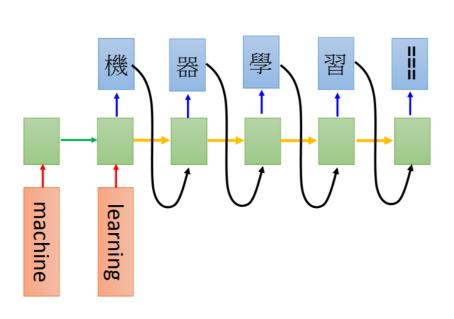
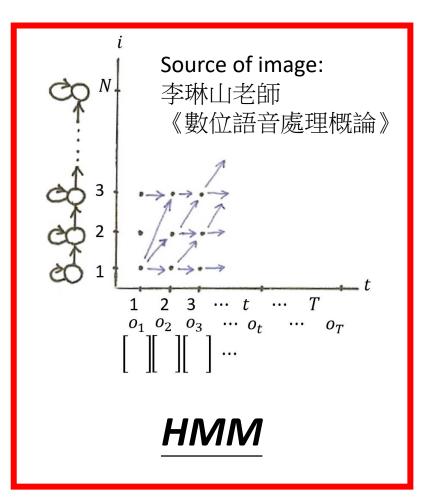


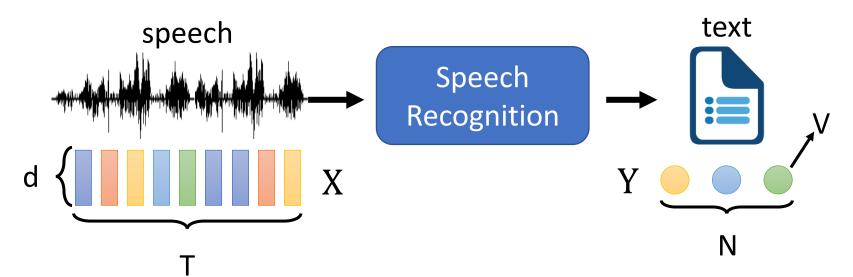
### Two Points of Views



Seq-to-seq



# Hidden Markov Model (HMM)



$$P_{\theta}(X|Y) = ?$$

The token here is small unit called state.

#### **Training**

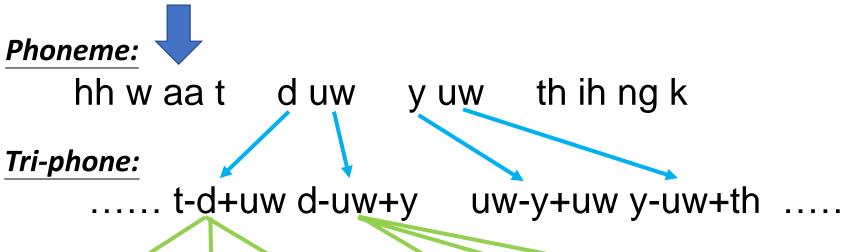
$$\theta^* = \arg\max_{\theta} \log P_{\theta}(X|\hat{Y})$$

#### Testing

$$Y^* = \arg\max_{Y} \log P_{\theta}(X|Y)$$

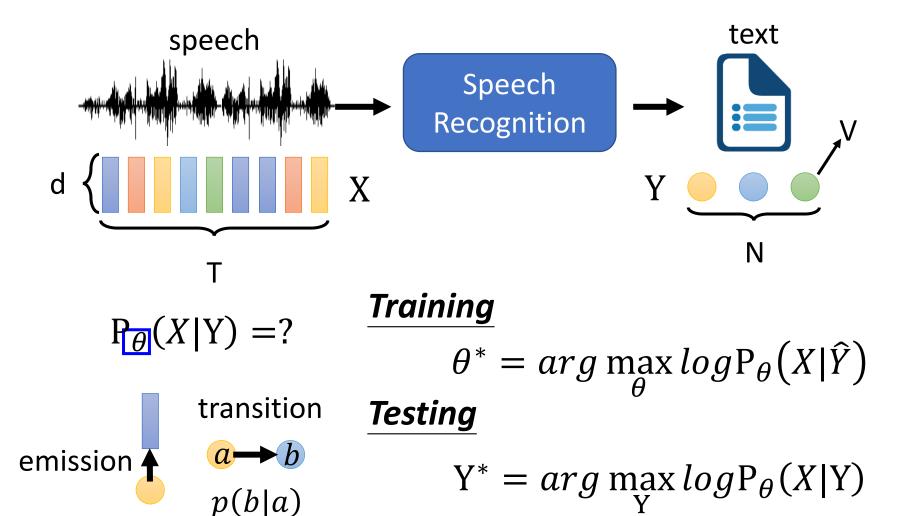
#### **HMM**

A sentence corresponds to a sequence of states
 what do you think



t-d+uw1 t-d+uw2 t-d+uw3 d-uw+y1 d-uw+y2 d-uw+y3 *State:* 

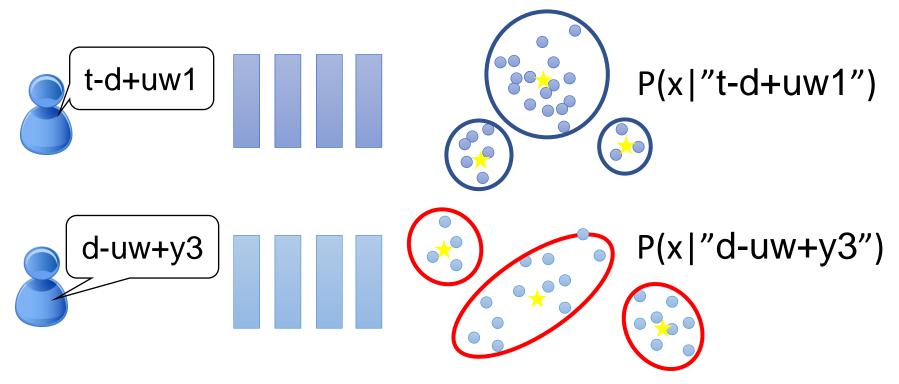
# Hidden Markov Model (HMM)



# HMM – Emission Probability

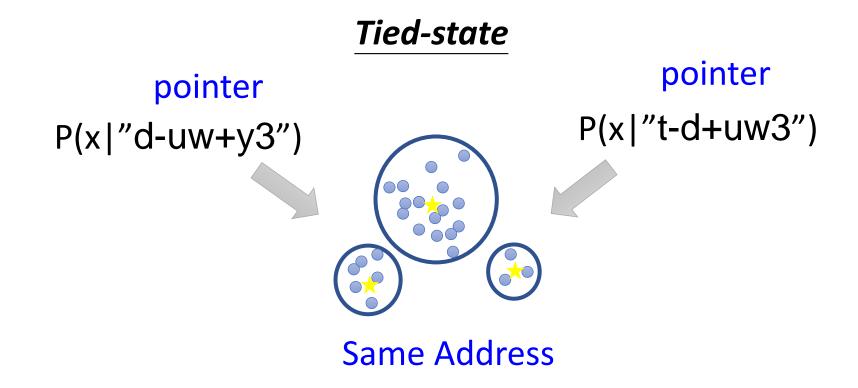
Each state has a stationary distribution for acoustic features

Gaussian Mixture Model (GMM)

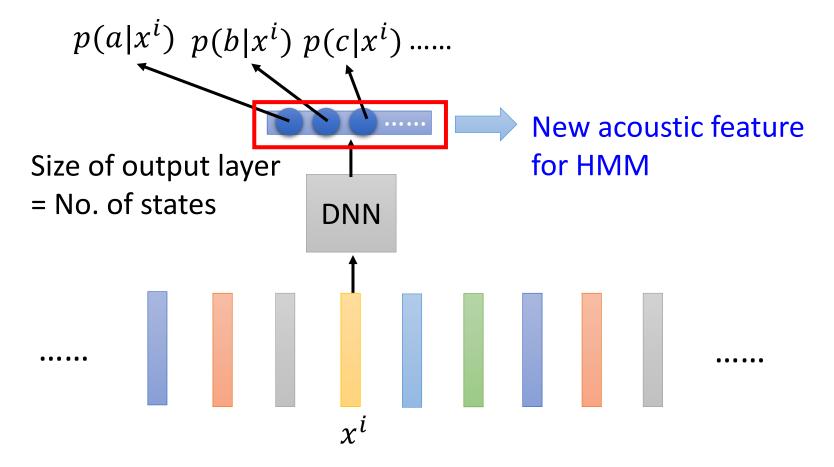


# HMM – Emission Probability

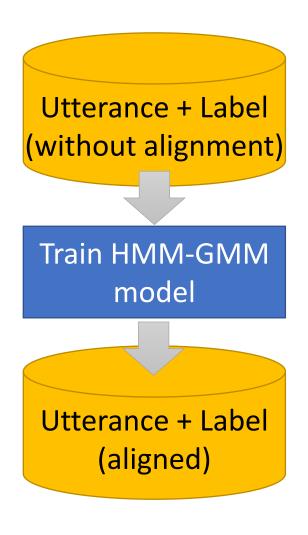
Each state has a stationary distribution for acoustic features

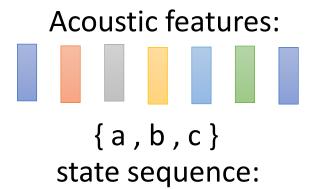


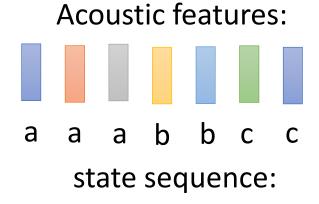
Problem (X|Y) =? 
$$\sum_{h \in align(Y)} P(X|h) \quad h = abccbc \times h = abbbccc \times h = abbbcccc \times h = abbbbcccc \times h = abbbbccccc \times h = abbbbcccc \times h = abbbbcccc \times h = abbbbccccc \times h = abbbbccccc \times h = abbbbcccc \times h = abbbbccccc \times h = abbbccccc \times h = ab$$

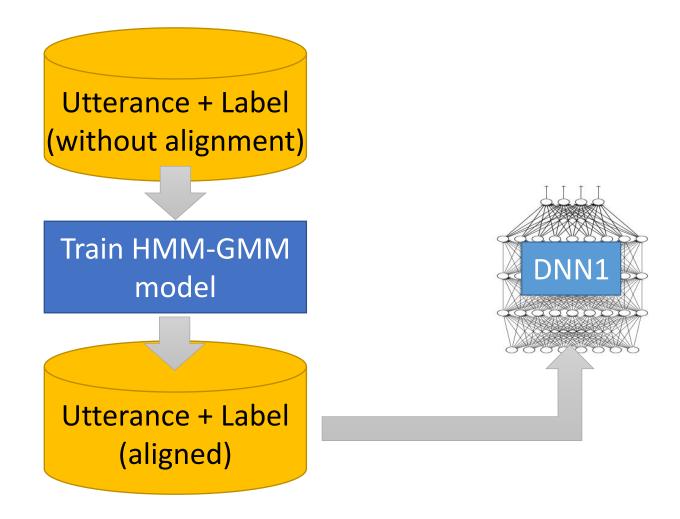


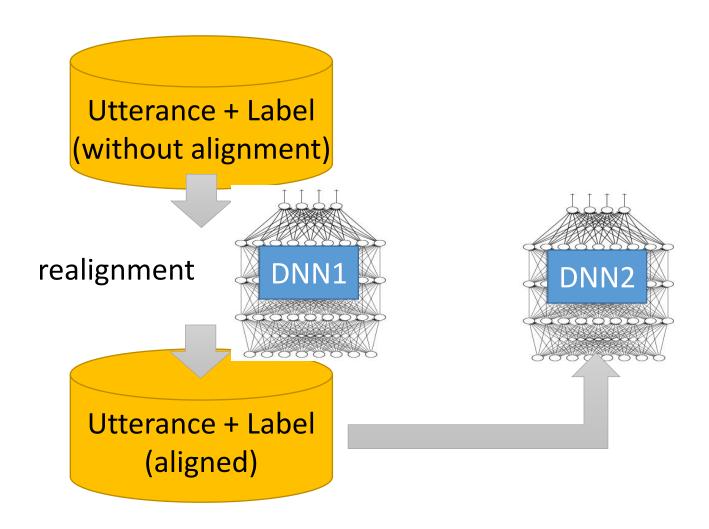
Last hidden layer or bottleneck layer are also possible.



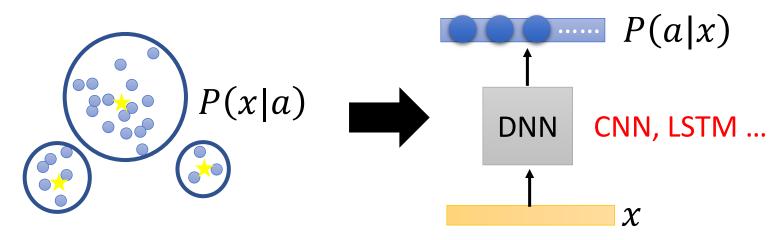








# Before End-to-end — Hybrid



DNN output 
$$P(x|a) = \frac{P(x,a)}{P(a)} = \frac{P(a|x)P(x)}{P(a)}$$
 Count from training data

# **Human Parity!**

- 微軟語音辨識技術突破重大里程碑:對話辨識能力達人類水準!(2016.10)
  - https://www.bnext.com.tw/article/41414/bn-2016-10-19-020437-216

Machine 5.9% v.s. Human 5.9%

[Yu, et al., INTERSPEECH'16]

- IBM vs Microsoft: 'Human parity' speech recognition record changes hands again (2017.03)
  - http://www.zdnet.com/article/ibm-vs-microsoft-human-parityspeech-recognition-record-changes-hands-again/

Machine 5.5% v.s. Human 5.1%

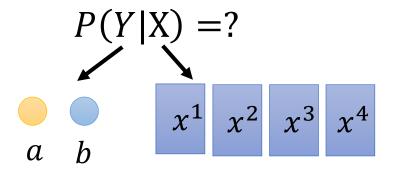
[Saon, et al., INTERSPEECH'17]

# Very Deep

	VGG Net (85M Parameters)	Residual-Net (38M Parameters)	LACE (65M Parameters)		
)	14 weight layers	49 weight layers	22 weight layers		
,	40x41 input	40x41 input	40x61 input		
	3 – conv 3x3, 96	3 – [conv 1x1, 64 conv 3x3, 64 conv 1x1, 256]	5 – conv 3x3, 128		
	Max pool	4 – [conv 1x1, 128 conv 3x3, 128 conv 1x1, 512]	5 – conv 3x3, 256		
	4 – conv 3x3, 192	6 – [conv 1x1, 256 conv 3x3, 256 conv 1x1, 1024]	5 – conv 3x3, 512		
	Max pool	3 – [conv 1x1, 512 conv 3x3, 512 conv 1x1, 2048]	5 – conv 3x3, 1024		
	4 – conv 3x3, 384	Average pool	1 – conv 3x4, 1		
	Max pool	Softmax (9000)	Softmax (9000)		
<b>6</b> ]	2-FC-4096				
.1	Softmax (9000)				

[Yu, et al., INTERSPEECH'16]

### LAS

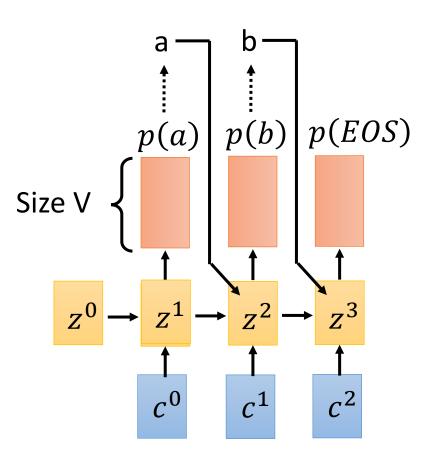


• LAS directly computes P(Y|X)

$$P(Y|X) = p(a|X)p(b|a,X)...$$

$$\theta^* = \arg\max_{\theta} \log P_{\theta}(\hat{Y}|X)$$

$$Y^* = arg \max_{Y} log P_{\theta}(Y|X)$$
  
Beam Search



### CTC, RNN-T

$$P(Y|X) = ?$$

$$x^{1} x^{2} x^{3} x^{4}$$

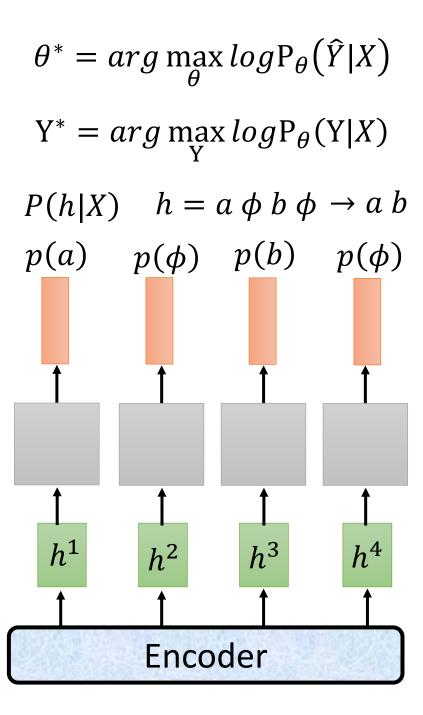
$$a b$$

• LAS directly computes P(Y|X)

$$P(Y|X) = p(a|X)p(b|a,X)...$$

 CTC and RNN-T need alignment

$$P_{\theta}(Y|X) = \sum_{h \in align(Y)} P(h|X)$$



### HMM, CTC, RNN-T

#### **HMM**

#### CTC, RNN-T

$$P_{\theta}(X|Y) = \sum_{h \in align(Y)} P(X|h) \qquad P_{\theta}(Y|X) = \sum_{h \in align(Y)} P(h|X)$$

$$P_{\theta}(Y|X) = \sum_{h \in align(Y)} P(h|X)$$

- 1. Enumerate all the possible alignments
- 2. How to sum over all the alignments
- 3. Training:

$$\theta^* = \arg\max_{\theta} \log P_{\theta}(\widehat{Y}|X)$$

$$\frac{\partial P(\widehat{Y}|X)}{\partial \theta} = \widehat{X}$$

4. Testing (Inference, decoding):

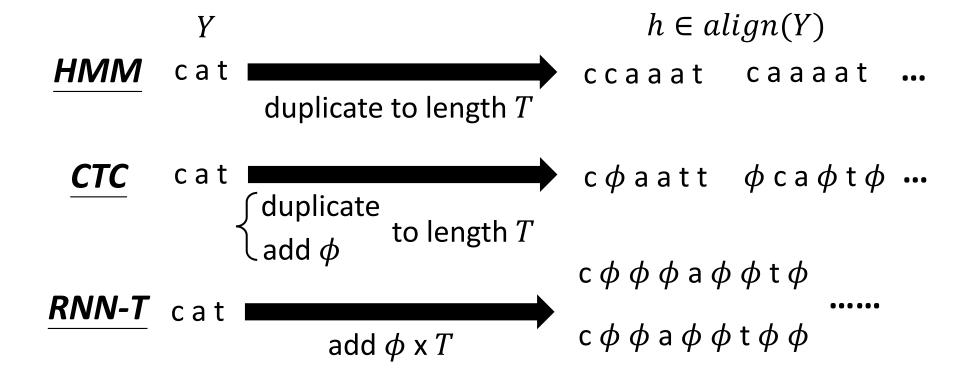
$$Y^* = arg \max_{Y} log P_{\theta}(Y|X)$$

#### LAS

# All the alignments

#### 你們在忙什麼 ☺



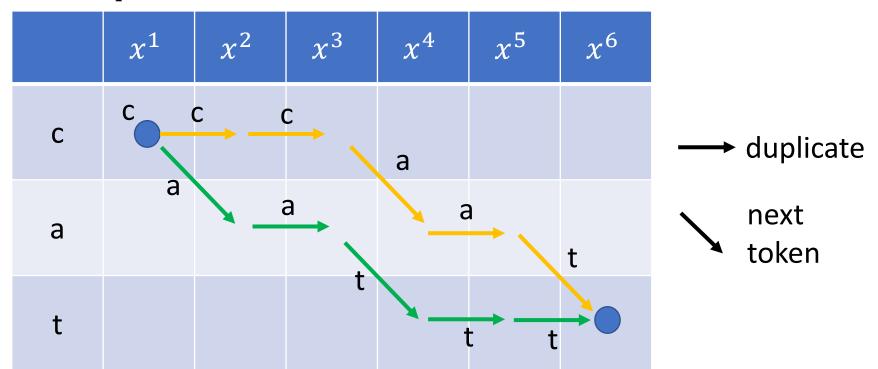


#### duplicate to length T

For n = 1 to Noutput the n-th token  $t_n$  times

**constraint**: 
$$t_1 + t_2 + \cdots + t_N = T$$
,  $t_n > 0$ 

#### Trellis Graph



**HMM** cat

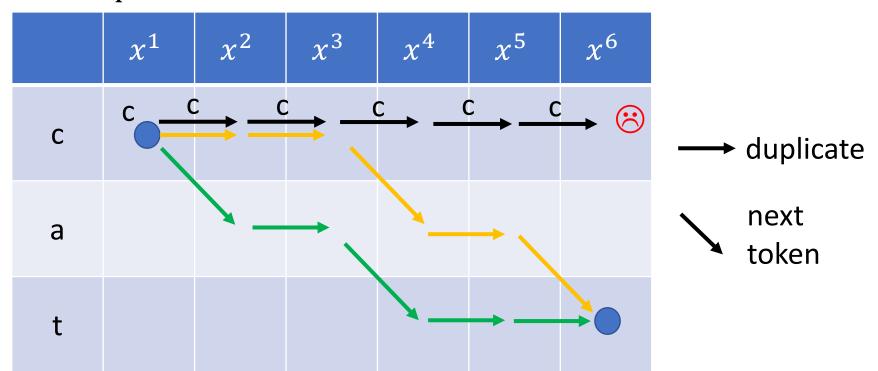
ccaaat caaaat ...

duplicate to length T

For n = 1 to Noutput the n-th token  $t_n$  times

**constraint**:  $t_1 + t_2 + \cdots + t_N = T$ ,  $t_n > 0$ 

#### Trellis Graph



CTC

cat 
$$\begin{array}{c} \text{c}\,\phi\,\text{aatt}\quad\phi\,\text{c}\,\phi\,\text{w}\\ \text{duplicate}\\ \text{add}\,\phi \end{array}$$
 to length  $T$ 

output " $\phi$ "  $c_0$  times For n = 1 to *N* output the n-th token  $t_n$  times output " $\phi$ "  $c_n$  times constraint:  $t_1 + t_2 + \cdots t_N +$  $c_0 + c_1 + \cdots c_N = T$  $t_n > 0$   $c_n \ge 0$ 

cat  $\begin{array}{c|c} \text{c} & \text{c} & \text{c} & \text{d} & \text{$ 

	$x^1$	$x^2$	$x^3$	<i>x</i> <sup>4</sup>	<i>x</i> <sup>5</sup>	<i>x</i> <sup>6</sup>
φ						
С		→ du	plicate			
φ		ins	sert $\phi$			
а			xt toker			
φ		(φ	can be	skipped	)	
t						
φ						

cat  $\begin{array}{c|c} \text{c} & \text{c} & \text{c} & \text{d} & \text{$ 

	$x^1$	$x^2$	$x^3$	$x^4$	<i>x</i> <sup>5</sup>	<i>x</i> <sup>6</sup>
φ	• ~	→ dı	uplicate	φ		
С		ne	ext toke	n		
$\phi$			annot sk			
а		aı	ny toker	1		
$\phi$						
t						
φ						

cat  $\begin{array}{c|c} \text{c} & \text{c} & \text{c} & \text{d} & \text{$ 

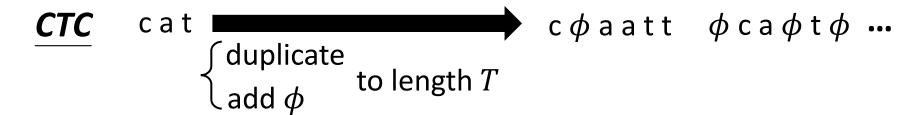
	$x^1$	$x^2$	$x^3$	$x^4$	$x^5$	<i>x</i> <sup>6</sup>
φ						
С						
φ					→ dup	olicate
а			→ dup	licate	ins	ert $\phi$
$\phi$			inse	ert $\phi$		
t			nex	t token		
φ						

cat  $\begin{array}{c|c} \text{c} & \text{c} & \text{c} & \text{d} & \text{d} \\ & & \text{d} & \text{d} \\ & \text{add} & \phi \end{array}$ 

	$x^1$	$x^2$	$x^3$	<i>x</i> <sup>4</sup>	<i>x</i> <sup>5</sup>	<i>x</i> <sup>6</sup>
φ	$\phi_{\bullet}$	С				
С	C		-			
$\phi$	a			a		
а		1			Þ	
$\phi$		φ			t	
t			t			
$\phi$				φ	φ	<b>→</b> •

cat  $\begin{array}{c|c} c & c & c & \phi &$ 

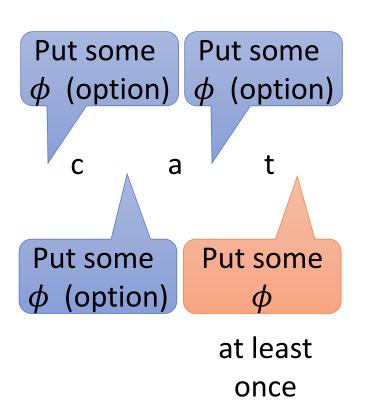
	$x^1$	$x^2$	$x^3$	$x^4$	<i>x</i> <sup>5</sup>	x <sup>6</sup>
φ	$\phi$	С				
С	c					
φ		a			а	
а						
φ				t	t	
t				1	$\phi$ ,	
$\phi$					φ	<b>→</b>



	$x^1$	$x^2$	$x^3$	<i>x</i> <sup>4</sup>	<i>x</i> <sup>5</sup>	<i>x</i> <sup>6</sup>	
φ							
S			•			next to	oken
$\phi$		IS	the sa	me tok	ken		
е			→ dup	olicate			
φ			ins	ert $\phi$			
е			nex	t token			
φ			ee	→ e			



$$c \phi \phi \phi a \phi \phi t \phi$$
 $c \phi \phi a \phi \phi t \phi \phi$ 

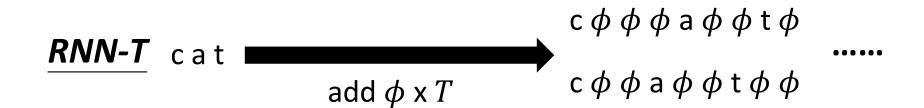


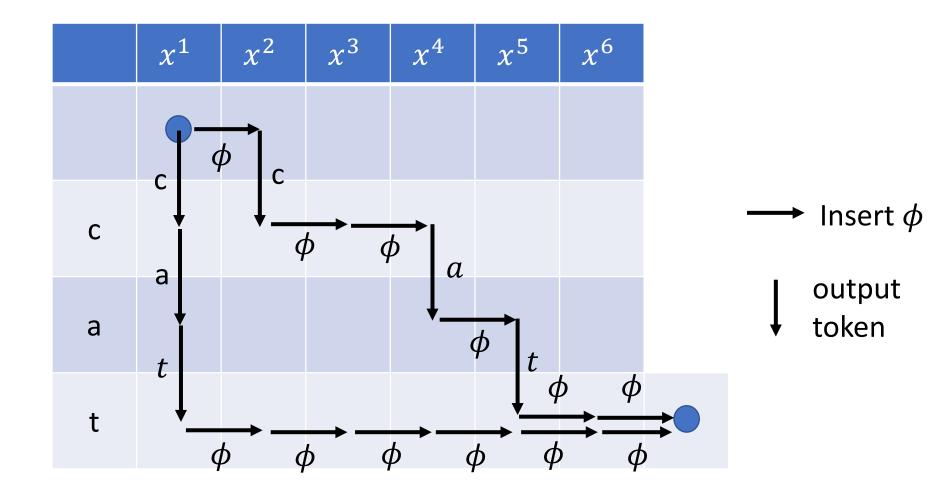
output " $\phi$ "  $c_0$  times

For n = 1 to Noutput the n-th token 1 times
output " $\phi$ "  $c_n$  times constraint:  $c_0 + c_1 + \cdots c_N = T$   $c_N > 0$   $c_n \ge 0$  for n = 1 to N-1

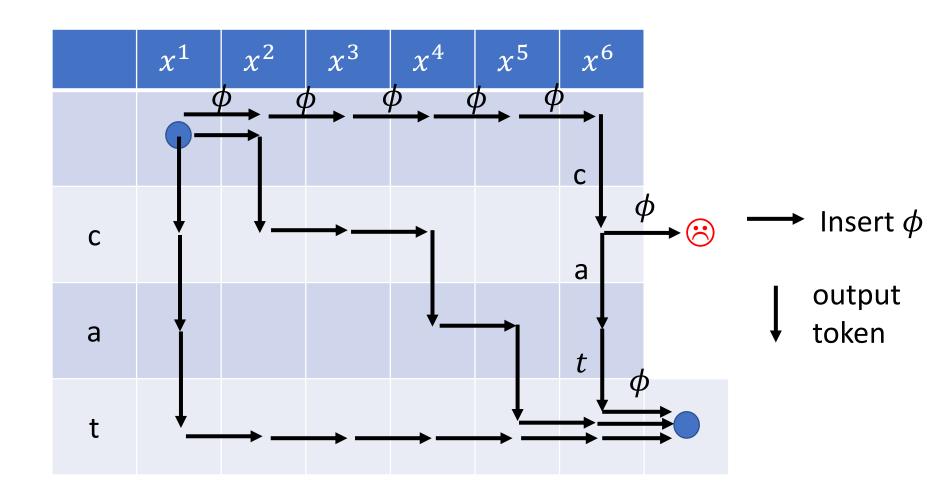


	$x^1$	$x^2$	$x^3$	$x^4$	$x^5$	x <sup>6</sup>			
	c	<i>b</i> →							
С								<b>→</b>	Insert $\phi$
а								1	output token
t						$\overline{\phi}$	<b>→</b> •		









### HMM, CTC, RNN-T

#### **HMM**

CTC, RNN-T

$$P_{\theta}(X|Y) = \sum_{h \in align(Y)} P(X|h) \qquad P_{\theta}(Y|X) = \sum_{h \in align(Y)} P(h|X)$$

$$P_{\theta}(Y|X) = \sum_{h \in align(Y)} P(h|X)$$

- 1. Enumerate all the possible alignments
- 2. How to sum over all the alignments
- 3. Training:

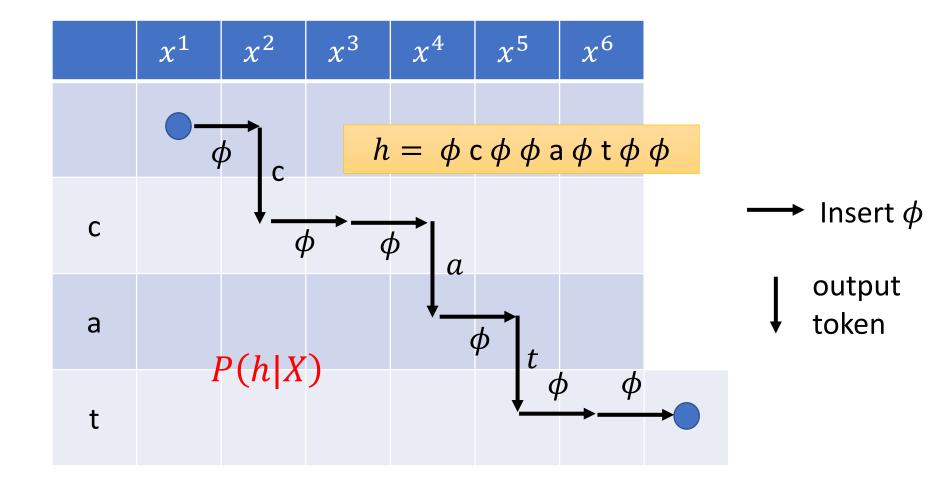
$$\theta^* = \arg\max_{\theta} \log P_{\theta}(\widehat{Y}|X)$$

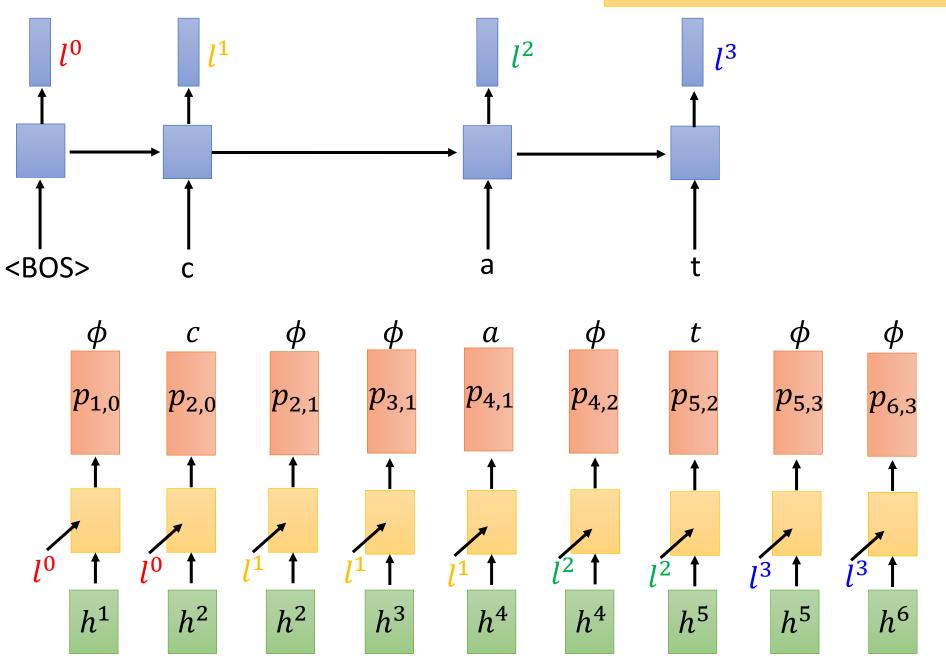
$$\frac{\partial P(\hat{Y}|X)}{\partial \theta} = ?$$

4. Testing (Inference, decoding):

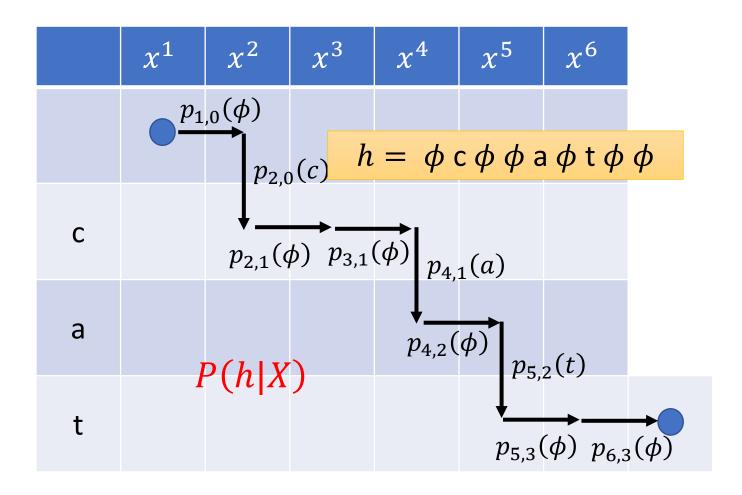
$$Y^* = arg \max_{Y} log P_{\theta}(Y|X)$$

### Score Computation

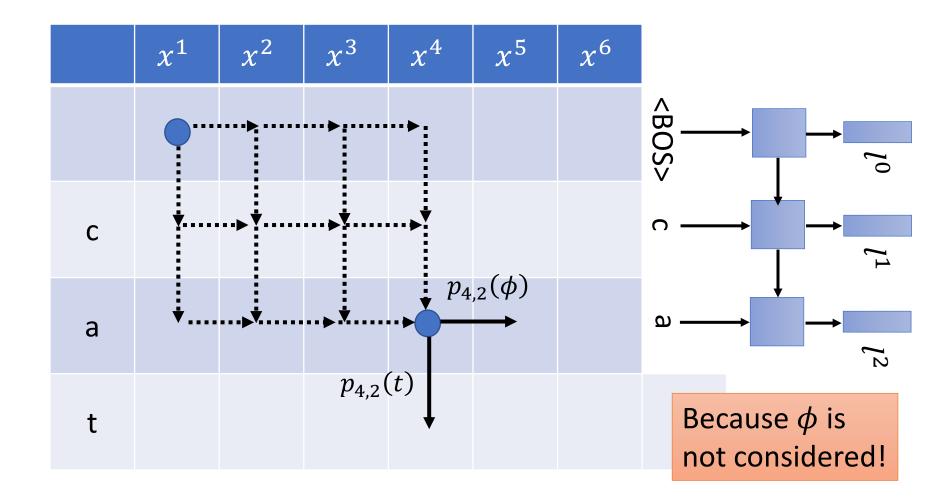




# Score Computation



## Score Computation



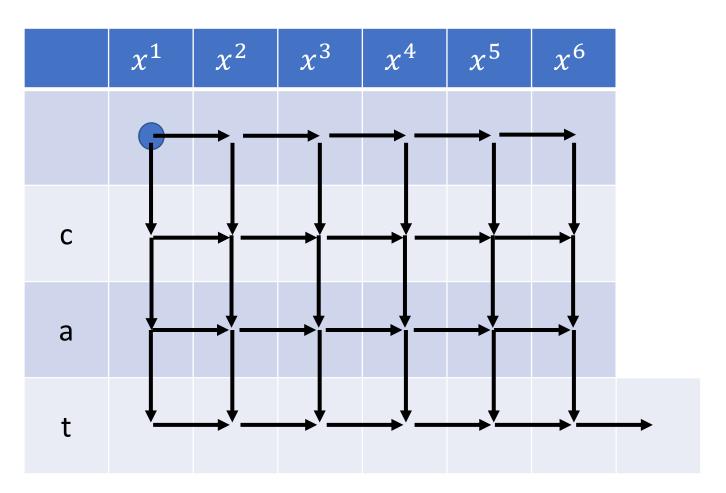
 $\alpha_{i,j}$ : the summation of the scores of all the alignments that read i-th acoustic features and output j-th tokens

$$\alpha_{4,2} = \alpha_{4,1} p_{4,1}(a) + \alpha_{3,2} p_{3,2}(\phi)$$

	$x^1$	$x^2$	$x^3$	$\chi^4$	<i>x</i> <sup>5</sup>	<i>x</i> <sup>6</sup>
	•			▶.		
С	<b>*</b>	••••	▶♥	$\alpha_{i}$	4,1 enerat	o "a"
а	<b>↓</b>	<b>,</b>	$\alpha_{3,2}$		4,2	с а
t				ad $x^4$ nerate	"φ",	

 $\alpha_{i,j}$ : the summation of the scores of all the alignments that read i-th acoustic features and output j-th tokens

$$\alpha_{4,2} = \alpha_{4,1}p_{4,1}(a) + \alpha_{3,2}p_{3,2}(\phi)$$



You can compute summation of the scores of all the alignments.

## HMM, CTC, RNN-T

### **HMM**

### CTC, RNN-T

$$P_{\theta}(X|Y) = \sum_{h \in align(Y)} P(X|h) \qquad P_{\theta}(Y|X) = \sum_{h \in align(Y)} P(h|X)$$

$$P_{\theta}(Y|X) = \sum_{h \in align(Y)} P(h|X)$$

- 1. Enumerate all the possible alignments
- 2. How to sum over all the alignments
- 3. Training:

$$\theta^* = \arg\max_{\theta} \log P_{\theta}(\widehat{Y}|X)$$

$$\frac{\partial P(\widehat{Y}|X)}{\partial \theta} = \widehat{X}$$

4. Testing (Inference, decoding):

$$Y^* = arg \max_{Y} log P_{\theta}(Y|X)$$

## Training

$$\theta^* = arg \max_{\theta} log P(\hat{Y}|X)$$

$$\theta \xrightarrow{p_{4,1}(a)} P(\hat{Y}|X)$$

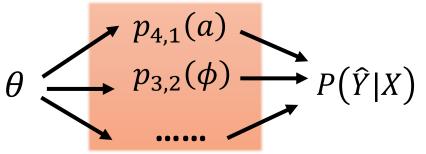
$$P(\hat{Y}|X) = \sum_{h} P(h|X)$$

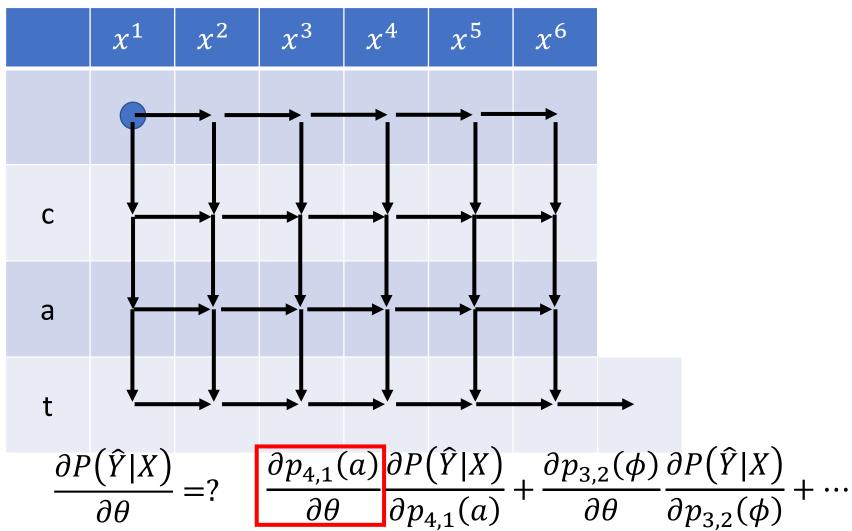
φ c φ φ a φ t φ φ

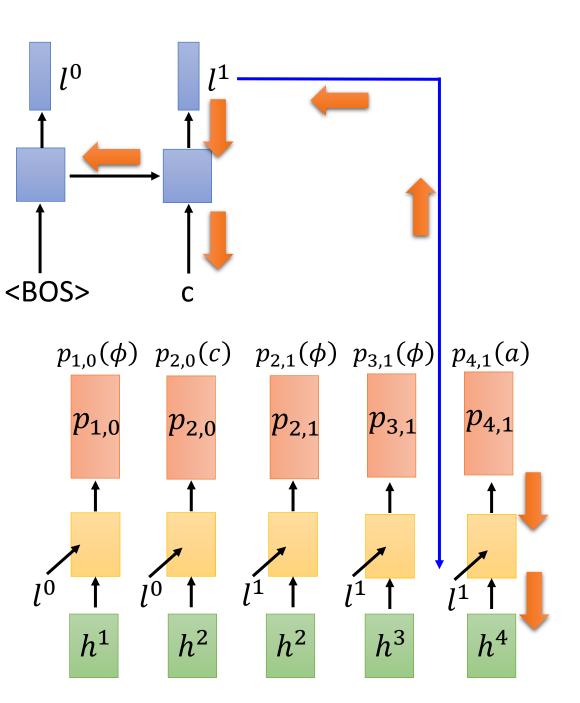
$$p_{1,0}(\phi)$$
  $p_{2,0}(c)$   $p_{2,1}(\phi)$   $p_{3,1}(\phi)$   $p_{4,1}(a)$   $p_{4,2}(\phi)$   $p_{5,2}(t)$   $p_{5,3}(\phi)$   $p_{6,3}(\phi)$ 

$$\frac{\partial P(\hat{Y}|X)}{\partial \theta} = ? \qquad \frac{\partial p_{4,1}(a)}{\partial \theta} \frac{\partial P(\hat{Y}|X)}{\partial p_{4,1}(a)} + \frac{\partial p_{3,2}(\phi)}{\partial \theta} \frac{\partial P(\hat{Y}|X)}{\partial p_{3,2}(\phi)} + \cdots$$

# Each arrow is a component







$$\frac{\partial p_{4,1}(a)}{\partial \theta} = ?$$

Backpropagation (through time)

$$\frac{\partial P(\hat{Y}|X)}{\partial \theta} = ? \qquad \frac{\partial p_{4,1}(a)}{\partial \theta} \frac{\partial P(\hat{Y}|X)}{\partial p_{4,1}(a)} + \frac{\partial p_{3,2}(\phi)}{\partial \theta} \frac{\partial P(\hat{Y}|X)}{\partial p_{3,2}(\phi)} + \cdots$$

$$P(\hat{Y}|X) = \sum_{\substack{h \text{ with } p_{4,1}(a) \\ p_{4,1}(a) \times other}} P(h|X) + \sum_{\substack{h \text{ without } p_{4,1}(a) \\ }} P(h|X)$$

$$\frac{\partial P(\hat{Y}|X)}{\partial p_{4,1}(a)} = \sum_{h \text{ with } p_{4,1}(a)} other = \sum_{h \text{ with } p_{4,1}(a)} \frac{P(h|X)}{p_{4,1}(a)}$$

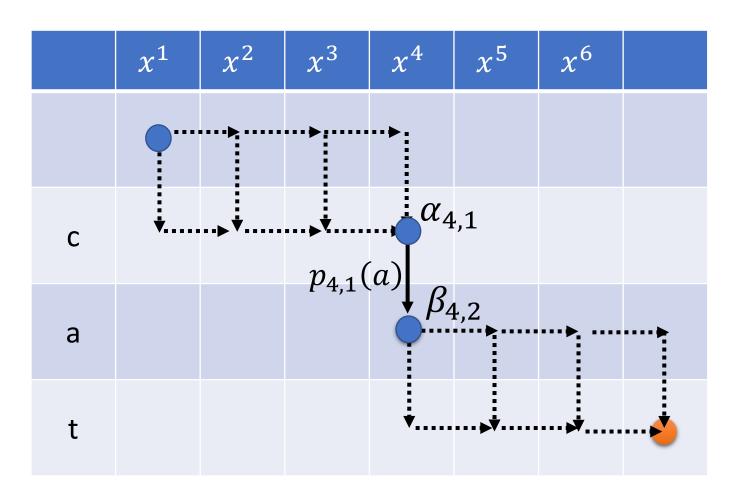
$$= \frac{1}{p_{4,1}(a)} \sum_{h \text{ with } p_{4,1}(a)} P(h|X)$$

 $\beta_{i,j}$ : the summation of the score of all the alignments staring from i-th acoustic features and j-th tokens

$$\beta_{4,2} = \beta_{4,3} p_{4,2}(t) + \beta_{5,2} p_{4,2}(\phi)$$

	$x^1$	$x^2$	$x^3$	$x^4$	<i>x</i> <sup>5</sup>	<i>x</i> <sup>6</sup>	
				read	<i>x</i> <sup>5</sup>		
С				gene	rate "	<i>þ"</i> ,	
			$eta_4$	0	$eta_{5,}$		
а			$P_4$	.,2	₽5, <del>→-</del> ·····	2 ···•. ····	
a	OT .	enerat	o "t"	Ť			
_	g	ciicial	.C (				
t			$eta_4$	,3	· · · • • • · · · · · ·	••••	•••

$$\frac{\partial P(\hat{Y}|X)}{\partial p_{4,1}(a)} = \frac{1}{p_{4,1}(a)} \sum_{\substack{a \text{ with } p_{4,1}(a)}} P(a|X) \quad \alpha_{4,1} \ p_{4,1}(a) \beta_{4,2}$$



## HMM, CTC, RNN-T

### **HMM**

CTC, RNN-T

$$P_{\theta}(X|Y) = \sum_{h \in align(Y)} P(X|h) \qquad P_{\theta}(Y|X) = \sum_{h \in align(Y)} P(h|X)$$

$$P_{\theta}(Y|X) = \sum_{h \in align(Y)} P(h|X)$$

- 1. Enumerate all the possible alignments
- 2. How to sum over all the alignments
- 3. Training:

$$\theta^* = \arg\max_{\theta} \log P_{\theta}(\widehat{Y}|X)$$

$$\frac{\partial P(\widehat{Y}|X)}{\partial \theta} = ?$$

4. Testing (Inference, decoding):

$$Y^* = arg \max_{Y} log P_{\theta}(Y|X)$$

## Summary

	LAS	СТС	RNN-T
Decoder	Not independent	independent	Not independent
Alignment	Not explicit (Soft alignment)	Yes	Yes
Training	Just train it	Sum over alignment	Sum over alignment
Streaming	No	Yes	Yes

### Reference

- [Yu, et al., INTERSPEECH'16] Dong Yu, Wayne Xiong, Jasha Droppo, Andreas Stolcke, Guoli Ye, Jinyu Li, Geoffrey Zweig, Deep Convolutional Neural Networks with Layer-wise Context Expansion and Attention, INTERSPEECH, 2016
- [Saon, et al., INTERSPEECH'17] George Saon, Gakuto Kurata, Tom Sercu, Kartik Audhkhasi, Samuel Thomas, Dimitrios Dimitriadis, Xiaodong Cui, Bhuvana Ramabhadran, Michael Picheny, Lynn-Li Lim, Bergul Roomi, Phil Hall, English Conversational Telephone Speech Recognition by Humans and Machines, INTERSPEECH, 2017