

Recipe for `bfs_dfs`:

Input: `graph`, which is a `DiGraph` object that represents the street graph

`rac_class`, which is a restricted access containerclass(queue or stack)

`start_node`, which is the starting node in `graph`

`end_node`, which is the end node in `graph`

Output: `parent`, which is a map that maps nodes in `graph` to their parent nodes

1. Initialize the variable `rac` to an empty `rac_class`
2. Initialize the variable `dist` to an empty map
3. Initialize the variable `parent` to an empty map
4. Iterate over each node in `graph` and assign the value of node to the variable `node`. Inside the iteration:
 - i. Assign the value of infinity to the value of `node` in `dist`.
 - ii. Assign the value of none to the value of `node` in `parent`
5. Assign the value of 0 to the value of `start_node` in the map `dist`
6. Push the `start_node` into `rac`
7. While length of `rac` doesn't equal to 0:
 - i. Remove the node from `rac` and assign the value of the node to the variable `node`
 - ii. Get the neighbors of the `node` from the `graph` by calling the method `get_neighbors` and assign the value to the variable `nbrs`.
 - iii. Iterate each node in `nbrs` and assign the value to `nbr`. Inside the iteration:
 - a) Check if the value of `nbr` in the map `dist` equals to infinity, if the output is true:
 1. the value of `nbr` in the map `dist` equals to the value of `nbr` in the map `dist` plus 1
 2. the value of `nbr` in the map `parent` equals to the value of `node`
 3. Push the `nbr` into `rac`
 4. Check if the value of `nbr` in the map `dist` equals to `end_node`, if the output is true:
Return `parent`
8. Return `parent`

Recipe for `dfs`:

Input: `graph`, which is a `DiGraph` object that represents the street graph

`start_node`, which is the starting node in `graph`

`end_node`, which is the end node in `graph`

`parent`, which is a map that maps nodes in `graph` to their parent nodes

Output: `parent`, which is a map that maps nodes in `graph` to their parent nodes

Algorithm used: `dfs`

Base case: `start_node=end_node`, or `counter=0`, which means the entire graph has been searched

Recursive case:

`start_node` does not equal to `end_node`, or `counter` does not equal to 0

1. Get the keys of the map `parent` and assign the value to the variable `key`.
2. Assign the value of 0 to the variable `counter`
3. Iterate each node in `nbrs` and assign the value to `element1`. Inside the iteration:
 - i. Determine whether `parent` has `element1` as one of its key, if the output is False:
 - a) Assign the value of 1 to the variable `counter`.
4. Determine whether `start_node=end_node` or `counter` equals to 0, if the output is true:
 - i. Return `parent`

If the output is false:

 - i. Iterate each node in `nbrs` and assign the value to `nbr`. Inside the iteration:
 - a) Determine whether `nbr` belongs to `key`, if the output is true:
 1. The value of `nbr` in the map `parent` equals to the value of `start_node`.
 2. Call the function `dfs`, with `graph`, `nbr`, `end_node` and `parent` as its arguments
 - ii. Return `parent`

Recipe for `astar`

Input: `graph`, which is a `DiGraph` object that represents the street graph

`start_node`, which is the starting node in `graph`

`end_node`, which is the end node in `graph`

`edge_distance`, which is a function used to calculate the g (actual distance) between two nodes

`straight_line_distance`, which is a function used to calculate h (heuristic distance) between the node and the ending node

Output:

`parent`, which is a map that maps nodes in `graph` to their parent nodes

Algorithms used: `edge_distance`, whose parameters are `node1`, `node2`, `graph`, return value of g
`straight_line_distance`, whose parameters are `node1`, `node2`, `graph`, return value of h

1. Initialize `openset`, `closedset` to empty sequences. Add `start_node` into the `openset`.
2. Create a map `gcost`, assign the value of 0 to the key `start_node`. Calculate the h value by calling the `straight_line_distance` function with `start_node`, `end_node`, `graph` and then map the h value to `start_node`. Use the variable `hcost` to refer to this map. Create a map `parent`, assign the value of None to the key `start_node`.
3. While the `openset` is not empty:
 - i. get the first element in the `openset` and assign its value to the variable `minnode`
 - ii. add the value of `minnode` in the map `gcost` with the value of `minnode` in the map `hcost`, assign the value of the sum to the variable `minf`.
 - iii. Iterate over each node in the `openset` and assign the value to the variable `node`, inside the iteration:
 - a) add the value of `node` in the map `gcost` with the value of `node` in the map `hcost`, assign the value of the sum to the variable `fcost`.
 - b) Determine whether `fcost` is smaller than `minf`, if the

output is true:

- i. Assign the value of `node` to `minnode`. Assign the value of `fcost` to `minf`
- iv. Determine if the value of `minnode` equals to the value of `end_node`. If the output is true:
 - a) Just stop
- v. Remove `minnode` from the `openset`. Add `minnode` into the `closedset`.
- vi. Get neighbors of the `minnode` by calling the function `get_neighbors` with `minnode` as its parameter. Iterate over each node of neighbors and assign the value to `nbr`. Inside the iteration:
 - i. Add the value of `minnode` in the map `gcost` with the value of `h`, calculated by calling the function `edge_distance` with `nbr`, `end_node`, `graph` as its 3 parameters. Assign the value of the sum to the variable `newgcost`.
 - ii. Determine if `nbr` in the `openset`, if the output is true:
 1. Determine if `newgcost` is smaller than the value `nbr` in the map `gcost`. If the output is true:
 - a) Assign the value of `newgcost` to the value `nbr` in the map `gcost`. Assign the value of `minnode` to the value of `nbr` in the map `parent`.
 - iii. If the output is false, determine whether `nbr` is both not in `openset` and not in `closedset`, if the output is true:
 1. Add `nbr` into the `openset`
 2. Assign the value of `minnode` to the value of `nbr` in the map `parent`.
 3. Calculate the value of `h` by calling the function `straight_line_distance` function with `nbr`, `end_node`, `graph` and then map the `h` value to the key `nbr` in the map `hcost`.
 4. Assign the value of `newgcost` to the value of the key `nbr` in the map `gcost`.
5. Return the map `parent`

Discussion:

1. The same place is that they have same starting point and end point. Besides, they both give routes by exploring points. Also the route given by them both may change even you fix the starting point and end point.

The difference is that the `bfs_dfs` will explore fewer points than recursive `dfs` algorithm. In fact, recursive `dfs` almost explore all the points while `bfs_dfs` only explores partial points. However, `bfs_dfs` actually gives the route that is farther than the route given by recursive `dfs`. Also, recursive one takes more time than `bfs_dfs`.

Therefore recursive `dfs` is better because it although it needs to explore the whole map, it can find the better route (shorter).

2. It depends. When your target is deep down in the map, it is better to use A star algorithm. This is because the route given by it is more close to the google map route. In fact, the distance of the route given by A star is shortest among all the algorithms.

But if your target is around the start point, bfs and A star work both very well because the route given by them are almost same and almost matches the google map route.

The reason I think is that A star algorithm always explores the node very deeply and downwardly. Therefore, it will work well when the goal is far away.

While bfs explores the route that is with fewest steps from the start point, therefore when the target is just around the start point, it works well.

3. dfs in bfs_dfs algorithm. This is because it always gives the farthest route compared with other algorithms. Sometimes it will even not get to the target. This is because it will just keep visiting the first child of every node it sees, so if the one you're looking for isn't the first child of its parent, it will never get there.

4. Maybe google map uses a better algorithm which can find the best route quickly accurately and efficiently. Our best algorithm will be slowed down when the map becomes larger while the google map will not. Another reason I think is that google map may have already stored large amount of data about the route choice. Therefore it can choose the best one or do the optimization based on its big data while ours doesn't too much existent data.