

Day 1:

Mercury.

opened Franck Hertz Data logger.

Target temperature of the Mercury sample - 145°C

$d = 1\text{cm}$ for mercury.

Set $U_1, U_3 = 1.5\text{dV}$

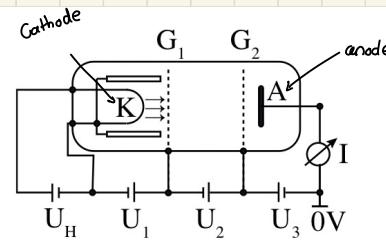
ran software \rightarrow straight line.

$\pm 0.01\text{V}$

$U_2 = 1.48 \pm 0.01\text{V}$

increased $U_1 = 3\text{V}$, right shape but not may peaks before \rightarrow Current = 1

decreased $U_1 = 2.11\text{V}$ \Leftarrow time step 30mV \rightarrow data 1



$\Rightarrow U_2$ Varying from 0 - 30V

Data 2: $U_3 = 1.47 \pm 0.01\text{V}$

$U_1 = 2.09 \pm 0.01\text{V}$

Plotted varying U_2 0 - 30 against Current
for each run (shown in figure 1)

Data 3: $U_3 = 1.53 \pm 0.01\text{V}$

$U_1 = 1.94 \pm 0.01\text{V}$

4:

Tried to find an average of data points and plot average values
but voltage measurements didn't line up.

5:

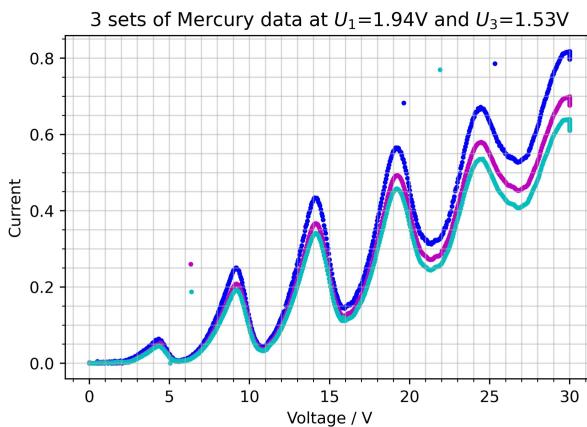
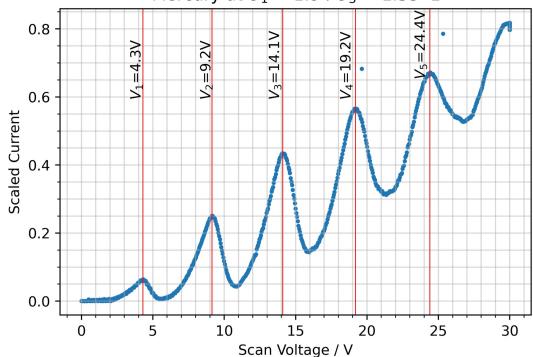


Figure 1

Therefore, measured energy gap for each data set
and averaged. figures (2, 3, 4)

Mercury at $U_1 = 1.94$ $U_3 = 1.53$ 1



Error on each reading was taken to be $\frac{1}{10}$ of smallest increment on graph (0.1V)

$$\Delta V_{21} = V_2 - V_1 = 9.2 - 4.3 = 4.9 \pm 0.1 \text{ V}$$

$$\sigma_{V_{21}} = \sqrt{2} \times 0.1 = 0.14 \text{ V}$$

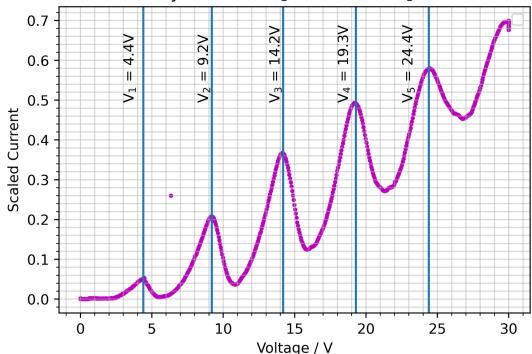
$$\text{or } \sigma_f^2 = \sigma_x^2 + \sigma_y^2 \text{ for } f = xy$$

$$\Delta V_{32} = V_3 - V_2 = 14.1 \pm 0.1 \text{ V}$$

$$\Delta V_{43} = 19.2 \pm 0.1 \text{ V}$$

$$\Delta V_{54} = 24.4 \pm 0.1 \text{ V}$$

Mercury data 2 at $U_1 = 1.94 \text{ V}$ and $U_3 = 1.53 \text{ V}$



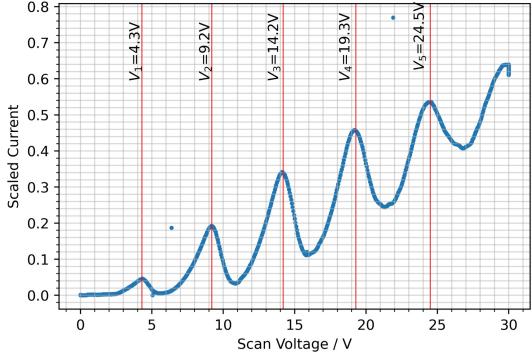
$$\Delta V_{21} = 4.8 \pm 0.1 \text{ V}$$

$$\Delta V_{32} = 5.0 \pm 0.1 \text{ V}$$

$$\Delta V_{43} = 5.1 \pm 0.1 \text{ V}$$

$$\Delta V_{54} = 5.1 \pm 0.1 \text{ V}$$

Mercury at $U_1 = 1.94$ $U_3 = 1.53$ 3



$$\Delta V_{21} = 4.9 \pm 0.1 \text{ V}$$

$$\Delta V_{32} = 5.0 \pm 0.1 \text{ V}$$

$$\Delta V_{43} = 5.1 \pm 0.1 \text{ V}$$

$$\Delta V_{54} = 5.2 \pm 0.1 \text{ V}$$

Explain Graph in Theory ✓

Average:

$$\bar{\Delta V} = 5.0$$

$$\sigma_{\Delta V} = \sqrt{\sum_i \left(\frac{\sigma_{V_i}}{V_i} \right)^2} = 0.1 \Rightarrow \left(\frac{\sigma_f}{f} \right)^2 = \left(\frac{\sigma_x}{x} \right)^2 + \left(\frac{\sigma_y}{y} \right)^2$$

$$\Delta V = (5.0 \pm 0.1) \text{ V}$$

for $f = xy$

We then wrote code to fit parabolas to the data:

The data was split into separate bins for data close to each maxima.

A second order polynomial was then fit to each of the 5 maxima.

$$y = ax^2 + bx + c$$

Each coefficient of this polynomial had its own error from the fit function. This was represented as a Covariance matrix.

$$\begin{pmatrix} \sigma_{aa}^2 & \sigma_{ab}^2 & \sigma_{ac}^2 \\ \sigma_{ab}^2 & \sigma_{bb}^2 & \sigma_{bc}^2 \\ \sigma_{ac}^2 & \sigma_{bc}^2 & \sigma_{cc}^2 \end{pmatrix} \quad \text{Therefore the square root of the diagonal gave the errors}$$

The derivative of this equation would give the maxima when equated to 0.

$$\frac{dy}{dx} = 0 = 2ax + b$$

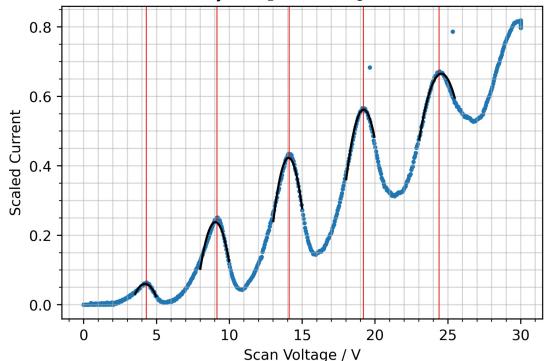
$$x_{\text{max}} = -\frac{b}{2a}$$

With an error given by:

$$\sigma_{\text{max}} = x_{\text{max}} \sqrt{\left(\frac{\sigma_b}{b}\right)^2 + \left(\frac{\sigma_a}{a}\right)^2}$$

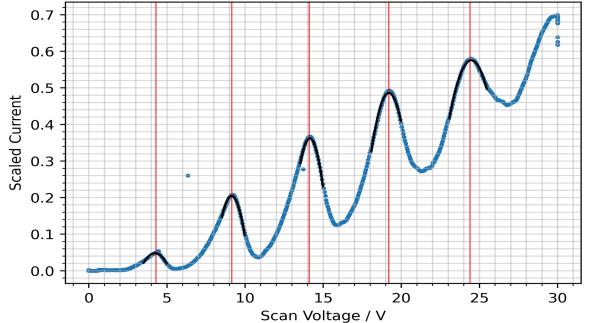
Therefore on a repeated for each parabola, the differences between maxima were calculated with error

Mercury at $U_1 = 1.94$ $U_3 = 1.53$ 1



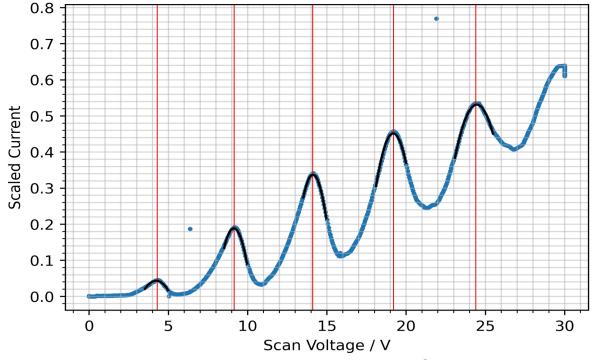
$$\begin{aligned}
 V_1 &= 4.21 \pm 0.03 \text{ V} & y_1 &= -0.06 x^2 + 0.52 x + -1.0445 \\
 V_2 &= 9.04 \pm 0.11 \text{ V} & y_2 &= -0.13 x^2 + 2.28 x + -10.0675 \\
 V_3 &= 14.06 \pm 0.15 \text{ V} & y_3 &= -0.17 x^2 + 4.69 x + -32.5845 \\
 V_4 &= 19.21 \pm 0.52 \text{ V} & y_4 &= -0.14 x^2 + 5.44 x + -51.6891 \\
 V_5 &= 24.55 \pm 0.39 \text{ V} & y_5 &= -0.08 x^2 + 4.03 x + -48.8238
 \end{aligned}$$

Mercury at $U_1 = 1.94$ $U_3 = 1.53$ 2



$$\begin{aligned}
 V_1 &= 4.23 \pm 0.03 \text{ V} & y_1 &= -0.05 x^2 + 0.42 x + -0.8468 \\
 V_2 &= 9.14 \pm 0.07 \text{ V} & y_2 &= -0.15 x^2 + 2.77 x + -12.4380 \\
 V_3 &= 14.14 \pm 0.33 \text{ V} & y_3 &= -0.19 x^2 + 5.27 x + -36.8983 \\
 V_4 &= 19.20 \pm 0.14 \text{ V} & y_4 &= -0.13 x^2 + 4.90 x + -46.5173 \\
 V_5 &= 24.48 \pm 0.06 \text{ V} & y_5 &= -0.08 x^2 + 3.93 x + -47.5330
 \end{aligned}$$

Mercury at $U_1 = 1.94$ $U_3 = 1.53$ 3



$$\begin{aligned}
 V_1 &= 4.23 \pm 0.02 \text{ V} & y_1 &= -0.05 x^2 + 0.38 x + -0.7697 \\
 V_2 &= 9.13 \pm 0.07 \text{ V} & y_2 &= -0.14 x^2 + 2.58 x + -11.6022 \\
 V_3 &= 14.12 \pm 0.09 \text{ V} & y_3 &= -0.17 x^2 + 4.84 x + -33.8538 \\
 V_4 &= 19.18 \pm 0.13 \text{ V} & y_4 &= -0.12 x^2 + 4.79 x + -45.5008 \\
 V_5 &= 24.46 \pm 0.06 \text{ V} & y_5 &= -0.08 x^2 + 3.79 x + -45.8139
 \end{aligned}$$

Using $\sigma_x = \sqrt{\sigma_x^2 + \sigma_y^2}$

$$\Delta V_{21} = 4.83 \pm 0.11 \text{ V}$$

$$\Delta V_{32} = 5.02 \pm 0.19 \text{ V}$$

$$\Delta V_{43} = 5.15 \pm 0.54 \text{ V}$$

$$\Delta V_{54} = 5.34 \pm 0.65 \text{ V}$$

Using $\sigma_m = \frac{1}{\sqrt{N}} \Delta V$

$$\Delta V_{avg} = 5.09 \pm 0.44 \text{ V}$$

$$\Delta V_{21} = 4.91 \pm 0.08 \text{ V}$$

$$\Delta V_{32} = 5.00 \pm 0.34 \text{ V}$$

$$\Delta V_{43} = 5.06 \pm 0.36 \text{ V}$$

$$\Delta V_{54} = 5.28 \pm 0.15 \text{ V}$$

$$\Delta V_{avg} = 5.06 \pm 0.26 \text{ V}$$

$$\Delta V = 5.07 \pm 0.30 \text{ V}$$

$$\Delta V_{21} = 4.90 \pm 0.07 \text{ V}$$

$$\Delta V_{32} = 4.99 \pm 0.11 \text{ V}$$

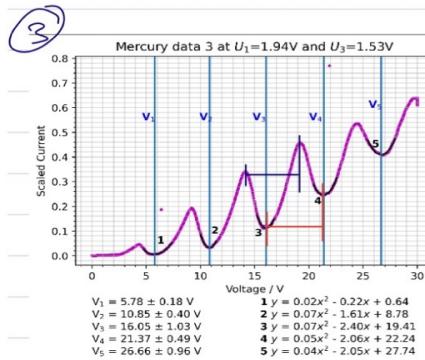
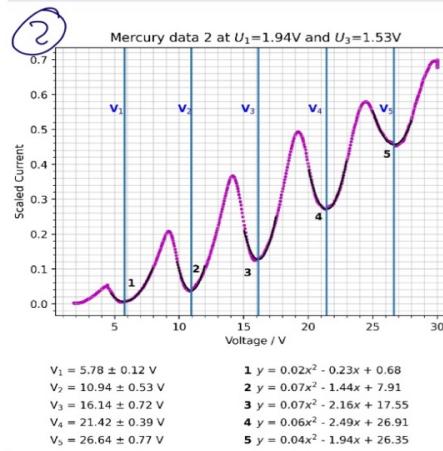
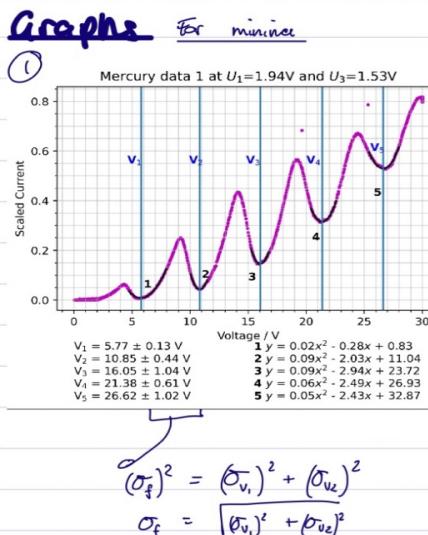
$$\Delta V_{43} = 5.06 \pm 0.16 \text{ V}$$

$$\Delta V_{54} = 5.28 \pm 0.14 \text{ V}$$

$$\Delta V_{avg} = 5.06 \pm 0.13 \text{ V}$$

This was repeated for the minimum to gauge which method gave a value closer to the true energy gap.

This was decided to be the maxima



Therefore, the average energy gap found by fitting functions to the data set is:

$$\Delta V = 5.07 \pm 0.30 \text{ V}$$

Then using $E = \varphi V$

$$\Delta E = (5.07 \pm 0.30) \text{ eV}$$

This corresponds to a wavelength of:

$$E = \frac{hc}{\lambda}, \lambda = \frac{hc}{E} \quad \alpha_\lambda = \lambda \times \frac{\alpha_E}{E}$$

$$\lambda = (245 \pm 15) \text{ nm}$$

This transition is the $6S6S \rightarrow 6SGP$

Ground state configuration:
 $(Xe)(4s)^1(5d)^0(6s)^2$
 $\uparrow \uparrow$
 $l=0 \quad 5 \text{ full}$
 $m_l=0$

This transition is expected to emit a photon with wavelength of $\lambda = 283.652 \text{ nm}$ ground state: 6^1S_0

$l=0, s=0, m_s=0$

1

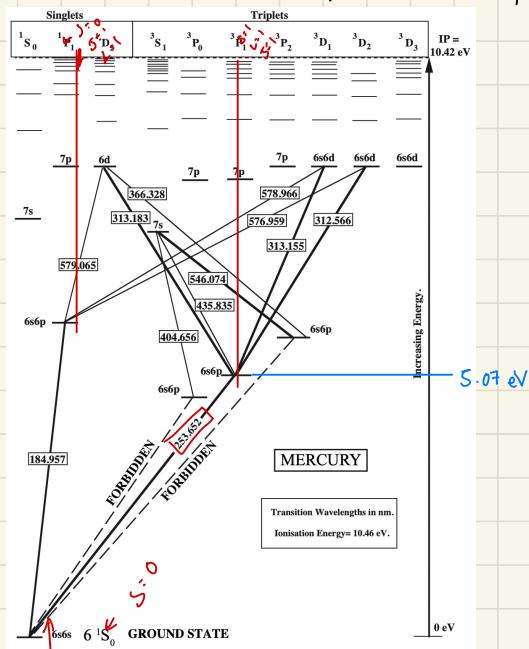
from grotrian diagram
on lab script

New features of Franck Hertz, Gerald Rappor
Klaus Sengstock and Valery BaeV.

Quotes the excitation energy from $6^1S_0 \rightarrow 6^3P$, to be

$$E = 4.89 \text{ eV}$$

which is in the range of our calculation



The $3P_1$ state is excited as this is the allowed transition with the lowest energy. It is important to note that electrons gain energy slowly across the grid and due to the high density of Hg atoms they collide as soon as they have the required energy so the electrons never have enough energy to perform the $1P_1$ transition.

Neon

Room temp: $21.5^{\circ}\text{C} \pm 0.25^{\circ}\text{C}$

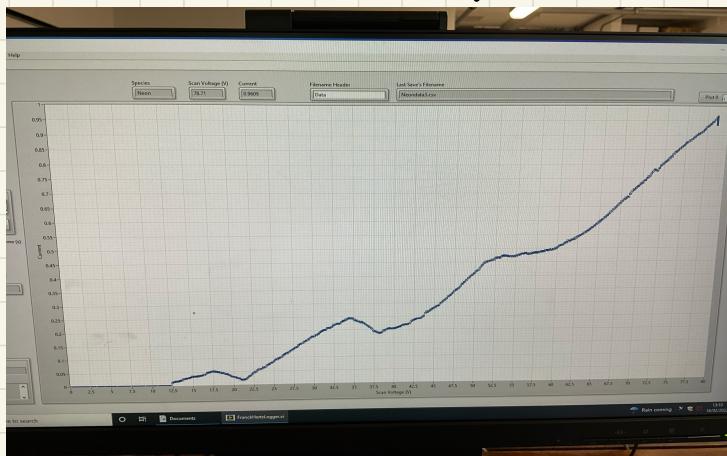
$$U_1 = 2.66 \pm 0.01\text{V} \quad \text{4 neondata1.csv}$$

$$U_3 = 2.83\text{V} \pm 0.01\text{V}$$

$$U_1 = 2.97 \pm 0.01\text{V} \quad \text{4 neondata3.csv}$$

$$U_3 = 2.69 \pm 0.01\text{V}$$

It was found that by applying Voltages U_1 and U_3 to get a 3rd minimum, the amplitudes became too small to measure accurately. These are settled for 2.



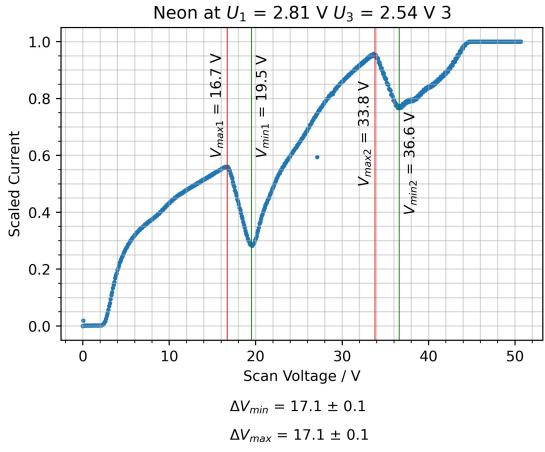
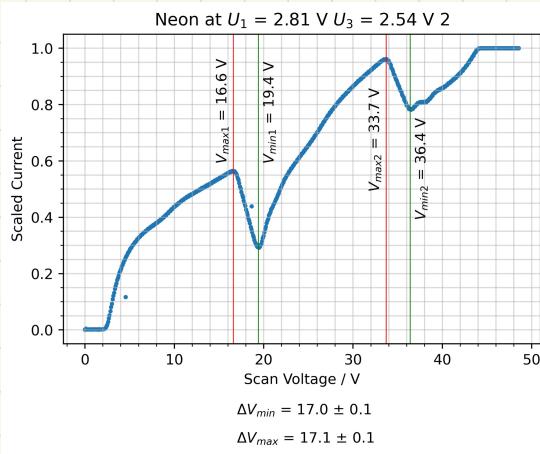
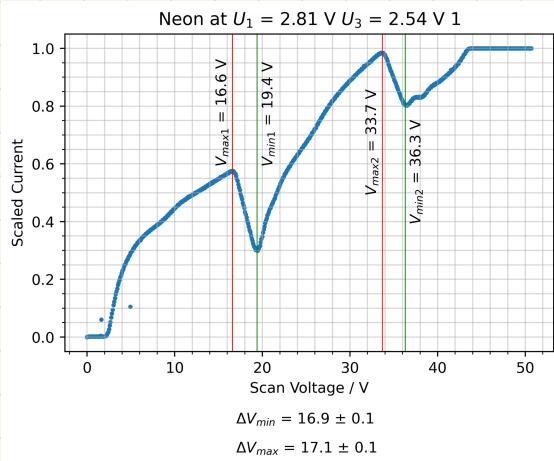
$$\left. \begin{array}{l} U_1 = 2.81 \pm 0.01\text{V} \\ U_3 = 2.54 \pm 0.01\text{V} \end{array} \right\} \begin{array}{l} \text{3 repeats were taken for these values} \\ \text{as these maximized the peaks.} \end{array}$$

at 83 ms interval

$$d = 0.55\text{cm}$$

(4, 5, 6)

We then estimated the minima and maxima for each set of readings:



The errors for each voltage reading was estimated to be $\pm 0.1 \text{ V}$ as when plotting lines this was the smallest distinguishable difference.

Then when finding the difference, this error was propagated

$$\sigma_f^2 = \sigma_x^2 + \sigma_y^2$$

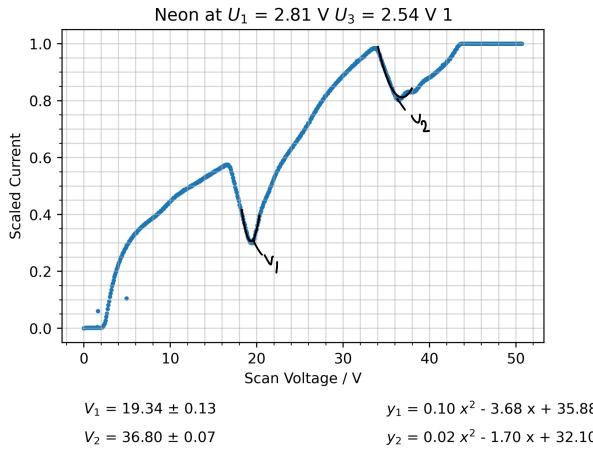
for $f = x + y$

and this was rounded down to 0.1 V to fit to 1dp.

$$\Delta V_{min \text{ avg}} = 17.0 \pm 0.1 \text{ V} \quad \text{~~0.2~~$$

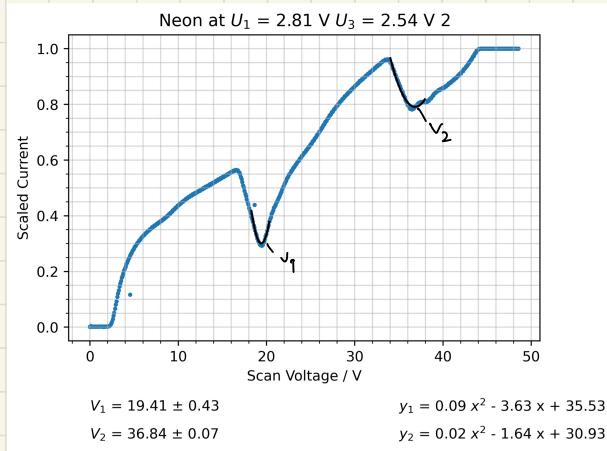
$$\Delta V_{max \text{ avg}} = 17.1 \pm 0.1 \text{ V}$$

This process was then repeated using the same method as mercury to fit parabolas to the minima:

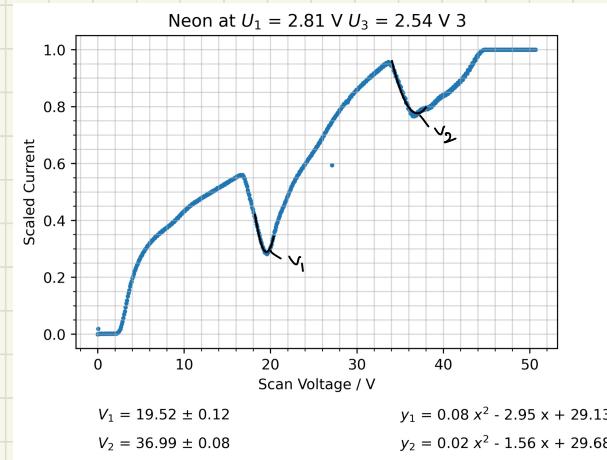


$$\Delta V = 17.46 \pm 0.15$$

all using
propagation \Rightarrow
before



$$\Delta V = 17.43 \pm 0.44$$



$$\Delta V = 17.47 \pm 0.14$$

$\Delta V_{\text{avg}} = 17.45 \pm 0.28$

The most probable excitations are the 10 from the ground state (2^1S_0) to the $3P$ states. These are between $(18.38 - 18.97)$ eV (errors negligible)

The ground state to $3s$ states are also possible but less probable. These energies are from 16.62 to 16.85 eV.

The lowest energy most probable excitation is therefore $\Delta E = (18.38 \pm 0.0000012)$ eV from NIST.

This does not overlap with our value.

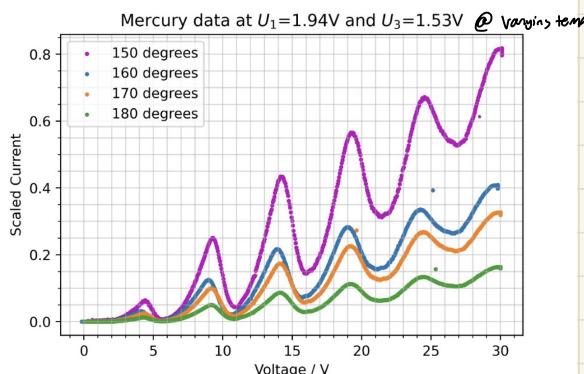
This could be due to a bad fit function or (more likely) the wrong minima was measured. If the other minima was measured the energy gap would be shifted up by ~ 1 eV which would then fall in range.

Orange light was observed which is consistent with electrons falling from $3P \rightarrow 3s$ state.

Equipment resolution not able to detect fine structure of atoms.

3^2P_1

Mercury Temperature Dependence



We repeated the experiment at varying temperatures to investigate a possible temperature dependence. It was observed that an increasing temperature decreased the current readings but the energy gap was unaffected.

This is explained as an increasing temperature increases the random motion of the mercury atoms. Therefore there are more collisions between electrons and atoms. Thus the increase in elastic collisions results in scattered electrons travelling a longer path, thus the time taken to reach the detector is higher and as $I = \frac{dQ}{dt}$

The current is lower.

Electric Field

The electric field can be calculated by:

$$E = \frac{V}{d}$$

And $F = Eq$ so, $F = \frac{Vq}{d}$

Therefore, $W = Fx = \frac{Vq}{d}x$ which is equal to kinetic energy

So $T(x) = \frac{Vq}{d}x$

d is width of grid
 q is electron charge
 x is distance travelled
and V is potential.

$d = 0.01$ m for mercury.

We expect from experiment that each electron collides twice before reaching the end of the accelerating voltage at 10V. (two points)
This is confirmed by:

$$\Theta_0 = \left(\frac{-b}{U_0} \right)^{\frac{1}{3}}$$
$$\Theta_{\Theta_0} = \frac{1}{3} \Theta_0 \times \left(\frac{\alpha_x}{\alpha} \right)$$

$\sqrt{(\frac{\Theta_0}{\Theta})^2 + (\frac{\Theta_{\Theta_0}}{\Theta_0})^2}$

$$T = 5.07 \pm 0.30 \text{ eV}$$

$$d = 0.010 \pm 0.005 \text{ m}$$

Set $V = 10 \text{ V}$

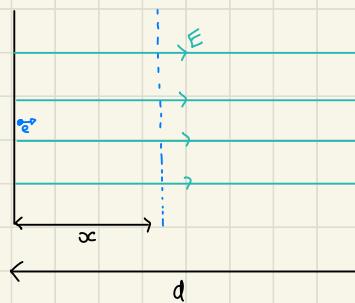
$$T = \frac{10q}{d} \propto$$

$$\sigma_c = \frac{dT}{10q} = 5.07 \times 10^{-3}$$

$$\sigma_{xc} = \sigma_c \sqrt{\left(\frac{\sigma_d}{d}\right)^2 + \left(\frac{\sigma_x}{x}\right)^2}$$

$$= 2.55 \times 10^{-3}$$

$$x = (5.07 \pm 2.55) \text{ mm}$$



high density of Hg makes this approximation valid

Electron travels a distance x to gain the excitation energy before it inelastically collides (assume instant).

At this point the electron has zero kinetic energy and is accelerated a further distance σ_x .

Therefore the number of expected inelastic collisions is:

$$n = \frac{d}{\sigma_x}$$

Therefore for 10V, $n = 1.97$

$\sigma_n = 1.40$ which includes the expected value of $n=2$.

$$\sigma_n = n \sqrt{\left(\frac{\sigma_d}{d}\right)^2 + \left(\frac{\sigma_x}{x}\right)^2}$$

dominant error from measuring d with ruler.
More accurate measurement (caliper?) would decrease error.

20V:

$$x = 2.535 \text{ mm}$$

$$\sigma_x = 1.28 \text{ mm}$$

$$x = (2.54 \pm 1.28) \text{ mm}$$

$$n = \frac{10}{2.54} = 3.94$$

$$\sigma_n = 2.80$$

$$n = (3.94 \pm 2.80) \text{ which includes the expected } n=4$$