

CS4450

Bill Harrison

Pattern  
Matching

Guards in  
Patterns

Where Clauses

Let Bindings

Case  
Expressions

# CS4450/7450

## Chapter 4: Syntax in Functions

### Principles of Programming Languages

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# What is a Pattern?

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```
data I = A | B | C
foo :: I -> String
foo A = "One"
foo B = "Two"
foo C = "Three"
```

A *pattern* is anything in the **argument position** of a function definition.

# What is a Pattern?

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```
data I = A | B | C
foo :: I -> String
foo A = "One"
foo B = "Two"
foo C = "Three"
```

A *pattern* is anything in the **argument position** of a function definition. There are:

- variable patterns, wildcard patterns, constructor patterns, as-patterns

...and bigger patterns are composed of smaller patterns.

# Wildcard Patterns

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The underscore “`_`” is a wildcard pattern. They match anything.

```
first :: (a, b, c) -> a
```

```
first (x, _, _) = x
```

```
second :: (a, b, c) -> b
```

```
second (_, y, _) = y
```

```
third :: (a, b, c) -> c
```

```
third (_, _, z) = z
```

Wildcards are good to use to indicate that you don't care about the value it matches.

# Variable Patterns

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Variable patterns match anything:

```
addVectors :: (Num a) => (a, a) -> (a, a) -> (a, a)
addVectors a b = (fst a + fst b, snd a + snd b)
```

# Variable Patterns

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Variable patterns match anything:

```
addVectors :: (Num a) => (a, a) -> (a, a) -> (a, a)
addVectors a b = (fst a + fst b, snd a + snd b)
```

In the following application, `a` and `b` are bound to `(5, 6)` and `(7, 8)`, respectively.

```
addVectors (5, 6) (7, 8)
```

# Variable Patterns

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Variable patterns match anything:

```
addVectors :: (Num a) => (a, a) -> (a, a) -> (a, a)
addVectors a b = (fst a + fst b, snd a + snd b)
```

In the following application, `a` and `b` are bound to `(5, 6)` and `(7, 8)`, respectively.

```
addVectors (5, 6) (7, 8)
```

Can also express structure of the input directly using patterns:

```
addVectors :: (Num a) => (a, a) -> (a, a) -> (a, a)
addVectors (x1, y1) (x2, y2) = (x1 + x2, y1 + y2)
```

# Constructor Patterns

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Recall that lists have two constructors:

```
data [a] = [] | (a : [a])
```



# Constructor Patterns

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Recall that lists have two constructors:

```
data [a] = [] | (a : [a])
```

Constructors, when appearing in argument position, are patterns:

```
length :: (Num b) => [a] -> b
```

```
length [] = 0
```

```
length (_:xs) = 1 + length xs
```

# Composite Patterns

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Patterns can be composed to make bigger patterns, thereby giving you more expressiveness in matching values:

```
tell :: (Show a) => [a] -> String
tell []          = "The list is empty"
tell (x:[])      = "The list has one element: " ++ show
                  x
tell (x:y:[])    = "The list has two elements: " ++ show
                  x ++ " and " ++ show y
tell (x:y:_)     = "This list is long. The first two
                  elements are: " ++ show x ++ " and " ++ show y
```

# As Patterns

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Here, “as” is @

```
capital :: String -> String
capital "" = "Empty string, whoops!"
capital all@(x:xs) = "The first letter of "
                    ++ all ++ " is " ++ [x]
```

```
ghci> capital "Dracula"
"The first letter of Dracula is D"
```

# Guards

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It's easy enough to write the maximum function using  
if-then-else:

```
max :: Float -> Float -> Float  
max a b = if a < b then b else a
```

# Guards

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It's easy enough to write the maximum function using `if-then-else`:

```
max :: Float -> Float -> Float  
max a b = if a<b then b else a
```

Another way to define the identical function is with *guards*:

```
max :: Float -> Float -> Float  
max a b | a<b           = b  
        | otherwise = a
```

# Why use guards: Readability.

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This is much more readable:

```
bmiTell :: (RealFloat a) => a -> String
bmiTell bmi
  | bmi <= 18.5 = "underweight"
  | bmi <= 25.0 = "normal"
  | bmi <= 30.0 = "overweight"
  | otherwise   = "obese"
```

# Why use guards: Readability.

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  | bmi <= 18.5 = "underweight"
  | bmi <= 25.0 = "normal"
  | bmi <= 30.0 = "overweight"
  | otherwise   = "obese"
```

...than this:

```
bmiTell :: (RealFloat a) => a -> String
bmiTell bmi = if bmi <= 18.5
               then "underweight"
               else if bmi <= 25.0
                   then "normal"
               else if bmi <= 30.0
                   then "overweight"
               else
                   "obese"
```

# Where clauses

let you define local variables

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```
bmiTell :: (RealFloat a) => a -> a -> String
bmiTell weight height
  | weight / height ^ 2 <= 18.5 = "underweight"
  | weight / height ^ 2 <= 25.0 = "normal"
  | weight / height ^ 2 <= 30.0 = "overweight"
  | otherwise                  = "obese"
```



# Where clauses

let you define local variables

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```
bmiTell :: (RealFloat a) => a -> a -> String
bmiTell weight height
  | weight / height ^ 2 <= 18.5 = "underweight"
  | weight / height ^ 2 <= 25.0 = "normal"
  | weight / height ^ 2 <= 30.0 = "overweight"
  | otherwise                  = "obese"
```

```
bmiTell :: (RealFloat a) => a -> a -> String
bmiTell weight height
  | bmi <= 18.5 = "underweight"
  | bmi <= 25.0 = "normal"
  | bmi <= 30.0 = "overweight"
  | otherwise   = "obese"
where
  bmi = weight / height ^ 2
  -- calculate bmi once, use value repeatedly
```

# Let definitions

...are just like where clauses

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```
cylinder :: (RealFloat a) => a -> a -> a
cylinder r h =
    let
        sideArea = 2 * pi * r * h
        topArea  = pi * r ^2
    in
        sideArea + 2 * topArea
```

- Variables defined in a `let` or `where` clauses are local
- E.g., `sideArea` and `topArea` can be used only in the body of the `let/where`.

# Case Expressions

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General form of a case expression:

```
case expression of pattern -> result  
                    pattern -> result  
                    pattern -> result  
                    ...
```

# Case Expressions

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General form of a case expression:

```
case expression of pattern -> result  
                    pattern -> result  
                    pattern -> result  
                    ...
```

```
head :: [a] -> a
```

```
head []      = error "empty list"
```

```
head (x:_) = x
```

# Case Expressions

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General form of a case expression:

```
case expression of pattern -> result
                        pattern -> result
                        pattern -> result
                        ...
```

```
head :: [a] -> a
head []      = error "empty list"
head (x:_) = x
```

A way to define the identical function:

```
head :: [a] -> a
head xs = case xs of
    []      -> error "empty list"
    (x:_)   -> x
```