

Homework 5

p86 B.1(b), p87 C.1(a,e), p97 A.3, p101 H.5 and I.3

1. **p86 B.1(b)** Compute $\alpha^{-1}, \alpha^2, \alpha^3, \alpha^4, \alpha^5$ where $\alpha = (1234)$

Solution.

2. **p87 C.1(a)** Determine if the permutation is even or odd. Justify your answer.

$$\pi = \begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \\ 7 & 4 & 1 & 5 & 6 & 2 & 3 & 8 \end{pmatrix}$$

Solution.

3. **p87 C.1(e)** Determine if the permutation is even or odd. Justify your answer.

$$(123)(2345)(1357)$$

Solution.

4. **p97 A.3** Let G_1, G_2 , and G_3 be groups, and let $f : G_1 \rightarrow G_2$ and $g : G_2 \rightarrow G_3$ be isomorphisms. Prove that $g \circ f : G_1 \rightarrow G_3$ is an isomorphism.

Solution.

5. **p101 H.5** Let c be a fixed element of G . Let H be a group with the same set as G , and with the operation $x * y = xcy$. Prove that the function $f(x) = c^{-1}x$ is an isomorphism from G to H .

Solution.

6. **p101 I.3** If G is any group, and a is any element of G , prove that $f(x) = axa^{-1}$ is an automorphism of G .

Solution.