



**03** Hr **53** Min **14** Sec

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## Coding Area

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## **Number Gravity**

+ Problem Description

Prior to discovery of laws of gravitation, a brave young scientist attempted decoding the how two natural bodies "move" or "accelerate" towards each other. Later Newton, formulated the laws and the equations. Your task is to compute some metrics when two bodies move towards each other with postulates that the young scientist hypothesized.

Newton's law of universal gravitation from classical physics states that the gravitational force between two masses is proportional to the product of the masses and inversely proportional to the square of the distance between them. Imagine a scenario where a similar law applies to two specified natural numbers (positive integers) that "move" or "accelerate" towards each other on the number line. Let us explain with an example: Let us say we start with the following two different natural numbers:

n1 = 11

n2 = 22

n2 > n1

We will assume that the two numbers are initially at rest at their respective positions on the number line at positions L1 = 11 and L2 = 22 units from zero (the origin).

We calculate the initial "force" between them as a constant 10 times their product divided by the square of their difference: F = 10\*11\*22/(22-11)\*\*2 = 20 units.

The initial "acceleration" of n1 towards n2 would be a1 = F/n1 = 1.82 unit while the initial "acceleration" of n2 towards n1 would be a2 = F/n2 = 0.91 unit.

With initial velocities u1 and u2 being zero,

the "distance" moved by n1 and n2 in unit time would be

s1 = 0 + a1/2 = 1.82/2 = 0.91 = 1 unit (rounded using <u>HALF\_UP semantics</u>)

s2 = 0 + a2/2 = 0.91/2 = 0.45 = 0 unit (rounded using <u>HALF\_UP semantics</u>).

The new velocities after unit time would be

v1 = u1 + a1 = 0 + 1.82 = 1.82 units and

v2 = v2 + a2 = 0 + 0.91 = 0.91 unit.

Hence after a unit of time, n1 would be at location 12 with a velocity of 1.82 units and n2 would be near location 22 itself with a velocity of 0.91 units. We can proceed in a similar way i.e.

Note the existing positions and velocities,

Calculate the revised force, accelerations, new positions, new velocities

Track the movements of the two numbers as follows:

| t | l1         | 12         | 2-<br> 1 | F     | u1    | u2   | a1   | a2   | s1    | s2   | v1    | v2   |
|---|------------|------------|----------|-------|-------|------|------|------|-------|------|-------|------|
| 0 | 11<br>(n1) | 22<br>(n2) | 11       | 20.00 | 0.00  | 0.00 | 1.82 | 0.91 | 0.91  | 0.45 | 1.82  | 0.91 |
| 1 | 12         | 22         | 10       | 24.20 | 1.82  | 0.91 | 2.20 | 1.10 | 2.92  | 1.46 | 4.02  | 2.01 |
| 2 | 15         | 21         | 6        | 67.22 | 4.02  | 2.01 | 6.11 | 3.06 | 7.07  | 3.54 | 10.13 | 5.06 |
| 3 | 22         | 17         | -5       | 96.80 | 10.13 | 5.06 | 8.80 | 4.40 | 14.53 | 7.26 | 18.93 | 9.46 |

Hence the two numbers n1 and n2 "meet" on the number line between time units 2 and 3 and the location could be taken as the average of positions (15 + 22 + 21 + 17)/4 = 18.75. The relevant equations for each unit time slice (delta t = 1) are: Equation Set 1: F = 10\*n1\*n2/(l2-l1)\*\*2 a1 = F/n1; a2 = F/n2 s1 = u1 + a1/2; s2 = u2 + a2/2 v1 = u1 + a1; v2 = u2 + a2 If it is found that the average of the last four positions exceeds the position of "crossing", then we could calculate intermediate positions by slicing the last time slice into two and using the following equations (for a half unit time slice, delta t = 1/2): Equation Set 2: F = 10\*n1\*n2/(l2-l1)\*\*2 a1 = F/n1; a2 = F/n2 s1 = u1/2 + a1/8; s2 = u2/2 + a2/8 v1 = u1 + a1/2; v2 = u2 + a2/2 (Note: It may be necessary to calculate intermediate positions by slicing again, delta t = 1/4 or 3/4) and use the appropriate motion equations.) Consider n1 = 11 and n2 = 40:

| t | l1         | 12         | 2 -<br> 1 | F    | u1   | u2   | a1   | a2   | s1   | s2   | v1   | v2   |
|---|------------|------------|-----------|------|------|------|------|------|------|------|------|------|
| 0 | 11<br>(n1) | 40<br>(n2) | 29        | 5.23 | 0.00 | 0.00 | 0.48 | 0.13 | 0.24 | 0.07 | 0.48 | 0.13 |
| 1 | 11         | 40         | 29        | 5.23 | 0.48 | 0.13 | 0.48 | 0.13 | 0.71 | 0.20 | 0.95 | 0.26 |
| 2 | 12         | 40         | 28        | 5.61 | 0.95 | 0.26 | 0.51 | 0.14 | 1.21 | 0.33 | 1.46 | 0.40 |
| 3 | 13         | 40         | 27        | 6.04 | 1.46 | 0.40 | 0.55 | 0.15 | 1.74 | 0.48 | 2.01 | 0.55 |
| 4 | 15         | 40         | 25        | 7.04 | 2.01 | 0.55 | 0.64 | 0.18 | 2.33 | 0.64 | 2.65 | 0.73 |
| 5 | 17         | 39         | 22        | 9.09 | 2.65 | 0.73 | 0.83 | 0.23 | 3.06 | 0.84 | 3.48 | 0.96 |
|   |            |            |           |      |      |      |      |      |      |      |      |      |

| 6 | 20 | 38 | 18  | 13.58  | 3.48  | 0.96 | 1.23  | 0.34 | 4.09  | 1.13 | 4.71  | 1.30 |
|---|----|----|-----|--------|-------|------|-------|------|-------|------|-------|------|
| 7 | 24 | 37 | 13  | 26.04  | 4.71  | 1.30 | 2.37  | 0.65 | 5.89  | 1.62 | 7.08  | 1.95 |
| 8 | 30 | 35 | 5   | 176.00 | 7.08  | 1.95 | 16.00 | 4.40 | 15.08 | 4.15 | 23.08 | 6.35 |
| 9 | 45 | 31 | -14 | 22.45  | 23.08 | 6.35 | 2.04  | 0.56 | 24.10 | 6.63 | 25.12 | 6.91 |
|   |    |    |     |        |       |      |       |      |       |      |       |      |

We find that the average of positions (30+35+45+31)/4 = 35.25 exceeds 35, the last position of n2. Hence to obtain the meeting point more accurately, we recalculate the parameters at t=8 and t = 8.5 as follows:

| 8.5 | 36 | 33 | -3 | 488.89 | 15.08 | 4.15 | 44.44 | 12.22 | 37.30 | 10.26 | 59.52 | 16.37 |
|-----|----|----|----|--------|-------|------|-------|-------|-------|-------|-------|-------|
| 8   | 30 | 35 | 5  | 176.00 | 7.08  | 1.95 | 16.00 | 4.40  | 5.54  | 1.52  | 15.08 | 4.15  |

Hence we can surmise that the two numbers 11 and 40 meet at the location (30 + 36 + 35 + 33)/4 = 33.50. Write a program to accept two natural numbers, carry out the calculations as above and output their meeting location (up to 2 decimal places of accuracy using Rounding down method) under the influence of "gravity".

+ Constraints

1< = L1 < L2 <= 50

+ Input Format

First Line contains two Integer Numbers L1 L2 delimited by space

+ Output

Meeting Point up to 2 decimal places of accuracy using Rounding down method.

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+ Explanation

Example 1

Input

11 22

Output

18.75

Example 2

Input

11 40

Output