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#### 1. Confidence Interval for One Population

To have R calculate a confidence interval, we use the "t.test()" command. As can be seen by name this uses the t test, not the z test. I will explain in Chapter 7 why this is the better methodology. In this lab, we will just be showing you which part of the output is necessary for this Lab; the complete output will be explained in Lab 6.

**Example (DATA SET: DMS.txt – website)** Many food products contain small quantities of substances that would give an undesirable taste or smell if they were present in large amounts. An example is the "off-odors" caused by sulfur compounds in wine. Oenologists (wine experts) have determined the odor threshold, the lowest concentration of a compound that the human nose can detect. For example, the odor threshold for dimethyl sulfide (DMS) is given in the oenology literature as 25 micrograms per liter of wine ( $\mu$ g/l). Untrained noses may be less sensitive, however. Here are the DMS odor thresholds for 10 beginning students of oenology:

31	31	43	36	23	34	32	30	20	24
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(a) Generate a 95% confidence interval for the mean DMS odor threshold among all beginning oenology students.

#### Solution:

The 95% confidence interval is (25.56935, 35.23065)

# 2. Calculating the power and generating a power curve

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To calculate the power, we want to know the probability that we will reject  $H_0$  when it is false. To perform power calculations, you need to assume the real value of  $\mu$ . Therefore, if  $H_a$ :  $\mu > \mu_0$ , we want to calculate  $P(X \ge x^* \mid \mu = \mu^*, \, \mu^* > \mu_0)$  where  $\mu^*$  is a specified value greater than  $\mu_0$  and  $x^*$  is the first value x, such that (s.t.)  $x^* > x = 0$  Reject  $H_0$ :  $\mu = \mu_0$ .

**Example** Consider the following competing hypotheses:

```
H_0: \mu = 500
H_a: \mu \neq 500
```

at the 1% level of significance assuming the population standard deviation, \sigma, is known.

- (a) Generate a power curve.
- (b) What sample size would be required for the power to be at least 0.80 against the specific alternative of  $\mu$  = 498.5?

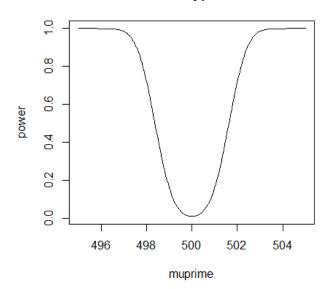
#### Solution:

(a) Generate a power curve.

```
# variables to change:
# n, alpha, mu0, sigma
# muprime: the real values of mu
   by 0.05 - this needs to be fine enough so that the curve
               looks smooth
n < -10
alpha <- 0.01
mu0 <- 500
sigma <- 2
sigman <- sigma/sqrt(n) #standard error</pre>
#z is from alpha/2 for a 2-tailed test
z \leftarrow qnorm(1 - alpha/2)
muprime <- seg(from=495, to=505, by=0.05)
x1 \leftarrow mu0 - z*sigman #Value for which <math>x < x1 \Rightarrow H 0 will be rejected
x2 \leftarrow mu0 + z*sigman #Value for which <math>x > x2 => H 0 will be rejected
px1 <- pnorm(x1, muprime, sigman) #CDF up to x1 for various muprime
px2 \leftarrow pnorm(x2, muprime, sigman, lower.tail = FALSE) #S X(x2): muprime
power <- px1 + px2 #Left Tail + Right Tail (Tails NOT symmetric!)</pre>
beta <- 1 - power #When obtaining by 'hand' beta is easier to find first
power
plot(muprime, power, main="Power for the Hypothesis Test", type="1")
```

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## Power for the Hypothesis Test



Note: To answer the questions in Part 1; just change put in the appropriate value in the following command, that is replace 'seg' with the appropriate value.

```
muprime <- seq (from=495, to=505, by=0.05)</pre>
```

# (b) What sample size would be required for the power to be at least 0.80 against the specific alternative of $\mu$ = 498.5?

```
#this time, I will fix muprime and change n;
n < -10:100
muprime <- 498.5
alpha <- .01
mu0 < -500
sigma < - 2
sigman <- sigma/sqrt(n)</pre>
z \leftarrow qnorm(1 - alpha/2)
x1 \leftarrow mu0 - z*sigman #Value for which <math>x < x1 \Rightarrow H 0 will be rejected
x2 \leftarrow mu0 + z*sigman #Value for which <math>x > x2 => H 0 will be rejected
px1 <- pnorm(x1, muprime, sigman) #CDF up to x1 for various muprime
px2 < -pnorm(x2, muprime, sigman, lower.tail = FALSE) #S <math>X(x2): muprime
power <- px1 + px2 #Left Tail + Right Tail (Tails NOT symmetric!)</pre>
beta <- 1 - power #When obtaining by 'hand' beta is easier to find first
answer <- data.frame(n, power)</pre>
answer
```

To determine the answer, look at the print out for the value of n that will produce the power that is desired.

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```
n power
1 10 0.4191298
...
11 20 0.7817959
12 21 0.8054092
13 22 0.8268992
14 23 0.8463833
...
```

I truncated the output to only the relevant parts. You may delete all lines except for the title line and the line that contains the n that you are interested in.

Therefore, n = 21 is the first value which has a power greater than 0.8.

This could also be visualized with the following lattice graphics code: