

CS4450/7450
Chapter 2: Starting Out
Principles of Programming Languages

Dr. William Harrison

University of Missouri

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GHCi is basically a fancy calculator

```
$ ghci
GHCi, version 7.10.3: http://www.haskell.org/
    ghc/  :? for help
Prelude> 4 + 2
6
Prelude> not (True && True)
False
Prelude> max 5 4
5
```

Type errors are your friends

```
Prelude> 99 + "Hey"
<interactive>:5:4:
  No instance for (Num [Char]) arising from
    a use of of `+`
  In the expression: 99 + "Hey"
  In an equation for `it`: it = 99 + "Hey"
Prelude>
```

GHCi Commands

Some Pragmatics

- `:l` or `:load` — load a file or module
- `:t:` or `:type` — give the type of an expression
- `:i` or `:info` — produce information about a definition
- `:q` or `:quit` — quit, derp.

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```
Prelude> :t not
not :: Bool -> Bool
Prelude> :i not
not :: Bool -> Bool    -- Defined in ?GHC.
      Classes?
Prelude>
```

“Baby’s First Program”

Entered in a file Chap2.hs:

```
module Chap2 where  
  
doubleMe x = x + x
```

“Baby’s First Program”, cont’d

```
$ ghci
GHCi, version 7.10.3: http://www.haskell.org/ghc/ :? for help
Prelude> :l Chap2.hs
[1 of 1] Compiling Chap2                ( Chap2.
      hs, interpreted )
Ok, modules loaded: Chap2.
*Chap2> doubleMe 9
18
*Chap2> doubleMe 3.14
6.28
*Chap2> :t doubleMe
```

“Baby’s First Program”, cont’d

```
$ ghci
GHCi, version 7.10.3: http://www.haskell.org/
    ghc/  :? for help
Prelude> :l Chap2.hs
[1 of 1] Compiling Chap2                ( Chap2.
    hs, interpreted )
Ok, modules loaded: Chap2.
*Chap2> doubleMe 9
18
*Chap2> doubleMe 3.14
6.28
*Chap2> :t doubleMe
```

```
doubleMe :: Num a => a -> a
*Chap2>
```


Lists, an Introduction to

```
Prelude> let lostNumbers = [4,8,15,16,23,42]
Prelude> lostNumbers
[4,8,15,16,23,42]

Prelude> 99 : lostNumbers
[99,4,8,15,16,23,42]

Prelude> [1,2,3,4] ++ [9,10,11,12]
[1,2,3,4,9,10,11,12]

Prelude> "hello" ++ " " ++ "world"
"hello world"

Prelude> ['w','0'] ++ ['0','t']
"w00t"
```

Type Declarations

In Haskell, a new name for an existing type can be defined using a type declaration.

```
type String = [Char]
```

String is a synonym for the type [Char].

Type declarations can be used to make other types easier to read. For example, given

```
type Pos = (Int, Int)
```

we can define

```
origin      :: Pos  
origin      = (0, 0)  
  
left        :: Pos -> Pos  
left (x, y) = (x-1, y)
```

Like function definitions, type declarations can also have parameters. For example, given

```
type Pair a = (a, a)
```

we can define

```
mult      :: Pair Int -> Int
mult (m,n) = m*n

copy      :: a -> Pair a
copy x    = (x,x)
```

Type declarations can be nested:

```
type Pos    = (Int,Int)    -- GOOD  
type Trans = Pos -> Pos    -- GOOD
```

However, they cannot be recursive:

```
type Tree = (Int,[Tree])  -- BAD
```

Data Declarations

A completely new type can be defined by specifying its values using a data declaration.

```
data Bool = False | True
```

`Bool` is a new type, with two new values `False` and `True`.

Note:

- The two values False and True are called the constructors for the type Bool.
- Type and constructor names must begin with an upper-case letter.
- Data declarations are similar to context free grammars. The former specifies the values of a type, the latter the sentences of a language.

Values of new types can be used in the same ways as those of built in types. For example, given

```
data Answer = Yes | No | Unknown
```

we can define:

```
answers      :: [Answer]
answers      = [Yes, No, Unknown]

flip         :: Answer -> Answer
flip Yes     = No
flip No      = Yes
flip Unknown = Unknown
```


The constructors in a data declaration can also have parameters. For example, given

```
data Shape = Circle Float
           | Rect Float Float
```

we can define:

```
square      :: Float -> Shape
square n    = Rect n n
area        :: Shape -> Float
area (Circle r) = pi * r^2
area (Rect x y) = x * y
```

Note:

- Shape has values of the form `Circle r` where `r` is a float, and `Rect x y` where `x` and `y` are floats.
- `Circle` and `Rect` **are** functions that construct values of type `Shape`:

```
-- Not a definition  
Circle :: Float -> Shape  
Rect   :: Float -> Float -> Shape
```

Not surprisingly, data declarations themselves can also have parameters. For example, given

```
data Maybe a = Nothing | Just a
```

we can define:

```
safediv      :: Int -> Int -> Maybe Int
safediv _ 0 = Nothing
safediv m n = Just (m `div` n)

safehead     :: [a] -> Maybe a
safehead [] = Nothing
safehead xs = Just (head xs)
```

Recursive Types

In Haskell, new types can be declared in terms of themselves. That is, types can be recursive.

```
data Nat = Zero | Succ Nat
```

Nat is a new type, with constructors `Zero :: Nat` and `Succ :: Nat -> Nat`.

Note:

- A value of type `Nat` is either `Zero`, or of the form `Succ n` where $n :: \text{Nat}$. That is, `Nat` contains the following infinite sequence of values:

`Zero`

`Succ Zero`

`Succ (Succ Zero)`

`⋮`

Note:

- We can think of values of type `Nat` as natural numbers, where `Zero` represents 0, and `Succ` represents the successor function $1+$.
- For example, the value

```
Succ (Succ (Succ Zero))
```

represents the natural number

```
1 + (1 + (1 + 0))
```

Using recursion, it is easy to define functions that convert between values of type `Nat` and `Int`:

```
nat2int          :: Nat -> Int
nat2int Zero     = 0
nat2int (Succ n) = 1 + nat2int n

int2nat          :: Int -> Nat
int2nat 0        = Zero
int2nat n        = Succ (int2nat (n - 1))
```

Two naturals can be added by converting them to integers, adding, and then converting back:

```
add      :: Nat -> Nat -> Nat
add m n = int2nat (nat2int m + nat2int n)
```

However, using recursion the function `add` can be defined without the need for conversions:

```
add Zero      n = n
add (Succ m) n = Succ (add m n)
```

The recursive definition for `add` corresponds to the laws

$$0 + n = n$$

and

$$(1 + m) + n = 1 + (m + n)$$

Using recursion, an expression tree can be defined using:

```
data Expr = Val Int
          | Add Expr Expr
          | Mul Expr Expr
```

One example of such a tree written in Haskell is

```
Add (Val 1) (Mul (Val 2) (Val 3))
```

Using recursion, it is now easy to define functions that process expressions. For example:

```
size          :: Expr -> Int
size (Val n)   = 1
size (Add x y) = size x + size y
size (Mul x y) = size x + size y

eval          :: Expr -> Int
eval (Val n)   = n
eval (Add x y) = eval x + eval y
eval (Mul x y) = eval x * eval y
```

Note:

- The three constructors have types:

```
-- Not a definition  
Val  :: Int -> Expr  
Add  :: Expr -> Expr -> Expr  
Mul  :: Expr -> Expr -> Expr
```

Using recursion, a binary tree can be defined using:

```
data Tree = Leaf Int
          | Node Tree Int Tree
```

One example of such a tree written in Haskell is

```
Node (Node (Leaf 1) 3 (Leaf 4))
      5
      (Node (Leaf 6) 7 (Leaf 9))
```

We can now define a function that decides if a given integer occurs in a binary tree:

```
occurs :: Int -> Tree -> Bool
occurs m (Leaf n)      = m==n
occurs m (Node l n r) = m==n
                        || occurs m l
                        || occurs m r
```

In the worst case, when the integer does not occur, this function traverses the entire tree.

Search trees have the important property that when trying to find a value in a tree we can always decide which of the two sub-trees it may occur in:

```
occurs :: Int -> Tree -> Bool
occurs m (Leaf n)           = m==n
occurs m (Node l n r) | m==n = True
                      | m<n  = occurs m l
                      | m>n  = occurs m r
```

This new definition is more efficient, because it only traverses one path down the tree.

What is the precondition for Node?

Finally consider the function `flatten` that returns the list of all the integers contained in a tree:

```
flatten :: Tree -> [Int]
flatten (Leaf n)      = [n]
flatten (Node l n r) = flatten l
                      ++ [n]
                      ++ flatten r
```

A tree is a search tree if it flattens to a list that is ordered.