion of Michelsen-Morely experiment?
 - According to the postulates of Einstein theory, laws of physics are same in all inertial frame. What about non-inertial frames? Why they can't be same in non-inertial frame?
 - What were the limitations of Galilean transformations? Obtain Lorentz transformation laws for position and time coordinates. Why we consider $y=y'$ and $z=z'$? (2,3,5)
- How are continuous and characteristic X-rays produced? How can you control the intensity and penetrating power of the X-rays?
 - Work function of nickel is 5.01 eV. Will violet light of wavelength 400nm cause the photoelectric effect in nickel?
 - Cite an experiment which proved de Broglie's hypothesis. (3,3,4)

P.T.O.

(2)

- IV. a) What is the Born's interpretation of quantum mechanical wave function? What are the essential requirements for an acceptable (well-behaved) wave function?
- b) Using operator mechanics find commutator $[\hat{x}, \hat{p}_x^2]$.
- c) Qualitatively show that Heisenberg's Uncertainty principle is natural consequence of wave nature of particle. (4,4,2)

UNIT - II

- V. a) A particle having energy E faces a step potential barrier of height V_0 at $X=0$. Show that even if $E < V_0$, the particle has finite probability to tunnel into the region $X > 0$.
- b) Prove that average value of r for a 1s electron in hydrogen atom is $\frac{3}{2} a_0$. a_0 is Bohr

radius and wave function for 1s electron is $\psi = \frac{e^{-\frac{r}{a_0}}}{\sqrt{\pi a_0^3}}$

- VI. a) How is the Pauli exclusion principle a consequence of antisymmetric wave function?
- b) Show that Rayleigh-Jeans law failed but Plank's radiation law successfully explained the observed radiation spectrum of a blackbody. (5,5)
- VII. a) Discuss the phenomenon of thermionic emission in metals. Obtain Richardson - Dushman equation.

- b) Show that the most probable speed of an ideal gas molecule is $\sqrt{\frac{2kt}{m}}$. (6,4)

1018

B. Engg. (Mechanical)

1st Year (2nd Semester)

APH-203: Quantum and Statistical Physics

(Common with ECE, IT & EEE)

Time allowed: 3 Hours

Max. Marks: 50

Note: Attempt five questions in all, including Question No. 1 which is compulsory and selecting two questions from each Part.

x-x-x

Q1. Attempt any five parts:

- (a) For most of the stars gravitational red shift is not apparent. Why?
- (b) What bearing would you think the uncertainty principle has on the zero point energy of a harmonic oscillator?
- (c) Why is it impossible for a $2^2D_{3/2}$ state to exist?
- (d) Find the value of $[\hat{x}, \hat{p}_x^2]$.
- (e) What is the significance of Fermi energy in a fermion system at 0K? At $T > 0K$?
- (f) Calculate the number of different arrangements of 6 bosons among 4 cells of equal a priori probability.
- (g) Under what circumstances, if any, is L_z equal to L ?

5 X 2=10

Part A

- Q2. (a) Deduce the relativistic velocity addition theorem. Show that it is consistent with second postulate of relativity. (4)
- (b) Show that the mass of an object depends on its velocity. Cite an experiment to support this fact. (4)
- (c) An electron ($m = 0.511 \text{ MeV}/c^2$) and a photon ($m=0$) both have momenta of $2.00 \text{ MeV}/c$. Find the total energy of each. (2)

- Q3. (a) What is Compton Effect? Find the maximum energy of the recoil electron. (6)
- (b) Find the Schwarzschild radius of the earth, whose mass is $5.98 \times 10^{24} \text{ Kg}$. (2)
- (c) A positron collides head on with an electron and both are annihilated. Each particle had a kinetic energy of 1 MeV. Find the wavelength of the resulting photons. (2)

- Q4. (a) Is it correct to say that the maximum photoelectron energy KE_{max} is proportional to the frequency of incident light? If not, what would a correct statement of the relationship between KE_{max} and frequency ' f ' be? (3)
- (b) The wave function of a particle is $\psi = A \cos^2 x$ for $-\frac{\pi}{2} < x < \frac{\pi}{2}$. (i) Find the value of A . (ii) Find the probability that the particle be found between $x=0$ and $x=\frac{\pi}{4}$. (4)
- (c) What is Heisenberg's uncertainty principle? Apply it to prove the non-existence of the electron in the nucleus. (3)

P.T.O

Part B

- Q5. (a) Show that the evenly spaced energy levels of quantum harmonic oscillator are given by equation: $E_n = \left(n + \frac{1}{2}\right) \hbar \omega$ where n is quantum number. What is zero point energy of the harmonic oscillator. (6)
- (b) An electron is bound by a potential which closely approaches an infinite potential square well of width $2.5 \times 10^{-10} \text{ m}$. Calculate the lowest three permissible quantum energies the electron can have. (4)
- Q6. (a) Write the wave function for hydrogen atom. Discuss the significance of the quantum numbers. (5)
- (b) What was the basic objective of Stern Gerlach experiment? With suitable schematic, discuss the observations and results of the experiment. (5)
- Q7 (a) Show that the average kinetic energy of a three dimensional gas of N free electrons at 0°K is $\overline{E}_0 = \frac{3}{5} E_F$. (5)
- (b) State Plank's radiation law and derive it from Bose-Einstein statistics. How does this law solve ultraviolet catastrophe? (5)

x-x-x

1127

B.E. (Biotechnology)

First Semester

APH-103: Quantum and Statistical Physics
(Common with IT and CSE)

Time allowed: 3 Hours

Max. Marks: 50

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- Qualitatively argue that Heisenberg's uncertainty principle is natural consequence of wave nature of a particle.
- Why a particle of mass m trapped in an infinitely deep one dimensional potential well can never be at rest.
- How is the performance of PIN diode improves due to tunneling effect.

Section A

- What was the objective of Michelson Morley experiment. Describe the working of interferometer used in this experiment. Giving observations, discuss the inferences drawn from this experiment. (7)
 - Derive the energy-momentum relation $E^2 = p^2 c^2 + m^2 c^4$. (3)
- How was meson decay problem explained through the concept of special theory of relativity. (5)
 - Show that $(x^2 + y^2 + z^2 - c^2 t^2)$ is invariant under Lorentz transformations. (5)
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P.T.O.

- (b) An x-ray photon is found to have its wavelength doubled on being scattered through 90° . Find the wavelength and energy of the incident photon. (4)

Section B

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x-x-x