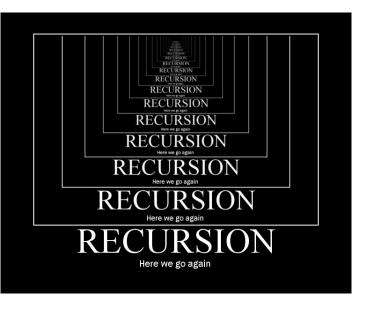
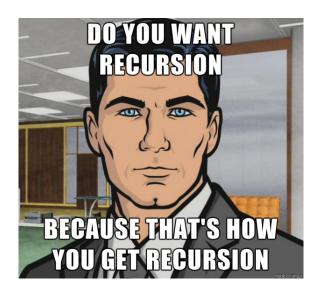
# CS4450/7450 AoPL, Chapter 5: Recursion Principles of Programming Languages

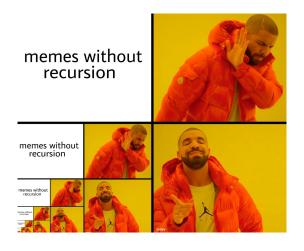
Dr. William Harrison

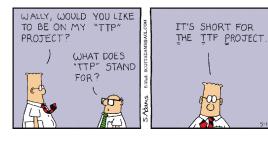
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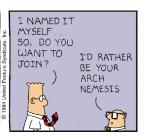
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#### Announcements

- We're continuing with William Cook's online textbook, Anatomy of Programming Languages. It is available here. We're in Chapter 5.
- All programming languages have some notion of recursion—even if you don't think of it as recursion:

```
while b { c } = if b then c ; while b { c } else halt
```

• This chapter answers the question: what is recursion?

# Outline for section 1

Semantics of Recursion

2 Understanding Recursion using Haskell Recursion

## Recursive Functions

Recursive Functions are functions that call themselves:

```
let
   fac = \ n -> if n == 0 then 1 else n * fac(n-1)
in
   fac(5)
```

• In the concrete syntax of the FirstClassFunctions.hs interpreter, this is written:

```
var fac = function(n) { if (n==0) 1 else n * fac(n-1) }; fac(5)
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• Let's test this out using First Class Functions.

# Review from AoPL 2: Scope

#### Scope of a Variable Declaration

is the portion of the code text where that declaration holds.

### What's the Problem?

• The scope of the red declaration is the red code, not the blue code:

```
var fac = function(n) { if (n==0) 1 else n * fac(n-1) }; fac(5)
```

so there's no binding for fac

# Outline for section 2

Semantics of Recursion

2 Understanding Recursion using Haskell Recursion

# Implementing Recursion using Haskell's Recursion

Here's the way we defined local declarations

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eval (Declare x exp body) env = eval body newEnv
where newEnv = (x, eval exp env) : env
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  - To allow the bound variable x to be used within the expression exp, the expression must be evaluated in the new environment.

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- The problem here is that the bound expression exp is evaluated in the parent environment env.
  - To allow the bound variable x to be used within the expression exp, the expression must be evaluated in the new environment.
- Fortunately this is easy to implement in Haskell:

```
eval (Declare x exp body) env = eval body newEnv
where newEnv = (x, eval exp newEnv) : env
```

• We still need non-recursive declarations; e.g., don't intend for the following to be recursive:

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let x = x + 1 in x
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Additional eval clause:

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eval (RecDeclare x exp body) env = eval body newEnv
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Additional eval clause:

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eval (RecDeclare x exp body) env = eval body newEnv
where newEnv = (x, eval exp newEnv) : env
```

• In the concrete syntax of the RecursiveFunctions.hs interpreter, this is written:

```
rec fac = function(n) { if (n==0) 1 else n * fac(n-1) }; fac(5)
```