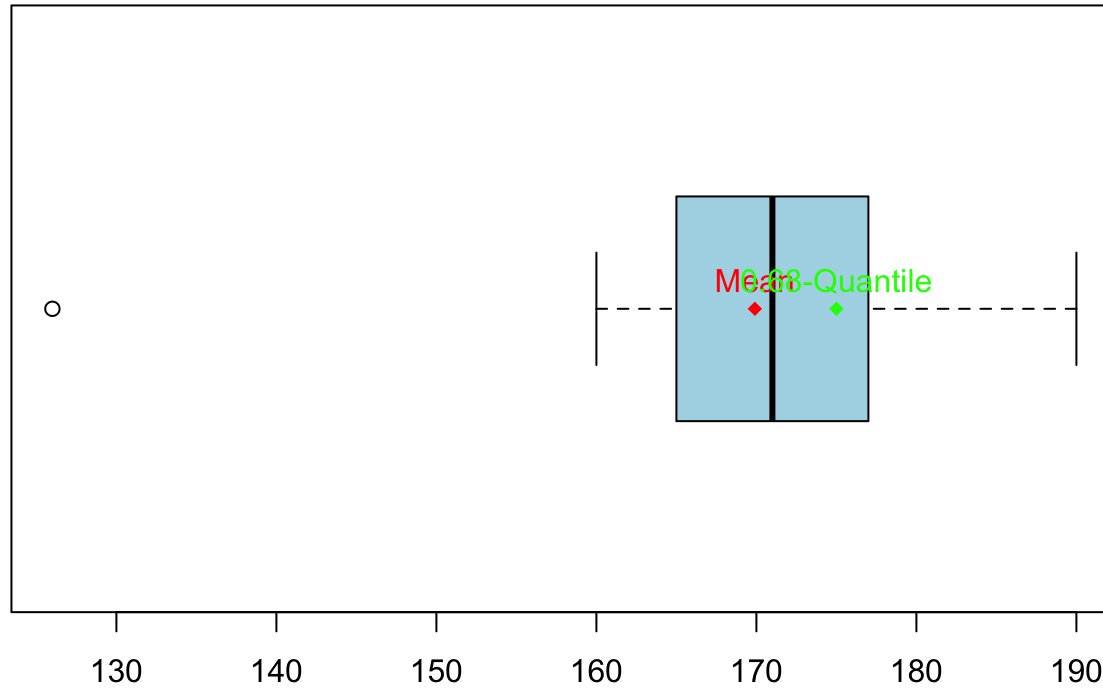


# Quiz1

2024-02-15

## Problem 1

Box Plot with Mean, 0.68-Quantile, and Outliers



## Mean: 169.9048

## 0.68-Quantile: 175

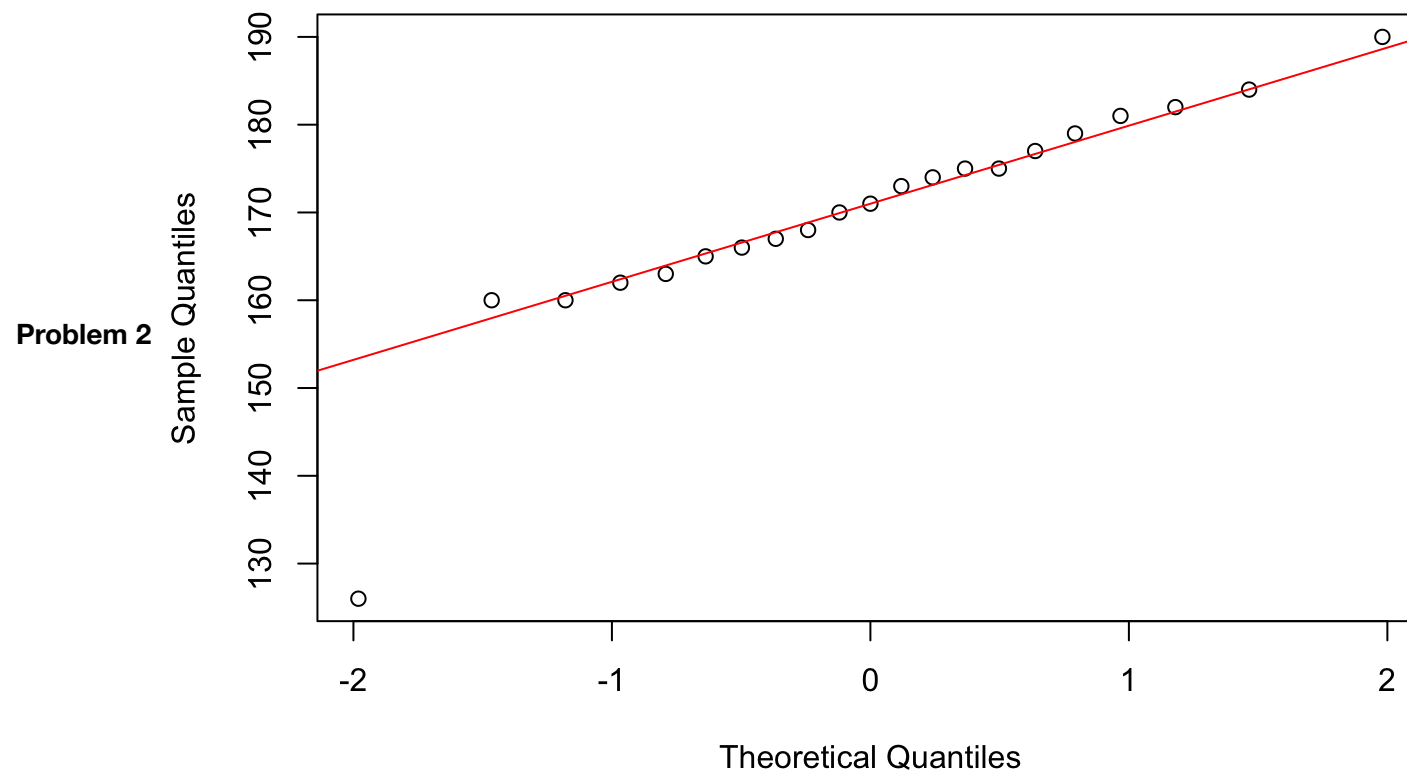
## Q1: 165

## Q2 (Median): 171

## Q3: 177

## Outliers: 126

**Normal Q-Q Plot**



## IQR: 12

## Variance: 168.4905

```
## Standard Deviation: 12.98039
```

```
## Mean: 169.9048
```

```
## Median: 171
```

```
## The distribution is negatively skewed.
```

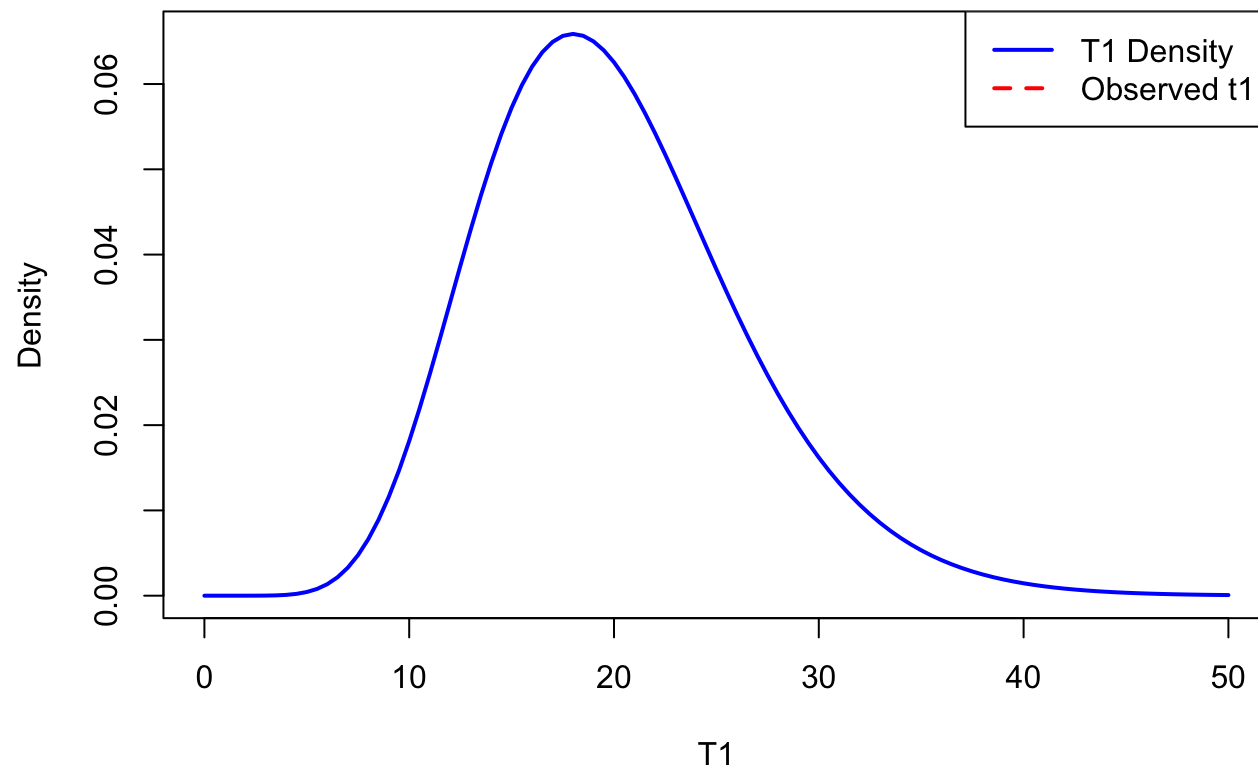
### Problem 3

i

```
## Observed value t1: 130.5769
```

```
##  $P(|T1| \leq |t1|)$ : 1
```

### Density Curve of T1

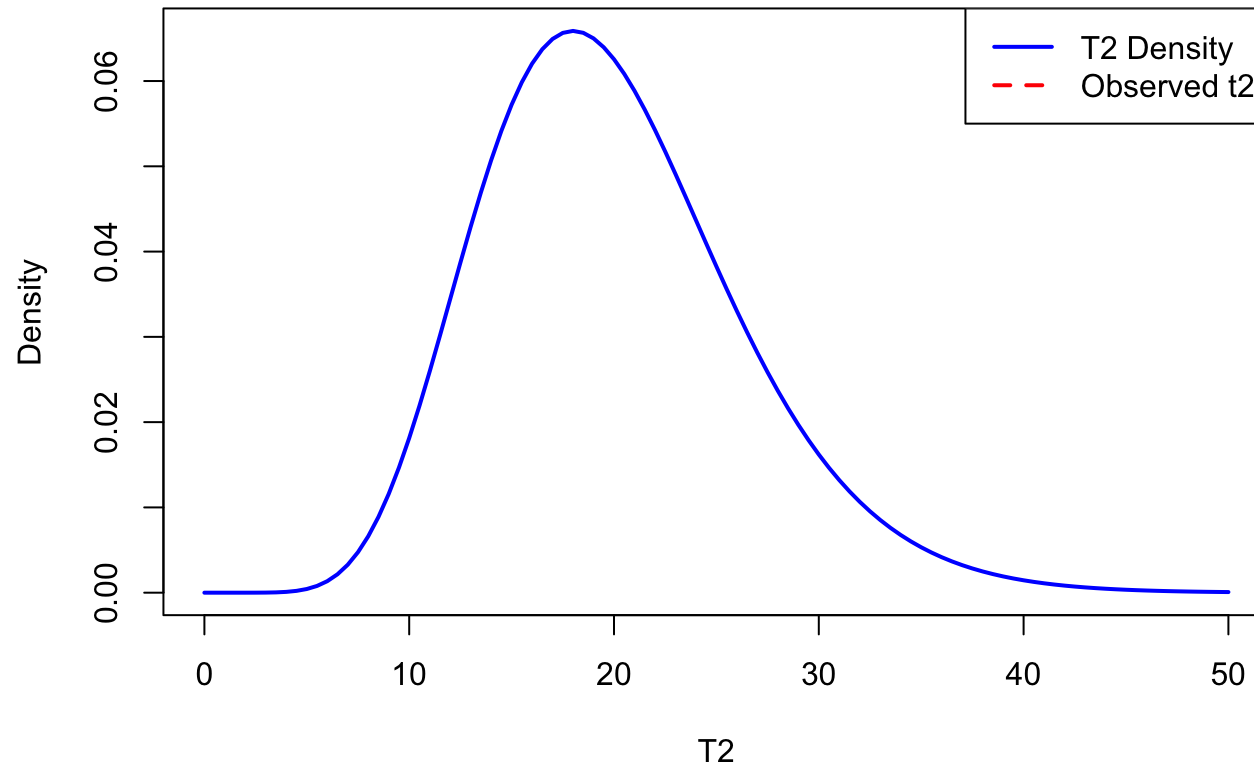


ii

```
## Observed value t2: 129.6081
```

```
## P(|T2| <= |t2|): 1
```

## Density Curve of T2



iii

No they are not different because both are calculated based on chi-square distributions.

iv

t-distribution  $t_3 = -0.984309$   $P(T_3 > t_3) = 0.8316388$

v

student t-distribution  $t_4 = -0.38666112$   $P(T_4 > t_4) = 0.648454$

### Problem 4

i. Linear Combination of Normal Random Variables

ii. Sum of Scaled Chi-Squared Random Variables

- iii. Ratio of Normal to Square Root of a Weighted Sum of Chi-Squared Variables
- iv. Ratio of Two Chi-Squared Variables

**Problem 5**

- i.
- ii. The first one is a normal distribution  $N(0,1)$  The second one is a chi-squared distribution.
- iii.

The mathematical expectation of the first one is  $\sigma^2$  and for the second one the  $(n-1)/n \sigma^2$

- iii. They are not independent and uncorellated because the covariance between  $\mu^2$  and  $\sigma^2$  is zero.