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LAB REPORT

on

Artificial Intelligence (23CS5PCAIN)

Submitted by

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in partial fulfillment for the award of the degree of
BACHELOR OF ENGINEERING
in
COMPUTER SCIENCE AND ENGINEERING



B.M.S. COLLEGE OF ENGINEERING

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**B.M.S. College of Engineering,
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CERTIFICATE

This is to certify that the Lab work entitled “Artificial Intelligence (23CS5PCAIN)” carried out by **Harbakshish Singh Arora (1BM23CS104)**, who is a bonafide student of **B.M.S.**

College of Engineering. It is in partial fulfillment for the award of **Bachelor of Engineering in Computer Science and Engineering** of the Visvesvaraya Technological University, Belgaum. The Lab report has been approved as it satisfies the academic requirements in respect of an Artificial Intelligence (23CS5PCAIN) work prescribed for the said degree.

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Program 1: Implement Tic – Tac – Toe Game & Implement vacuum cleaner agent.

ALGORITHM (Tic-Tac-Toe) :

TIC TAC TOE

→ Algorithm:

- Step 1 → Start by building a 3×3 board, keep player as 'O' and the computer as 'X'.
- Step 2 → Let the user play the first move, also initialize all the winning patterns.
- Step 3 → Loop until a winner is not found or till all the boxes aren't occupied.
 - In the loop everytime check for a winner or for a draw.
 - When the computer has it's turn, first try to check if human is winning, if so try to block it.
 - Else try to play the best move which could be placing at the centre (block 4) or the corners. Also if the computer is winning, check the sequence and try to complete the winning sequence. Switch the input back to user.
- Step 4 → Give the result after the loop is terminated.

→ Eg:

'O' is human
'X' is computer

TIC TAC TOE

player wins

player wins

player wins

player wins

Draw

player wins

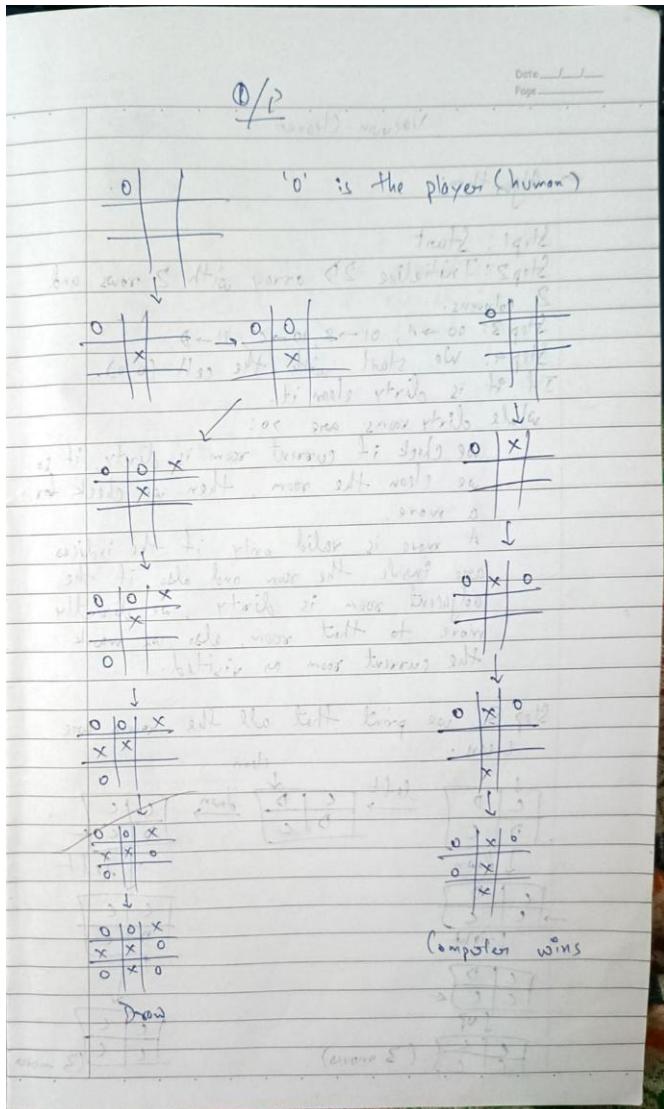
Draw

player wins

Draw

player wins

Draw



CODE (Tic-Tac-Toe) :

```

import math import
random def
print_board(board):
    """Prints the current state of the game board."""
for row in [board[i:i+3] for i in range(0, 9, 3)]:
    print('| ' + ' | '.join(row) + ' |')
def available_moves(board):
    """Returns a list of available spots on the board."""
return [i for i, spot in enumerate(board) if spot == ' ']
def check_winner(board, player):
    """Checks if the given player has won the game."""

```

```

# Check for winning rows    for i in
range(0, 9, 3):      if all(s == player for s
in board[i:i+3]):  

    return True  
  

# Check for winning columns   for i in range(3):  

if board[i] == board[i+3] == board[i+6] == player:  

    return True  
  

# Check for winning diagonals   if board[0]
== board[4] == board[8] == player:      return
True   if board[2] == board[4] == board[6] ==
player:  

    return True  
  

return False  
  

def minimax(board, is_maximizing):  

    """  

    Minimax algorithm to find the best move.  

    'X' is the maximizing player (computer), 'O' is the minimizing player (human).  

    """  

    ai_player =  

    'X'  human_player  

    = 'O'  
  

    if check_winner(board, ai_player):  

        return 1, None  if  

check_winner(board, human_player):  

        return -1, None  if not  

available_moves(board):  

    return 0, None

```

```

if is_maximizing:      best_score = -
math.inf      best_move = None      for
move in available_moves(board):
board[move] = ai_player      score, _
= minimax(board, False)
board[move] = ''      if score >
best_score:      best_score = score
best_move = move      return
best_score, best_move  else:
best_score = math.inf
best_move = None      for move in
available_moves(board):
board[move] = human_player
score, _ = minimax(board, True)
board[move] = ''      if score <
best_score:      best_score = score
best_move = move
return best_score, best_move

```

```
def get_computer_move(board):
```

```
"""

```

Gets a beatable move for the computer. It finds all moves with a positive score and chooses one randomly. If no such moves exist, it chooses a random move to prolong the game.

```
"""
ai_player =
'X'  human_player
= 'O'
```

```
# If the board is empty, take the center.
if not available_moves(board):
return 4
```

```

# Check for an immediate win for the computer
for move in available_moves(board):
    board[move] = ai_player      if
check_winner(board, ai_player):
    board[move] = ''
return move      board[move]
= ''

```

```

# Check for an immediate block of the human
player   for move in available_moves(board):
board[move] = human_player      if
check_winner(board, human_player):
    board[move] = ''
return move      board[move]
= ''

```

```

# If no immediate win or block, use a simplified minimax approach.
# Find all moves that result in a positive score.
positive_moves = []   for move in
available_moves(board):
board[move] = ai_player      score, _
= minimax(board, False)
board[move] = ''      if score > 0:
    positive_moves.append(move)

```

```

# If there are any moves that lead to a win or a draw, pick one at random.
if positive_moves:
    return random.choice(positive_moves)

```

```

# If all remaining moves lead to a loss, choose a random available move to delay the loss.
return random.choice(available_moves(board))

```

```

def get_player_move(board):
    """Gets a valid move from the human
player."""
    while True:
        move = int(input("Enter your move (1-9): ")) - 1
    if move not in available_moves(board):
        print("Invalid move. Please enter a number from 1-9 that is not taken.")
    else:
        return move
    except ValueError:
        print("Invalid input. Please enter a number.")

def play_game():
    """The main function to run the Tic-Tac-Toe game loop."""
    board = [' '] * 9
    print("Welcome to Tic-Tac-Toe!") print_board(board)

    # Let the human player ('O') go first.
    turn = 'O'

    while True:
        if turn == 'O':
            # Human's turn
            move =
            get_player_move(board)
            board[move] = 'O'
        else:
            # Computer's turn
            print("Computer is thinking...")
            move = get_computer_move(board)
            board[move] = 'X'

            print(f'Player {turn} makes a move to square {move + 1}')
            print_board(board)

```

```
# Check for a winner after the
move      if check_winner(board, turn):
print(f"{turn} wins!")      break

# Check for a tie      if not
available_moves(board):
    print("It's a draw!")
break

# Switch turns      turn = 'X'
if turn == 'O' else 'O'
```

```
if __name__ == "__main__":
    play_game()
```

OUTPUT:

```
Welcome to Tic-Tac-Toe!
| | | |
| | | |
| | | |
Enter your move (1-9): 5
Player 0 makes a move to square 5
| | | |
| | 0 | |
| | | |
Computer is thinking...
Player X makes a move to square 6
| | | |
| | 0 | X |
| | | |
Enter your move (1-9): 1
Player 0 makes a move to square 1
| 0 | | |
| | 0 | X |
| | | |
Computer is thinking...
Player X makes a move to square 9
| 0 | | |
| | 0 | X |
| | | X |
Enter your move (1-9): 3
Player 0 makes a move to square 3
| 0 | | 0 |
| | 0 | X |
| | | X |
Computer is thinking...
Player X makes a move to square 2
| 0 | X | 0 |
| | 0 | X |
| | | X |
Enter your move (1-9): 7
Player 0 makes a move to square 7
| 0 | X | 0 |
| | 0 | X |
| 0 | | X |
0 wins!
```

ALGORITHM (Vacuum Cleaner):

Vacuum Cleaner

→ Algorithm:

Step 1: Start
 Step 2: Initialize 2D array with 2 rows and 2 columns.
 Step 3: 00 → A, 01 → B, 10 → C, 11 → D
 Step 4: We start with the cell (0,0).
 If it is dirty clean it.
 while dirty rooms are > 0:
 we check if current room is dirty, if so we clean the room, then we check for a move.
 A move is valid only if the indices are inside the room and also if the adjacent room is dirty, we directly move to that room, also we mark the current room as visited.

Step 5: we print that all the rooms were clean:

→ Output:

Room = $\begin{bmatrix} D & C \\ D & D \end{bmatrix}$

Started with (0,0) & cleaned it
 Moved to (1,0) & cleaned it
 Moved to (1,1) & cleaned it
 Room is cleaned

Room is clean!

CODE (Vacuum cleaner) :

```
# Initialize room (2x2 grid), each cell could be 'dirty' or 'clean'
room = [
    ['dirty', 'clean'],
    ['dirty', 'dirty']
]
# Starting position
x, y = 0, 0

# Function to check if the current cell is dirty
def is_dirty(x, y):
    return room[x][y] == 'dirty'
```

```

# Function to clean the current cell
def clean(x, y):
    room[x][y] = 'clean'
    print(f'Cleaned cell ({x},{y})')

# Function to move to a new position (up, down, left, or right)
def move_to(new_x, new_y):
    global x, y
    x, y = new_x, new_y
    print(f'Moved to ({x},{y})')

# Function to check if all cells are
# clean
def all_clean():
    for i in range(2):
        for j in range(2):
            if room[i][j] == 'dirty':
                return False
    return True

# Cleaning path: Visit each cell and clean (left to right, top to bottom)
# The allowed moves are up, down, left, right
cleaning_path = [(0, 0), (0, 1), (1, 1), (1, 0)]

# Start cleaning the room following the
# path for cell in cleaning_path:
move_to(cell[0], cell[1])  if
is_dirty(cell[0], cell[1]):  clean(cell[0],
cell[1])

# Final check to see if the room is clean
if all_clean():
    print("Room is clean!") else:
print("Some cells are still dirty.")

```

OUTPUT :

```
Moved to (0,0)
Cleaned cell (0,0)
Moved to (0,1)
Moved to (1,1)
Cleaned cell (1,1)
Moved to (1,0)
Cleaned cell (1,0)
Room is clean!
```

Program 2: Implement 8-puzzle **ALGORITHM:**

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8 - Puzzle Problem

→ Algorithm:

- 1) Initialize the board, start with the initial state where pieces are placed randomly.
- 2) Store the initial state in a queue and keep a visited array to check if the sequence has occurred or not, we will use BFS here.
- 3) Until the queue is empty:
 - a) If we reach the final state, return else, we try to move the blank piece in a valid place by doing a valid move. A move is valid if the sequence hasn't occurred before and we are moving inside the box.
 - b) We add the next state to the queue and keep moving until we find the solution.

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→ Output: 2 moves

1) Best Case
Initial state =

1	2	3
4	5	6
0	7	8

Solution found in 2 moves. Right → Right

2) Average case =

1	0	3
4	5	6
7	8	2

R → D → D → L → U → R → U → L → D → D → R
Solution found in 11 moves

3) Worst case =

1	0	4
3	5	6
7	8	2

No solution exists (Solved in 156 moves)

CODE:

```
from collections import deque
import copy
```

```
# Define the goal state
GOAL_STATE = [[1, 2, 3],
               [4, 5, 6],
               [7, 8, 0]]
```

```
# Directions for moving the blank tile
DIRECTIONS = {
    'Up': (-1, 0),
    'Down': (1, 0),
    'Left': (0, -1),
    'Right': (0, 1)}
```

```

}

def find_blank(state):
    for i in range(3):
        for j in range(3):
            if state[i][j] == 0:
                return i, j

def is_valid(x, y):
    return 0 <= x < 3 and 0 <= y < 3

def get_neighbors(state):
    neighbors = []
    x, y = find_blank(state)

    for move, (dx, dy) in DIRECTIONS.items():
        new_x, new_y = x + dx, y + dy
        if is_valid(new_x, new_y):
            new_state = copy.deepcopy(state)          # Swap blank with adjacent tile
            new_state[x][y], new_state[new_x][new_y] = new_state[new_x][new_y], new_state[x][y]
            neighbors.append((move, new_state))      return neighbors

def bfs(start_state):
    queue =
    deque([(start_state, [])])      visited
    = set()

    while queue:
        current_state, path = queue.popleft()      state_tuple
        = tuple(tuple(row) for row in current_state)

        if current_state == GOAL_STATE:
            return path # Return the solution if we reach the goal state

        if state_tuple in visited:
            continue      visited.add(state_tuple)
        for move, neighbor in
        get_neighbors(current_state):
            queue.append((neighbor, path + [move]))

# Example usage
start_state = [[1, 2, 3],
               [0, 4, 6],
               [7, 5, 8]]

```

```
solution = bfs(start_state)

# Since we removed "no solution" handling, it will keep exploring until it finds the solution
if solution:
    print("Solution found in", len(solution), "moves:")
    print(" -> ".join(solution))
```

OUTPUT:

```
Solution found in 3 moves:
[1, 2, 3]
[0, 4, 6]
[7, 5, 8]
-----
[1, 2, 3]
[4, 0, 6]
[7, 5, 8]
-----
[1, 2, 3]
[4, 5, 6]
[7, 0, 8]
-----
[1, 2, 3]
[4, 5, 6]
[7, 8, 0]
-----
```

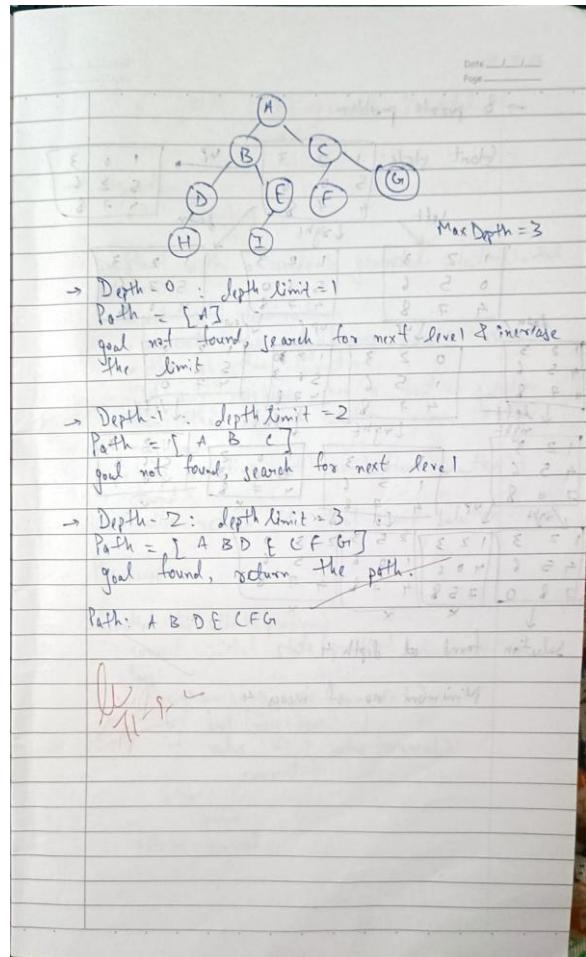
Program 3: Implement IDDFS

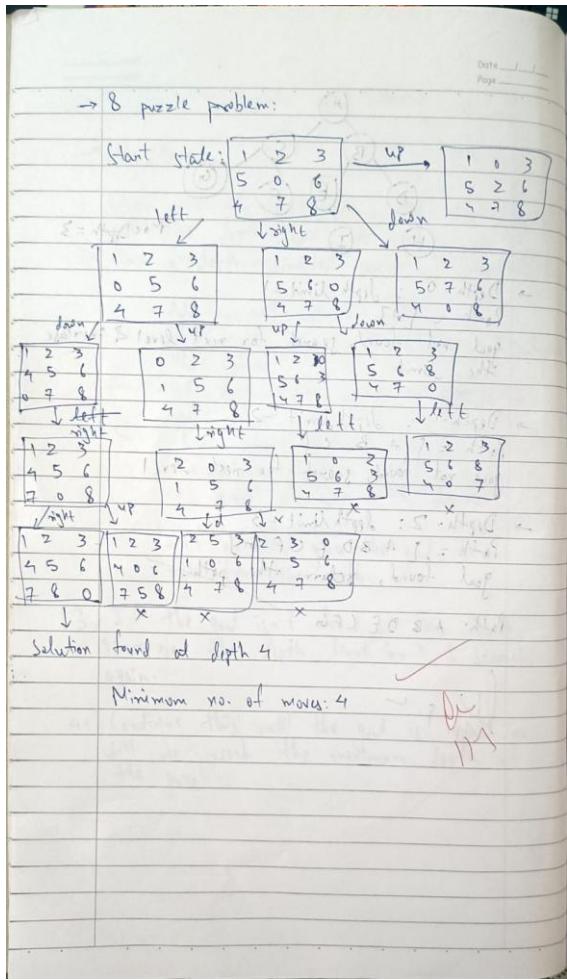
ALGORITHM :

8-Puzzle using IDDFS (Right)

→ Algorithm:

- Start with the root node as the starting point, set the depth-limit to zero.
- Run a depth-limited search with current limit:
 - Add current node to path
 - If current node is the goal, stop & return the path.
 - If depth limit reaches 0, remove this node from path & return failure. (not found at this level).
 - Else for children of this node:
 - use recursion with dep-th-1.
 - If no child gives the goal, remove this node from the path.
- If the goal isn't found at this depth, increase the depth limit by 1 & search again.
- Continue this until the goal is found or till we reach the maximum depth of the graph.





CODE :

```
from collections import deque
```

Directions for movement

MOVES = {

'Up': -3,

'Down': 3,

'Left': -1,

'Right': 1

1

```
# Define the goal state
```

GOAL STATE = (1, 2, 3)

4 5 6

7 8

7, 8, 9)

```
# Valid indices for moves def  
valid_moves(indices):
```

valid_moves(index):

```

moves = []    row, col =
divmod(index, 3)

    if row > 0: moves.append('Up')
    if row < 2: moves.append('Down')
    if col > 0: moves.append('Left')    if
    col < 2: moves.append('Right')

return moves

# Apply move to a state def
apply_move(state, move):
    idx = state.index(0)
    new_idx = idx + MOVES[move]

    # Special case for left/right edge wrapping
    if move == 'Left' and idx % 3 == 0:
        return None    if move == 'Right'
    and idx % 3 == 2:
        return None

    state = list(state)    state[idx], state[new_idx] =
    state[new_idx], state[idx]    return tuple(state)

# DFS with depth limit def
dls(state, depth, visited, path):
    if state == GOAL_STATE:
        return path

    if depth == 0:
        return None

    visited.add(state)    for move in
    valid_moves(state.index(0)):      next_state =
    apply_move(state, move)    if next_state
    and next_state not in visited:
        result = dls(next_state, depth - 1, visited.copy(), path + [(move, next_state)])
    if result:            return result    return None

# IDDFS main function def
iddfs(start_state, max_depth=50):
    for depth in range(max_depth):

```

```

    print(f"\n--- Iteration {depth + 1}: Depth Limit = {depth} ---")
visited = set()      path = dls(start_state, depth, visited, [])
if path is not None:
    return path
return None

# Function to print the puzzle state in a readable format
def print_state(state):
    for i in range(0, 9, 3):
        print(state[i:i+3])
        print()

# Example usage if
__name__ == '__main__':
    start = (1, 2, 3,
4, 5, 6,
0, 7, 8)

    print("Initial State:")
    print_state(start)

    solution = iddfs(start)
if solution:
    print(f"Solution found in {len(solution)} moves:")
    current_state = start
    for move, state in solution:
        print(f"Move: {move}")
        print_state(state)
        current_state = state
    else:
        print("No solution found.")

```

OUTPUT :

```
Initial State:  
(1, 2, 3)  
(4, 5, 6)  
(0, 7, 8)  
  
--- Iteration 1: Depth Limit = 0 ---  
  
--- Iteration 2: Depth Limit = 1 ---  
  
--- Iteration 3: Depth Limit = 2 ---  
Solution found in 2 moves:  
Move: Right  
(1, 2, 3)  
(4, 5, 6)  
(7, 0, 8)  
  
Move: Right  
(1, 2, 3)  
(4, 5, 6)  
(7, 8, 0)
```

Program 4: Implement Hill Climbing & Simulated Annealing

ALGORITHM:

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Hill Climbing and Simulated Annealing

→ Algorithm:

- Hill Climbing

is Start with a randomly generated solution (initial solution).

repeat until termination:

- Generate the neighbouring solution using the objective function.
- If any neighbour has a better solution than the current solution, move to that neighbour.
- Keep repeating until no better solution is found.
- Finally return the best found solution.

Pseudocode

```

function hillClimb(problem):
    current = initial-state(problem)
    loop:
        neighbours = generate(current)
        b = best(neighbours)
        if value(b) > value(current):
            current = b
        else:
            break
    return current

```

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N Queens using Hill Climb

1. Start with a random board.
2. Generate neighbours by moving a queen to every other row.
3. Choose the neighbour with the least no. of pair of queens attacking each other.
4. Move to the best neighbour if it exists else stop.
5. Continue until we reach optimal solution.
6. Return the best found solution.

→ Output:

Initial board:

Q	.	.	.
.	Q	.	.
.	.	Q	.
.	.	.	Q

Move to board with 1 attack:

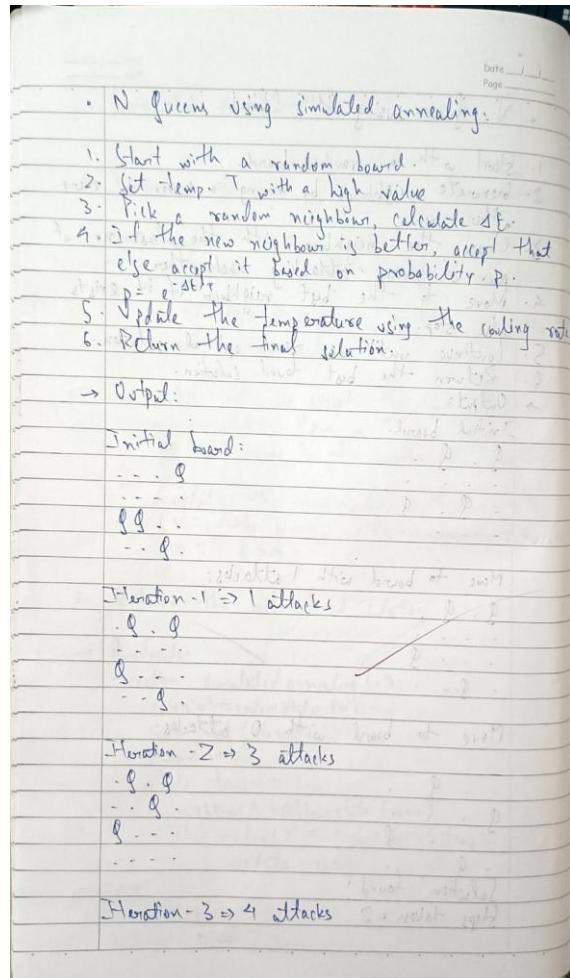
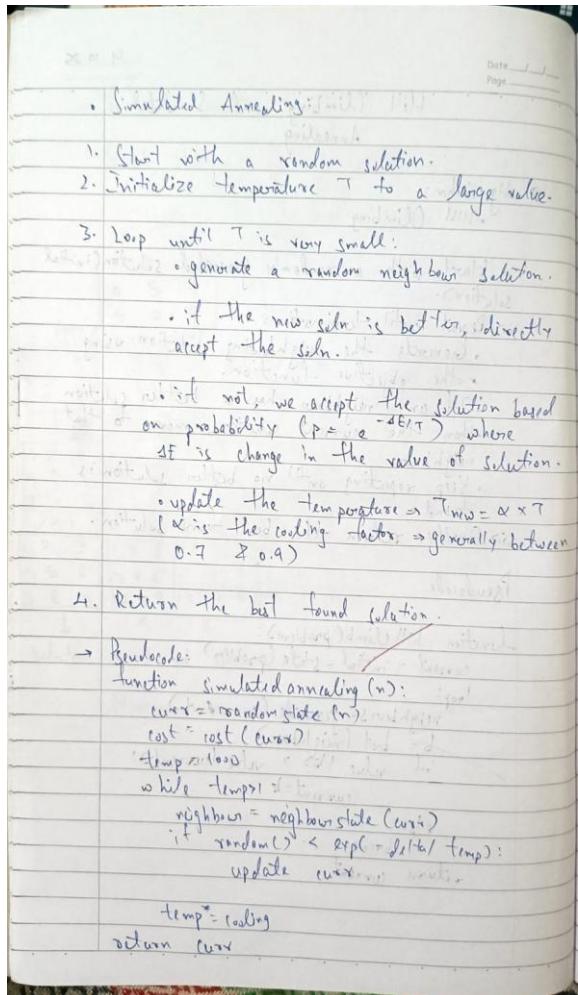
Q	.	.	.
.	Q	.	.
.	.	Q	.
.	.	.	Q

Move to board with 0 attacks:

Q	.	.	.
.	Q	.	.
.	.	Q	.
.	.	.	Q

Solution found!

Steps taken = 2



CODE (Hill Climbing) :

```

import random
def heuristic(board):
    h = 0
    n = len(board)
    for i in range(n):
        for j in range(i+1, n):
            if board[i] == board[j] or abs(board[i]-board[j]) == abs(i-j):
                h += 1
    return h
  
```

```

def hill_climbing_restart(initial_board,
                           max_restarts=100):
    N = len(initial_board)
    board = [x-1 for x in initial_board] # 0-based
    h = heuristic(board)
  
```

```

    restart_count = 0
    while h != 0 and restart_count < max_restarts:
        steps = 0
        while True:
            best_board = board[:]
            best_h = h
  
```

```

for col in range(N):           for row in
range(N):           if row != board[col]:
neighbor = board[:]
neighbor[col] = row           h_neighbor
= heuristic(neighbor)         if
h_neighbor < best_h:
best_board = neighbor         best_h
= h_neighbor     steps += 1     if
best_h >= h: # stuck      break
board = best_board     h = best_h     if
h == 0:           break     if h == 0:
print(f'Solution found after {restart_count} restarts and {steps} steps.')
break
# Random restart    board = [random.randint(0,
N-1) for _ in range(N)]    h = heuristic(board)
restart_count += 1

return [x+1 for x in board], h

# User input
N = int(input("Enter number of queens (N): ")) print(f'Enter the initial
positions of {N} queens (row numbers 1 to {N}):') initial_board =
list(map(int, input().split()))

solution, h_val =
hill_climbing_restart(initial_board) print("Final
board:", solution) print("Heuristic H =", h_val)

```

OUTPUT (Hill Climbing) :

```

Enter number of queens (N): 4
Enter the initial positions of 4 queens (row numbers 1 to 4):
3 4 1 2
Solution found after 0 restarts and 3 steps.
Final board: [2, 4, 1, 3]
Heuristic H = 0

==== Code Execution Successful ====

```

CODE (Simulated Annealing):

```

from datetime import datetime
import random, time, math
from copy import deepcopy, copy
import decimal

```

```

class Board:    def __init__(self,
queen_count=4):
    self.queen_count = queen_count
    self.reset()

    def reset(self):
        self.queens = [-1 for i in range(0, self.queen_count)]

        for i in range(0, self.queen_count):
            self.queens[i] = random.randint(0, self.queen_count - 1)
        # self.queens[row] = column

    def calculateCost(self):
        threat = 0

        for queen in range(0, self.queen_count):
            for
next_queen in range(queen+1, self.queen_count):
                if self.queens[queen] == self.queens[next_queen] or abs(queen - next_queen) ==
abs(self.queens[queen] - self.queens[next_queen]):
                    threat += 1

        return threat

    @staticmethod    def
calculateCostWithQueens(queens):
    threat = 0
    queen_count = len(queens)

    for queen in range(0, queen_count):
        for
next_queen in range(queen+1, queen_count):
            if queens[queen] == queens[next_queen] or abs(queen - next_queen) ==
abs(queens[queen] - queens[next_queen]):
                threat += 1

    return threat

    @staticmethod
def toString(queens):
    board_string = ""

    for row, col in enumerate(queens):
        board_string += "(%s, %s)\n" % (row, col)

```

```

    return board_string

    def getLowerCostBoard(self):
displacement_count = 0      temp_queens =
self.queens      lowest_cost =
self.calculateCost(temp_queens)

        for i in range(0, self.queen_count):
            temp_queens[i] = (temp_queens[i] + 1) % (self.queen_count - 1)

        for j in range(queen+1, self.queen_count):
            temp_queens[j] = (temp_queens[j] + 1) % (self.queen_count - 1)

    def __str__(self):
board_string = ""

        for row, col in enumerate(self.queens):
            board_string += "(%s, %s)\n" % (row, col)

    return board_string

class SimulatedAnnealing:
def __init__(self, board):
self.elapsedTime = 0;
self.board = board
self.temperature = 4000
self.sch = 0.99
self.startTime =
datetime.now()

    def run(self):
        board = self.board
board_queens = self.board.queens[:]
solutionFound = False

        for k in range(0, 170000):
            self.temperature *= self.sch
board.reset()          successor_queens =
board.queens[:]
            dw = Board.calculateCostWithQueens(successor_queens) -
Board.calculateCostWithQueens(board_queens)      exp =
decimal.Decimal(decimal.Decimal(math.e) **) (decimal.Decimal(-dw) *

```

```

decimal.Decimal(self.temperature)))

    if dw > 0 or random.uniform(0, 1) < exp:
board_queens = successor_queens[:]

    if Board.calculateCostWithQueens(board_queens) == 0:
print("Solution:")      print(Board.toString(board_queens))
self.elapsedTime = self.getElapsedTime()      print("Success,
Elapsed Time: %sms" % (str(self.elapsedTime)))      solutionFound
= True      break

if solutionFound == False:
    self.elapsedTime = self.getElapsedTime()      print("Unsuccessful,
Elapsed Time: %sms" % (str(self.elapsedTime)))

return self.elapsedTime

def getElapsedTime(self):      endTime = datetime.now()
elapsedTime = (endTime - self.startTime).microseconds / 1000
return elapsedTime

```

```

if __name__ == '__main__':
    board = Board()
print("Board:")  print(board)
SimulatedAnnealing(board).run()

```

OUTPUT (Simulated Annealing):

Board:

(0, 1)
(1, 0)
(2, 1)
(3, 3)

Solution:

(0, 2)
(1, 0)
(2, 3)
(3, 1)

Success, Elapsed Time: 7.9ms

Program 5: A* Algorithm

ALGORITHM :

8 - Puzzle using A*

→ Pseudocode:

1. Initialize
Open list

- Start with the defined goal state.
- Initialize open list with a priority queue with start state.
- Also initialize an empty closed list.
- Keep solution with least $f(n)$.

```

func Astart(start, goal):
    open ← priority queue ordered by f-g
    g[start] = 0
    p[start] = None
    while open is not empty:
        curNode ← pop(open)
        if curNode == goal:
            return curNode
        for each n of curNode:
            new ← g[curNode] + 1
            if n not in g or new < g[n]:
                g[n] ← new
                f ← new + h(n)
                push(open, n, f)
                parent[n] = curNode
    return failure
  
```

→ Output:
Solution found in 18 moves

1	2	3		4	5	6		7	8	9
0	4	6		3	5	1		2	7	8
5	8	7		4	3	6		2	1	9
↓				↓				↓		
1	2	3		4	5	6		7	8	9
4	0	6		3	5	1		2	7	8
5	8	7		2	3	6		1	4	9
↓				↓				↓		
1	2	3		4	6	8		5	7	9
4	5	7		3	2	8		6	1	0
0	5	9		↓				0	7	3
↓				1	2	3		4	5	6
8	0	6		5	3	7		2	1	9
4	5	7		2	1	3		4	6	8
↓				↓				↓		
1	2	3		4	5	6		7	8	9
8	0	6		3	2	7		1	4	9
4	5	7		2	1	3		4	6	8
↓				↓				↓		
1	2	3		4	6	8		5	7	9
8	0	6		3	2	7		1	4	9
4	5	7		2	1	3		4	6	8
↓				↓				↓		
1	2	3		4	8	5		7	6	9
0	7	6		3	2	1		4	5	8
4	5	9		2	1	3		4	6	7
↓				↓				↓		
1	2	3		4	5	6		7	8	9
0	8	5		3	2	1		4	6	7
4	7	6		2	1	3		4	5	8
↓				↓				↓		
1	2	3		4	5	6		7	8	9

	1	2	3	
	8	0	5	
	4	7	6	
	↓			
	1	2	3	
	0	8	5	
	4	7	6	
	↓			
	1	2	3	
	4	8	5	
	7	0	6	
	↓			
	1	2	3	
	4	5	6	
	8	7	0	
	↓			
	1	2	3	
	4	5	6	
	7	8	0	goal state

CODE :

```

import heapq

class PuzzleState:    def __init__(self, board, parent=None,
move="", depth=0, cost=0):
    self.board = board
    self.parent = parent
    self.move = move
    self.depth = depth
    self.cost = cost

    def __lt__(self, other):
        return self.cost < other.cost

    def blank_pos(self):
        return self.board.index(0)

```

```

def expand(self):
    b = self.blank_pos()
    row, col = divmod(b, 3)
    dirs = {
        "Up": (row - 1, col),
        "Down": (row + 1, col),
        "Left": (row, col - 1),
        "Right": (row, col + 1)
    }
    nxt = [] for mv, (r, c) in dirs.items(): if 0 <= r < 3 and 0 <= c < 3:
        idx = r * 3 + c nb = self.board[:]
        nb[b], nb[idx] = nb[idx], nb[b]
        nxt.append(PuzzleState(nb, self, mv, self.depth + 1))
    return nxt

def build_path(self):
    p, node = [], self
    while node:
        p.append((node.move, node.board, node.depth)) node = node.parent return list(reversed(p))

def misplaced_tiles(state, goal):
    return sum(1 for i in range(9) if state.board[i] not in (0, goal[i]))

def manhattan_distance(state, goal):
    d = 0 for i, v in enumerate(state.board): if v != 0:
        r1, c1 = divmod(i, 3) r2,
        c2 = divmod(goal.index(v), 3) d += abs(r1 - r2) + abs(c1 - c2) return d

def a_star(start, goal, h):
    opened = [] closed = set() nodes = 0 s = PuzzleState(start)
    s.cost = h(s, goal)
    heapq.heappush(opened, (s.cost, nodes, s))

```

```

while opened:      cur =
    heapq.heappop(opened)
    nodes += 1

    if cur.board == goal:
        return cur.build_path(), nodes

    closed.add(tuple(cur.board))

    for nxt in cur.expand():
        if tuple(nxt.board) in closed:
            continue      nxt.cost =
        nxt.depth + h(nxt, goal)
        heapq.heappush(opened, nxt)

    return None, nodes

def print_solution(path, total_nodes):
    print("Steps:\n")
    for mv, st, d in path:
        label = "Start" if mv == "" else f"Move {mv}"
        print(f"{label} | Depth {d}")
        for i in range(0, 9, 3):
            print(" ".join(str(x) if x != 0 else " " for x in st[i:i+3]))
    print()
    print(f"Total Moves: {len(path)-1}")
    print(f"Nodes Expanded: {total_nodes}")

if __name__ == "__main__":
    start = [1, 2, 3,
             4, 0, 6,
             7, 5, 8]

    goal = [1, 2, 3,
            4, 5, 6,
            7, 8, 0]

    print("A* (Misplaced Tiles)\n")  sol1, n1 =
    a_star(start, goal, misplaced_tiles)  if sol1:
        print_solution(sol1, n1)
    else:
        print("No solution.")

```

```

print("\nA* (Manhattan Distance)\n")    sol2, n2
= a_star(start, goal, manhattan_distance)  if sol2:
    print_solution(sol2, n2)
else:
    print("No solution.")

```

OUTPUT :

```

A* (Misplaced Tiles)

Steps:

Start | Depth 0
1 2 3
4   6
7 5 8

Move Down | Depth 1
1 2 3
4 5 6
7   8

Move Right | Depth 2
1 2 3
4 5 6
7 8

Total Moves: 2
Nodes Expanded: 3

A* (Manhattan Distance)

Steps:

Start | Depth 0
1 2 3
4   6
7 5 8

Move Down | Depth 1
1 2 3
4 5 6
7   8

Move Right | Depth 2
1 2 3
4 5 6
7 8

Total Moves: 2
Nodes Expanded: 3

```

Program 6: Propositional Logic

ALGORITHM :

<p style="text-align: center;">Propositional Logic</p> <p>→ Pseudocode</p> <pre> function TT-Entails(KB, α) inputs: KB (knowledge base, a sentence in propositional logic), α (query, a sentence in propositional logic) symbols → a list of proposition symbols in KB and α solution TT-Check-All(KB, α, symbols, { }) </pre> <p>function TT-Check-All(KB, α, symbols, model)</p> <pre> if EMPTY? (symbols) then if P1-TRUE? (KB, model) then return P1-TRUE? (α, model) else return true // when KB false, always return true else do P1 ← FIRST(symbols) rest ← REST(symbols) return (TT-Check-All(KB, α, rest, model ∪ {P1 = true})) ∨ (TT-Check-All(KB, α, rest, model ∪ {P1 = false})) </pre>	<p>Date 16/10/25 Page _____</p> <p>$\neg(\neg q \rightarrow p) \rightarrow p \rightarrow \neg q$</p> <p>$\neg q \wedge p$</p> <ul style="list-style-type: none"> Truth Table (for different KB values) <table border="1"> <thead> <tr> <th>P</th> <th>Q</th> <th>R</th> <th>$\neg q$</th> <th>$q \rightarrow p$</th> <th>$p \rightarrow q$</th> <th>$\neg q \wedge p$</th> <th>$\neg q \vee p$</th> </tr> </thead> <tbody> <tr><td>f</td><td>t</td><td>f</td><td>t</td><td>t</td><td>t</td><td>f</td><td>t</td></tr> <tr><td>f</td><td>f</td><td>t</td><td>t</td><td>t</td><td>t</td><td>f</td><td>t</td></tr> <tr><td>f</td><td>t</td><td>f</td><td>f</td><td>t</td><td>t</td><td>f</td><td>t</td></tr> <tr><td>t</td><td>f</td><td>f</td><td>t</td><td>f</td><td>t</td><td>t</td><td>t</td></tr> <tr><td>t</td><td>t</td><td>f</td><td>f</td><td>f</td><td>t</td><td>f</td><td>t</td></tr> <tr><td>t</td><td>f</td><td>t</td><td>t</td><td>t</td><td>t</td><td>f</td><td>t</td></tr> <tr><td>t</td><td>t</td><td>t</td><td>t</td><td>t</td><td>t</td><td>t</td><td>t</td></tr> <tr><td>t</td><td>t</td><td>f</td><td>t</td><td>t</td><td>f</td><td>t</td><td>t</td></tr> </tbody> </table> <p>⇒ Does KB entail P</p> <table border="1"> <thead> <tr> <th>P</th> <th>KB</th> </tr> </thead> <tbody> <tr><td>f</td><td>f</td></tr> <tr><td>t</td><td>t</td></tr> <tr><td>t</td><td>f</td></tr> <tr><td>f</td><td>f</td></tr> <tr><td>t</td><td>t</td></tr> <tr><td>t</td><td>f</td></tr> <tr><td>f</td><td>t</td></tr> <tr><td>f</td><td>f</td></tr> </tbody> </table> <p>• When ever KB is true, P is also true.</p> <p>⇒ If KB entails P</p>	P	Q	R	$\neg q$	$q \rightarrow p$	$p \rightarrow q$	$\neg q \wedge p$	$\neg q \vee p$	f	t	f	t	t	t	f	t	f	f	t	t	t	t	f	t	f	t	f	f	t	t	f	t	t	f	f	t	f	t	t	t	t	t	f	f	f	t	f	t	t	f	t	t	t	t	f	t	t	t	t	t	t	t	t	t	t	t	f	t	t	f	t	t	P	KB	f	f	t	t	t	f	f	f	t	t	t	f	f	t	f	f
P	Q	R	$\neg q$	$q \rightarrow p$	$p \rightarrow q$	$\neg q \wedge p$	$\neg q \vee p$																																																																																				
f	t	f	t	t	t	f	t																																																																																				
f	f	t	t	t	t	f	t																																																																																				
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t	f	f	t	f	t	t	t																																																																																				
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Date _____
Page _____

→ Does KB entail $R \Rightarrow P$?

R	P	$R \Rightarrow P$	KB
f	f	t	f
t	f	f	t
f	t	t	f
t	t	t	f
f	t	t	t
t	f	t	f
t	t	t	f

∴ We can see that when KB is true $R \Rightarrow P$ is false.

→ Does KB entail $Q \Rightarrow R$?

$Q \Rightarrow R$	KB
f	f
t	t
f	f
t	f
t	t
f	f
t	f

Whenever KB is true, $Q \Rightarrow R$ is also true
 \therefore KB entails $Q \Rightarrow R$

CODE :

```
import itertools
```

```
# Logical operations  
def implies(a, b):  
    return not a or b
```

```
def or_operator(a, b):  
    return a or b
```

```
def not_operator(a):  
    return not a
```

```
# Constructing the truth table  
def construct_truth_table():
```

```

truth_values = [True, False]
truth_table = []

# Generate all combinations for Q, P, R for values
in itertools.product(truth_values, repeat=3):
    Q, P, R = values

    # Evaluate KB sentences      q_implies_p =
    implies(Q, P)      p_implies_not_q = implies(P,
    not_operator(Q))      q_or_r = or_operator(Q, R)

    # KB = (Q → P) ∧ (P → ¬Q) ∧ (Q ∨ R)
    kb_is_true = q_implies_p and p_implies_not_q and q_or_r

    # Entailment expressions
    entail_r = R      entail_r_implies_p =
    implies(R, P)      entail_q_implies_r =
    implies(Q, R)

    # Add row to truth table      truth_table.append((
    Q, P, R,      q_implies_p, p_implies_not_q, q_or_r,
    kb_is_true,      entail_r, entail_r_implies_p,
    entail_q_implies_r
    ))
return truth_table

# Print the truth table nicely def
print_truth_table(truth_table):
    header = [
        "Q", "P", "R",
        "Q → P", "P → ¬Q", "Q ∨ R",
        "KB (all true)",
        "R", "R → P", "Q → R"
    ]
    print(" | ".join(header))
    print("-" * 85)

    for row in truth_table:
        # Format True/False as T/F for compactness
        formatted_row = [("T" if val else "F") for val in row]
        print(" | ".join(formatted_row))

```

```

# Generate and print truth table
truth_table = construct_truth_table()
print(truth_table)

# Additionally, check entailment by verifying if for all models where KB is true, entailment is true

def check_entailment(truth_table,
                     entailment_index):
    for row in truth_table:
        kb_true = row[6]      entailment_val =
        row[entailment_index]      if kb_true and not
        entailment_val:
            return False
    return True

print("\nEntailment Results:") print(f"Does KB entail R?
{check_entailment(truth_table, 7)}") print(f"Does KB entail R → P?
{check_entailment(truth_table, 8)}") print(f"Does KB entail Q →
R? {check_entailment(truth_table, 9)}")

```

OUTPUT :

Q	P	R	$Q \rightarrow P$	$P \rightarrow \neg Q$	$Q \vee R$	KB (all true)	R	$R \rightarrow P$	$Q \rightarrow R$
T	T	T	T	F	T	F	T	T	T
T	T	F	T	F	T	F	F	T	F
T	F	T	F	T	T	F	T	F	T
T	F	F	F	T	T	F	F	T	F
F	T	T	T	T	T	T	T	T	T
F	T	F	T	T	F	F	F	T	T
F	F	T	T	T	T	T	T	F	T
F	F	F	T	T	F	F	F	T	T

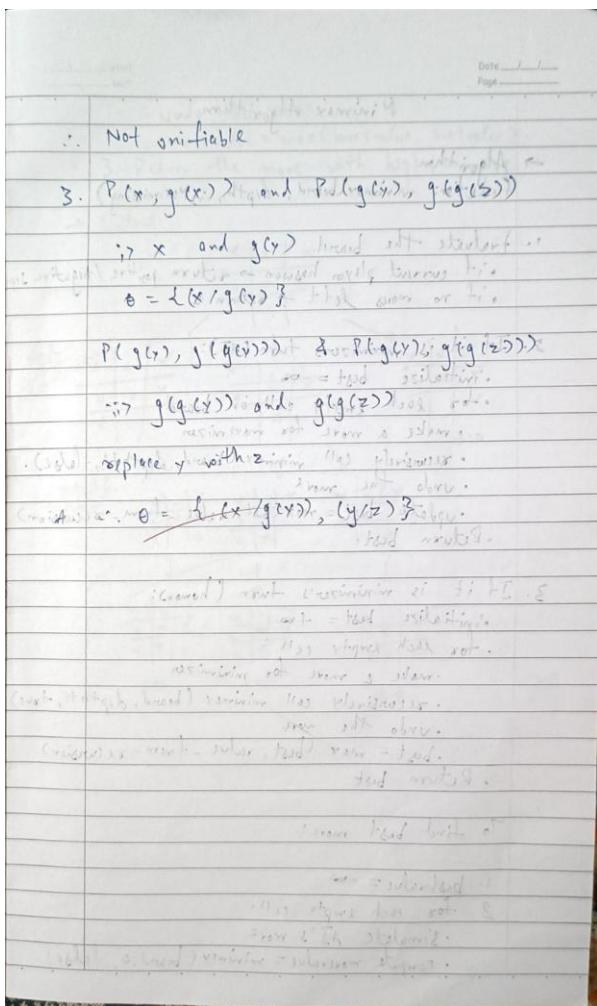
T	T	T	T	F	T	F	T	T	T
T	T	F	T	F	T	F	F	T	F
T	F	T	F	T	T	F	T	F	T
T	F	F	F	T	T	F	F	T	F
F	T	T	T	T	T	T	T	T	T
F	T	F	T	T	F	F	F	T	T
F	F	T	T	T	T	T	T	F	T
F	F	F	T	T	F	F	F	T	T

Entailment Results:

Does KB entail R? True
 Does KB entail $R \rightarrow P$? False
 Does KB entail $Q \rightarrow R$? True

Program 7: Unification Algorithm:

Date <u>30/10/26</u> Page _____	Date <u>30/10/26</u> Page _____
<p style="text-align: center;"><u>Unification</u></p> <p>→ Algorithm (contd.)</p> <p>Unify (φ_1, φ_2)</p> <p>$(C(x)) \rightarrow \text{true } (\varphi)$</p> <p>1. If $\varphi_1 \neq \varphi_2$ is a variable or constant, then:</p> <ul style="list-style-type: none"> a) if $\varphi_1 \neq \varphi_2$ are identical, return NIL. b) else if φ_1 is a variable: <ul style="list-style-type: none"> if φ_1 occurs in φ_2, return FAILURE. else return $\{\varphi_2 / \varphi_1\}$. c) else if φ_2 is a variable: <ul style="list-style-type: none"> if φ_2 occurs in φ_1, return FAILURE. else return $\{\varphi_1 / \varphi_2\}$. d) else return FAILURE. <p>2. If the initial predicate symbol in φ_1 and φ_2 isn't same, return FAILURE.</p> <p>3. If φ_1, φ_2 have diff no. of arguments, return FAILURE.</p> <p>4. Set substitution $\text{set}(\text{SUBST}) = \text{NIL}$. $\theta = \{\}$</p> <p>5. For i=1 to no. of elements in φ_1, φ_2: <ul style="list-style-type: none"> a) call unify function with ith element of both φ_1, φ_2, put result in S. <ul style="list-style-type: none"> b) if $S = \text{failure}$ then return FAILURE. c) if $S \neq \text{NIL}$, then do: <ul style="list-style-type: none"> Apply S to remainder of both φ_1, φ_2. $\Rightarrow \text{SUBST} = \text{APPEND}(S, \text{SUBST})$ <p>6. Return SUBST</p> </p>	<p>→ $P(f(x), g(y), z)$</p> <p>$P(f(g(z)), g(f(x)), f(a))$</p> <p>$\Rightarrow f(x) \text{ and } f(g(z))$</p> <p>$\Rightarrow x \rightarrow g(z)$ (as both have some predicates)</p> <p>∴ we replace x with $g(z)$:</p> <p>$\theta = \{x/g(z)\}$</p> <p>$P(f(g(z)), g(f(y)), z)$ and $P(f(g(z)), g(f(y)), f(a))$</p> <p>$\Rightarrow g(z) \text{ and } g(f(y)) \text{ or }$</p> <p>$y \rightarrow f(a)$ (as both have some predicates)</p> <p>$\theta = \{x/g(z), y/f(a)\}$</p> <p>$P(f(g(z)), g(f(a)), f(a))$</p> <p>$P(f(g(z)), g(f(a)), f(a)) \text{ or }$</p> <p>$A - \theta = \{x/g(z), y/f(a)\}$</p> <p>2. $g(x, f(x))$ and $g(f(y), y)$ for no. 2</p> <p>→ $\theta = \{x/y\}$ (as both have same predicates)</p> <p>$\Rightarrow x/y \text{ and } f(y) = y$ (as both have same predicates)</p> <p>$\Rightarrow f(y) = y$ (as both have same predicates)</p> <p>$\therefore \theta = \{x/y\}$</p> <p>$g(f(y), f(f(y)))$ and $g(f(y), y)$</p> <p>$\Rightarrow f(f(y)) \text{ and } y$ (as both have same predicates)</p> <p>$\Rightarrow y \text{ occurs on both sides}$</p>



CODE :

```

class Variable: def
  __init__(self, name):
    self.name = name

  def __eq__(self, other):
    return isinstance(other, Variable) and self.name == other.name

  def __hash__(self):
    return hash(self.name)

  def __repr__(self):
    return self.name

class Constant: def
  __init__(self, value):
    self.value = value
  
```

```

def __eq__(self, other):
    return isinstance(other, Constant) and self.value == other.value

def __hash__(self):
    return hash(self.value)

def __repr__(self):
    return str(self.value)

class Function:
    def __init__(self, name, args):
        self.name = name
        self.args = args

    def __eq__(self, other):
        return (isinstance(other, Function) and
                self.name == other.name and len(self.args) ==
                len(other.args) and all(a == b for a, b in
                zip(self.args, other.args)))

    def __hash__(self):
        return hash((self.name, tuple(self.args)))

    def __repr__(self):
        return f'{self.name}({", ".join(map(str, self.args))})'

def unify(term1, term2, substitution=None):
    """
    Unifies two first-order logic terms and returns the MGU (substitution)
    or None if unification is not possible.

    """
    if substitution is None:
        substitution = {}

    # Apply existing substitutions
    term1 = substitute(term1, substitution)
    term2 = substitute(term2, substitution)

    if term1 == term2:
        return substitution
    elif isinstance(term1, Variable):
        return unify_var(term1, term2, substitution)
    elif isinstance(term2, Variable):

```

```

        return unify_var(term2, term1, substitution)  elif
isinstance(term1, Function) and isinstance(term2, Function):      if
term1.name != term2.name or len(term1.args) != len(term2.args):
        return None # Function symbols or arity don't
match      for arg1, arg2 in zip(term1.args, term2.args):
substitution = unify(arg1, arg2, substitution)      if
substitution is None:
        return None # Sub-unification
failed      return substitution  else:
        return None # Cannot unify different types (e.g., Constant and Function)

def unify_var(var, x, substitution):
    """Handles unification when one of the terms is a variable."""
if var in substitution:
    return unify(substitution[var], x, substitution)
elif x in substitution:
    return unify(var, substitution[x],
substitution)  elif occurs_check(var, x,
substitution):      return None # Occurs check
fails  else:
    substitution[var] = x
return substitution

def occurs_check(var, term, substitution):
    """Checks if a variable occurs within a term, preventing infinite
substitutions."""
    term = substitute(term, substitution) # Apply current
substitutions  if var == term:      return True  elif isinstance(term, Function):
        return any(occurs_check(var, arg, substitution) for arg in term.args)
return False

def substitute(term, substitution):
    """Applies a given substitution to a term."""
if isinstance(term, Variable):
    return substitution.get(term, term)
elif isinstance(term, Function):
    return Function(term.name, [substitute(arg, substitution) for arg in term.args])
return term

# Example Usage: if
__name__ == "__main__":
    # Define terms
    x, y, z = Variable('x'), Variable('y'), Variable('z')
    a, b = Constant('a'), Constant('b')  f =

```

```

Function('f', [x, Constant('b')])    g = Function('g',
[Constant('a'), y])    h = Function('h', [z])

print(f"Unify(f(x, b), f(a, y)): {unify(Function('f', [x, b]), Function('f', [a, y]))} ")
print(f"Unify(g(a, y), g(a, b)): {unify(Function('g', [a, y]), Function('g', [a, b]))} ")
print(f"Unify(x, f(x, b)): {unify(x, Function('f', [x, b]))} " ) # Occurs check failure
print(f"Unify(f(x, y), f(a, g(z))): {unify(Function('f', [x, y]), Function('f', [a, Function('g',
[z])]))} ")   print(f"Unify(P(x, A), P(B, y)): {unify(Function('P', [x, Constant('A')]),
Function('P', [Constant('B'), y]))} ")

print("\n--- Your Requested Tests ---")

# 1. p(f(x), g(y), y) and p(f(g(z)), g(f(a)), f(a))  term1_1 =
Function('p', [Function('f', [x]), Function('g', [y]), y])
term1_2 = Function('p', [Function('f', [Function('g', [z])]), Function('g', [Function('f', [a])]),
Function('f', [a])])   print(f"Unify(p(f(x), g(y), y), p(f(g(z)), g(f(a)), f(a))): {unify(term1_1,
term1_2)} ")

# 2. q(x, f(x)) and q(f(y), y)  term2_1 = Function('q', [x,
Function('f', [x])])  term2_2 = Function('q', [Function('f', [y]), y])
print(f"Unify(q(x, f(x)), q(f(y), y)): {unify(term2_1, term2_2)} ")

# 3. p(x, g(x)) and p(g(y), g(g(z)))  term3_1 = Function('p', [x,
Function('g', [x])])  term3_2 = Function('p', [Function('g', [y]), Function('g',
[Function('g', [z])])])   print(f"Unify(p(x, g(x)), p(g(y), g(g(z)))):
{unify(term3_1, term3_2)} ")

```

OUTPUT :

```

Unify(f(x, b), f(a, y)): {x: a, y: b}
Unify(g(a, y), g(a, b)): {y: b}
Unify(x, f(x, b)): None
Unify(f(x, y), f(a, g(z))): {x: a, y: g(z)}
Unify(P(x, A), P(B, y)): {x: B, y: A}

--- Your Requested Tests ---
Unify(p(f(x), g(y), y), p(f(g(z)), g(f(a)), f(a))): {x: g(z), y: f(a)}
Unify(q(x, f(x)), q(f(y), y)): None
Unify(p(x, g(x)), p(g(y), g(g(z)))): {x: g(y), y: z}

```

Program 8: MinMax & AlphaBeta

ALGORITHM :

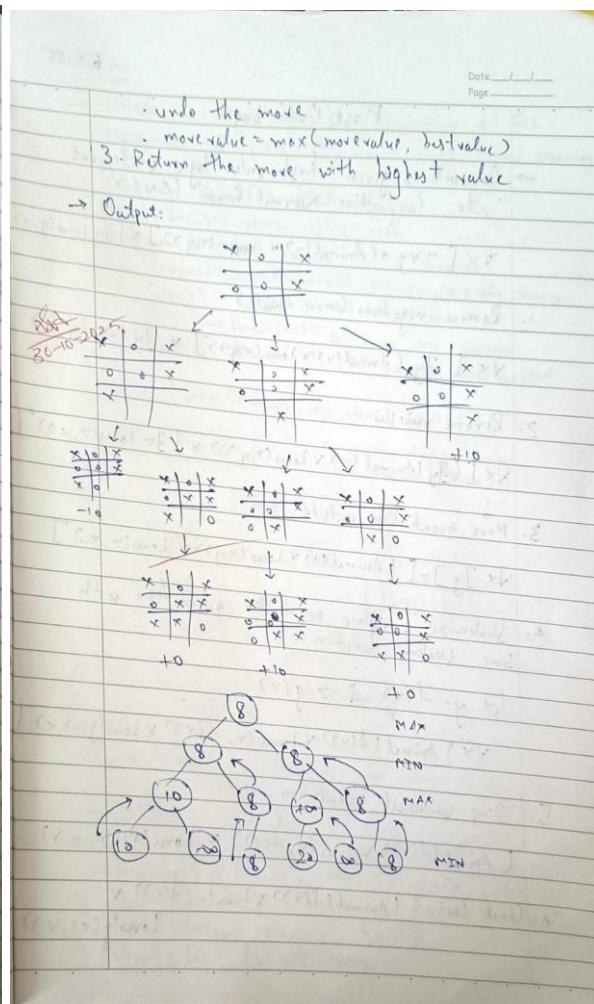
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Minimax Algorithm & Alpha-Beta Pruning

→ **Algorithm**

```

function minimax(board, depth, isMaximizing)
    alphaBeta(state, α, β)
    1. Evaluate the board
        • if current player has won → return positive/negative
        • if no moves left → return 0
    2. If it is maximizer's turn (A):
        • initialize best = -∞
        • for each empty cell on board:
            • make a move for maximizer
            • recursively call minimax (board, depth+1, -isMax)
            • undo the move, if best ≥ β → return best
            • update best = max(best, value - from recursion)
        • Return best. &  $\alpha = \max(\alpha, \text{best})$ 
    3. If it is minimizer's turn (B):
        • initialize best = +∞
        • for each empty cell:
            • make a move for minimizer
            • recursively call minimax (board, depth+1, +isMax)
            • undo the move, if best ≤ α → return best
            • update best = min(best, value - from recursion)
        • Return best &  $\beta = \min(\beta, \text{best})$ 
    To find best move:
    1. bestValue = -∞
    2. for each empty cell:
        • simulate AI's move
        • compute moveValue = minimax (board, 0, -isMax).
  
```



CODE :

```

def alpha_beta(node, depth, alpha, beta, maximizing_player, path):
    # Base case: if node is a leaf (integer), return its value and path
    if isinstance(node, int):
        return node, path

    if maximizing_player:
        value = float('-inf')
        best_path = None
        for i, child in enumerate(node):
            child_value, child_path = alpha_beta(
                child, depth + 1, alpha, beta, False, path + [i]
            )
            if child_value > value:
                value = child_value
                best_path = child_path
            alpha = max(alpha, value)
    else:
        value = float('inf')
        best_path = None
        for i, child in enumerate(node):
            child_value, child_path = alpha_beta(
                child, depth + 1, alpha, beta, True, path + [i]
            )
            if child_value < value:
                value = child_value
                best_path = child_path
            beta = min(beta, value)
    return value, best_path
  
```

```

        if child_value > value:
            value = child_value
            best_path = child_path

    # Artifact '62' removed here
    alpha = max(alpha, value)

    if alpha >= beta:
        print(f" [PRUNE] MAX (Depth {depth}): Alpha ({alpha}) >= Beta ({beta})")
        break

    return value, best_path

else:
    value = float('inf')
    best_path = None

    for i, child in enumerate(node):
        child_value, child_path = alpha_beta(
            child, depth + 1, alpha, beta, True, path + [i]
        )

        if child_value < value:
            value = child_value
            best_path = child_path

    beta = min(beta, value)

    if beta <= alpha:
        print(f" [PRUNE] MIN (Depth {depth}): Beta ({beta}) <= Alpha ({alpha})")
        break

    return value, best_path

if __name__ == "__main__":
    # Tree structure with artifact '63' removed
    tree = [
        [
            [
                [10, 11],
                [9, 12]
            ],
            [
                [14, 15],
                [13, 16]
            ]
        ]
    ]

```

```

        [13, 14]
    ],
],
[
[
    [
        [5, 2],
        [4, 1]
    ],
    [
        [3, 22],
        [20, 21]
    ],
]
]

print("Starting Alpha-Beta Pruning...\n" + "-"*30)

value, best_path = alpha_beta(tree, 0, float('-inf'), float('inf'), True, [])

print("-" * 30)
print(f"FINAL MINIMAX VALUE AT ROOT: {value}")
print(f"BEST PATH INDICES: {best_path}")

```

OUTPUT :

```

Starting Alpha-Beta Pruning...
-----
[PRUNE] MIN (Depth 3): Beta (9) <= Alpha (10)
[PRUNE] MAX (Depth 2): Alpha (14) >= Beta (10)
[PRUNE] MIN (Depth 3): Beta (5) <= Alpha (10)
[PRUNE] MIN (Depth 3): Beta (4) <= Alpha (10)
[PRUNE] MIN (Depth 1): Beta (5) <= Alpha (10)
-----
FINAL MINIMAX VALUE AT ROOT: 10
BEST PATH INDICES: [0, 0, 0, 0]

```

Program 9: Forward Chaining & Conversion to CNF

ALGORITHM :

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First Order Logic

- Convert the given first-order logic statement into Conjunctive Normal Form (CNF)

$$\forall x \exists y \forall z (\text{Animal}(y) \wedge \text{Loves}(x, y)) \vee \exists y \text{Loves}(y, x)$$

- Remove negations (move inside)
$$\forall x \exists y (\text{Animal}(y) \vee \text{Loves}(x, y)) \vee \exists y \text{Loves}(y, x)$$
- Remove variables
$$\forall x (\exists y (\text{Animal}(y) \vee \text{Loves}(x, y))) \vee \exists z \text{Loves}(z, x)$$
- Move quantifiers outside
$$\forall x \exists y \exists z (\text{Animal}(y) \vee \text{Loves}(x, y) \vee \text{Loves}(z, x))$$
- Skeletonize: replace existential quantification with some skeleton function
$$\text{let } f = \lambda(x). y \quad g = \lambda(x). z$$

$$\forall x (\text{Animal}(f(x)) \vee \text{Loves}(x, f(x)) \vee \text{Loves}(g(x), x))$$
- Drop universal quantifier
$$(\text{Animal}(f(x)) \vee \text{Loves}(x, f(x)) \vee \text{Loves}(g(x), x))$$

A. find CNF = $(\text{Animal}(f(x)) \vee \text{Loves}(x, f(x)) \vee \text{Loves}(g(x), x))$

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- Create a knowledge base consisting of FOL statements & prove the query using forward reasoning.
- Knowledge Base (FOL Statements):
 - $\text{Man}(\text{Marcus})$: Marcus is a man.
 - $\text{Pompion}(\text{Marcus})$: Marcus is a pompion.
 - $\forall x (\text{Pompion}(x) \rightarrow \text{Roman}(x))$: all pompions are Romans.
 - $\forall x (\text{Roman}(x) \rightarrow \text{Loyal}(x))$: all Romans are loyal.
 - $\forall x (\text{Man}(x) \rightarrow \text{Person}(x))$: all men are persons.
 - $\forall x (\text{Person}(x) \rightarrow \text{Mortal}(x))$: all persons are mortal.

Query: $\text{Mortal}(\text{Marcus})$

```

graph TD
    ManMarcus[Man(Marcus)] --> MonX[Man(x)]
    MonX --> PersonMarcus[Person(Marcus)]
    PersonMarcus --> MortalMarcus[Mortal(Marcus)]
    PompionMarcus[Pompion(Marcus)] --> PompionX[Man(x)]
    PompionX --> RomanMarcus[Person(Marcus)]
    RomanMarcus --> LoyalMarcus[Loyal(x)]
    LoyalMarcus --> MortalMarcus
  
```

B. Implement unification in first order logic

- OUTPUT:

$\text{Unify}(f(x), f(y))$: $\{x:a, y:b\}$
$\text{Unify}(f(x), f(a, g(z)))$: $\{x:a, y:g(z)\}$
$\text{Unify}(g(f(x)), g(a, b))$: $\{y:b\}$
$\text{Unify}(c, f(x, y))$: None

CODE (Forward Chaining) :

```

import re

def isVariable(x):
    return len(x) == 1 and x.islower() and x.isalpha()

def getAttributes(string):
    expr = r'\([^\)]+\)' matches =
    re.findall(expr, string)
    return matches

def getPredicates(string):
    expr = r'([a-zA-Z~]+)([^&]+)''
    return re.findall(expr, string)
  
```

```

class Fact:    def __init__(self,
expression):
    self.expression = expression.strip()      predicate,
params = self.splitExpression(expression)
self.predicate = predicate      self.params = params

    def splitExpression(self, expression):      predicate =
getPredicates(expression)[0]      params =
getAttributes(expression)[0].strip(')').split(',')      return
[p.strip() for p in params]

    def substitute(self, var_map):
        params = [var_map.get(p, p) for p in self.params]
return Fact(f'{self.predicate}({",".join(params)})')

    def __repr__(self):
return self.expression

class Implication:    def __init__(self,
expression):      self.expression =
expression.strip()      lhs, rhs =
expression.split('=>')      self.lhs =
[Fact(f.strip()) for f in lhs.split('&')]      self.rhs
= Fact(rhs.strip())

```

```

def infer(self, known_facts):
    substitutions = {}

        for fact in self.lhs:      matched =
False      for known in known_facts:
if known.predicate == fact.predicate:
            mapping = {}      for i, param
in enumerate(fact.params):      if
isVariable(param):
                mapping[param] =
known.params[i]      elif param !=
known.params[i]:      break
else:
                substitutions.update(mapping)
                matched = True
break      if not matched:
return None

    return self.rhs.substitute(substitutions)

```

```

class KB:
    def __init__(self):
        self.facts = set()
        self.implications = set()

    def tell(self, expr):
        if '=>' in expr:
            self.implications.add(Implication(expr))
        else:
            self.facts.add(Fact(expr))

    def infer_all(self):
        added = True
        while added:
            added = False
            for rule in self.implications:
                new_fact = rule.infer(self.facts)
                if new_fact and new_fact.expression not in [f.expression for f in self.facts]:
                    print(f"Derived: {new_fact.expression}")
                    self.facts.add(new_fact)
                    added = True

    def ask(self, query):
        print(f"\nQuerying {query}:")
        self.infer_all()
        facts = [f.expression for f in self.facts]
        for f in facts:
            if query in f:
                print(f"Yes, {query.split('(')[1].strip(')')} is {query.split('(')[0]}")
        else:
            print(f"No, cannot infer {query}.")

    def display(self):
        print("\nAll facts in Knowledge Base:")
        for i, f in enumerate(sorted([f.expression for f in self.facts])):
            print(f"\t{i+1}. {f}")

def main():
    kb = KB()
    n = int(input("Enter number of FOL expressions:"))
    print("Enter expressions:")
    for _ in range(n):
        kb.tell(input().strip())

    query = input("Enter query:").strip()
    kb.ask(query)
    kb.display()

```

```
if __name__ == "__main__":
    main()
```

OUTPUT (Forward Chaining) :

```
Enter number of FOL expressions: 6
Enter expressions:
Man(Marcus)
Pompeian(Marcus)
Pompeian(x) => Roman(x)
Roman(x) => Loyal(x)
Man(x) => Person(x)
Person(x) => Mortal(x)
Enter query: Mortal(Marcus)

Querying Mortal(Marcus):
Derived: Person(Marcus)
Derived: Roman(Marcus)
Derived: Mortal(Marcus)
Derived: Loyal(Marcus)
Yes, Marcus is Mortal.

All facts in Knowledge Base:
1. Loyal(Marcus)
2. Man(Marcus)
3. Mortal(Marcus)
4. Person(Marcus)
5. Pompeian(Marcus)
6. Roman(Marcus)
```

CODE (CNF) :

```
import re def getAttributes(string):    expr =
r'([^\s]+)'    matches = re.findall(expr, string)
return [m for m in str(matches) if m.isalpha()]
```

```
def getPredicates(string):
expr = r'[A-Za-z~]+([A-Za-z,]+)'
return re.findall(expr, string)
```

```

def DeMorgan(sentence):
    string =
    ".join(list(sentence).copy())  string
    = string.replace('~~', '')  flag = '[' in
    string  string = string.replace('~[', '')
    string = string.strip(']')
    for predicate in getPredicates(string):
        string = string.replace(predicate, f'~{predicate}')
        s = list(string)  for i,
        c in enumerate(s):      if
        c == 'V':          s[i] = '^'
        elif c == '^':      s[i] =
        'V'
        string = ".join(s)  string =
        string.replace('~~', '')  return
        f[{string}]' if flag else string

def Skolemization(sentence):
    SKOLEM_CONSTANTS = [f'{chr(c)}' for c in range(ord('A'), ord('Z')+1)]
    statement = ".join(list(sentence).copy())
    matches = re.findall('[\forall\exists].', statement)

    for match in matches[::-1]:
        statement = statement.replace(match, "")

    statements = re.findall(r'\[\w+[^]]+\]', statement)
    for s in statements:
        statement = statement.replace(s, s[1:-1])

```

```

for predicate in
getPredicates(statement):      attributes =
getAttributes(predicate)      if
".join(attributes).islower():
    statement = statement.replace(predicate, predicate)
else:
    aL = [a for a in attributes if a.islower()]
    aU = [a for a in attributes if not a.islower()][0] if attributes else ""
if aU:
    statement = statement.replace(aU, f'{SKOLEM_CONSTANTS.pop(0)}({aL[0]} if
len(aL) else match[1]}))'    return statement

def clean_output(expr):
    # Remove multiple brackets and redundant
negations    expr = expr.replace('~~', "")    while '[' in
expr or ']' in expr:
    expr = expr.replace('[', '[').replace(']', ']')

    expr = expr.strip('[] ')

    # Remove redundant outer brackets like [(p | q)] -> p | q
if expr.startswith('(') and expr.endswith(')'):
    expr = expr[1:-1]

    # Replace internal redundant
patterns    expr = re.sub(r'\s+', ' ', expr)
return expr

def fol_to_cnf(fol):
    statement = fol.replace("<=>", "_")
    while '_' in statement:

```

```

i = statement.index('_')
new_statement = '[' + statement[:i] + '=>' + statement[i+1:] + ']^[' + statement[i+1:] + '=>' +
statement[:i] + ']'
statement = new_statement

statement = statement.replace("=>", "-")

expr = r'\[([^\]]+)\]'
statements = re.findall(expr,
statement)  for i, s in
enumerate(statements):      if '[' in s and
']' not in s:      statements[i] += ']'
for s in statements:
    statement = statement.replace(s, fol_to_cnf(s))

while '-' in statement:
    i = statement.index('-')
    br = statement.index('[') if '[' in statement else 0      new_statement =
'~' + statement[br:i] + 'V' + statement[i+1:]      statement = statement[:br] +
new_statement if br > 0 else new_statement

while '~V' in statement:      i =
statement.index('~V')
    statement = list(statement)
    statement[i], statement[i+1], statement[i+2] = 'E', statement[i+2], '~~'
    statement = ".join(statement)

while '~E' in statement:      i =
statement.index('~E')
    s = list(statement)
    s[i], s[i+1], s[i+2] = 'V', s[i+2], '~~'

```

```

statement = ".join(s)

statement = statement.replace('~[A', '[~A')    statement =
statement.replace('~[E', '[~E')

```

```

expr = r'(~[AE].)'
statements = re.findall(expr, statement)
for s in statements:
    statement = statement.replace(s, fol_to_cnf(s))

```

```

expr = r'~\[[^\]]+\]'
statements = re.findall(expr, statement)
for s in statements:
    statement = statement.replace(s, DeMorgan(s))

```

return statement

```

def main():
    print("\n" + "="*50)
    print(" FOL to CNF Converter (Simplified Output)")
    print("="*50)
    print("Supports: A, E, ~, &, |, >>, <=>, brackets [] () {}")
    print("NOTE: Use 'V' for OR inside the formula if needed.")
    print("-" * 50)
    fol = input("Enter FOL formula: ").strip()
    print("-" * 50)
    try:
        raw_cnf = fol_to_cnf(fol)           result =
        Skolemization(raw_cnf)             cleaned =
        clean_output(result)      print(f"Original: {fol}")
        print(f"CNF Form: {cleaned}")      except

```

```

Exception as e:      print("\nError: Could not parse
the formula.")           print("Details:", e)
print("*50 + "\n") if __name__ == "__main__":
main()

```

OUTPUT (CNF):

```

=====
          FOL to CNF Converter (Simplified Output)
=====
Supports: ∀, ∃, ~, &, |, >>, <=>, brackets [] () {}
NOTE: Use 'V' for OR inside the formula if needed.
-----
Enter FOL formula: ∀x[~∀y~(Animal(y)V Loves(x,y))]V[∃y Loves(y,x)]
-----
Original:  ∀x[~∀y~(Animal(y)V Loves(x,y))]V[∃y Loves(y,x)]
CNF Form:  Animal(y)V Loves(x,y))]V[ Loves(y,x
=====
```

Program 10: Resolution ALGORITHM

⋮

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Resolution in FOL

→ Algorithm:

- 1) Convert all sentences to CNF.
- 2) Negate conclusions & convert the results to CNF.
- 3) Add negated conclusion or no premise clause.
- 4) Repeat until contradiction or no progress is made.

• Example:

- $\text{allergies}(x) \rightarrow \text{sneeze}(x)$
 $\Rightarrow \neg \text{allergies}(x) \vee \neg \text{sneeze}(x)$
- $\text{cat}(y) \wedge \text{allergic_to_cat}(x) \rightarrow \text{allergies}(x)$
 $\Rightarrow \neg \text{cat}(y) \vee \neg \text{allergic_to_cat}(x) \vee \text{allergies}(x)$
- $\text{cat}(\text{Felix})$
- $\text{allergic_to_cat}(\text{Many})$
- To prove: $\text{sneeze}(\text{Many})$

→ So we include $\neg \text{sneeze}(\text{Many})$ to the KB & try to prove contradiction.

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→ Resolution:

$$\begin{array}{c} \neg \text{allergies}(x) \vee \text{sneeze}(x) \quad \neg \text{cat}(y) \vee \neg \text{allergic_to_cat}(x) \\ \neg \text{allergies}(x) \vee \neg \text{sneeze}(x) \quad \neg \text{allergic_to_cat}(x) \\ \neg \text{allergies}(x) \quad \neg \text{sneeze}(x) \\ \neg \text{allergies}(x) \quad \neg \text{allergic_to_cat}(\text{Many}) \quad \neg \text{cat}(\text{Felix}) \\ \neg \text{allergic_to_cat}(\text{Many}) \quad \neg \text{allergic_to_cat}(\text{Many}) \end{array}$$

~~Right~~

∴ We have a contradiction.
 $\Rightarrow \neg \text{sneeze}(\text{Many})$ is false

∴ $\text{sneeze}(\text{Many})$ is true
 \Rightarrow Hence we prove that many sneezes.

→ OUTPUT:

The negation is unsatisfiable. By resolution, Many sneezes is proven.

CODE:

```
from sympy import symbols from sympy.logic.boolalg import
Implies, And, Or, Not, to_cnf from sympy.logic.inference
import satisfiable
```

```
# Define symbols
Food = symbols('Food')
Apple = symbols('Apple')
Vegetables = symbols('Vegetables')
Peanuts = symbols('Peanuts')
John_likes_x = symbols('John_likes_x')
Anil_eats_x = symbols('Anil_eats_x')
Harry_eats_x = symbols('Harry_eats_x')
```

```

Alive_x = symbols('Alive_x')
Killed_x = symbols('Killed_x')

# Knowledge Base in propositional logic
# a. John likes all kind of food -> For each food x, John_likes_x if Food(x)
kb = And(
    Implies(Food, John_likes_x), # a
    Implies(Or(Apple, Vegetables), Food), # b
    Implies(And(Anil_eats_x, Not(Killed_x)), Food), # c
    And(Anil_eats_x, Alive_x), # d
    Implies(Anil_eats_x, Harry_eats_x), # e
    Implies(Alive_x, Not(Killed_x)), # f
    Implies(Not(Killed_x), Alive_x) # g
)
)

# We want to prove: John likes peanuts -> John_likes_x for Peanuts
# Assume the negation of the goal for resolution goal_negation
= Not(John_likes_x)

# Combine KB with negated goal
combined = And(kb, goal_negation)

# Check satisfiability
sat_result = satisfiable(combined)

if sat_result:
    print("The negation is satisfiable. Cannot prove John likes peanuts from KB.") else:
    print("The negation is unsatisfiable. By resolution, John likes peanuts is proven!")

```

OUTPUT :

The negation is unsatisfiable. By resolution, John likes peanuts is proven!