

AI assignment2

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Algorithm for converting the problem into CNF

- **TYPE 1 clauses:**

Each edge in the given graph should be present in at-least one of the subgraphs i.e. for an edge i in graph and subgraph j where $1 \leq j \leq k$ So, add clauses-
for each i

$$e_{i,1} \vee e_{i,2} \vee \dots \vee e_{i,k}$$

Complexity $O(kn^2)$

- **TYPE 2 clauses:**

No subgraph should be empty i.e. at least one edge j where $1 \leq j \leq n$ of graph should be present in a subgraph k . So, add clauses-
for each k

$$e_{1,k} \vee e_{2,k} \vee \dots \vee e_{n,k}$$

Complexity $O(kn^2)$

- **TYPE 3 clauses:**

Any edge which is not in the given graph should not be in any of the subgraphs. So, add clauses-

for each e_j not present in the given graph

$$\text{NOT } e_{j,1} \ \& \ \text{NOT } e_{j,2} \ \& \ \dots \ \& \ \text{NOT } e_{j,k}$$

Complexity $O(kn^2)$

- **TYPE 4 clauses:**

Each subgraph should be complete. If an edge from i to j $e_{ij,k}$ is present in subgraph k then $V_{i,k}$ and $V_{j,k}$ should also be present and vice versa should also be true. So, add clauses-
for each $e_{ij,k}$ not present in the given graph

$$e_{ij,k} \iff (V_{i,k} \ \& \ V_{j,k})$$

whose CNF equivalent is $(\text{NOT } V_{i,k} \vee \text{NOT } V_{j,k} \vee e_{ij,k}) \ \& \ (V_{i,k} \vee \text{NOT } e_{ij,k}) \ \& \ (V_{j,k} \vee \text{NOT } e_{ij,k})$
Complexity $O(kn^2)$

- **TYPE 5 clause:**

No subgraph should be superset of the other subgraph i.e. not all vertices of one subgraph should be present in any other subgraph. So, add clauses-

for two subgraphs k_1 and k_2

for each vertex $1 \leq i \leq n$

$$\text{NOT}(V_{1,k_1} \implies V_{1,k_2} \ \& \ \dots \ \& \ V_{i,k_1} \implies V_{i,k_2} \ \& \ V_{n,k_1} \implies V_{n,k_2})$$

Complexity $O(k^2n)$