

Linked List 3: Doubly Linked List

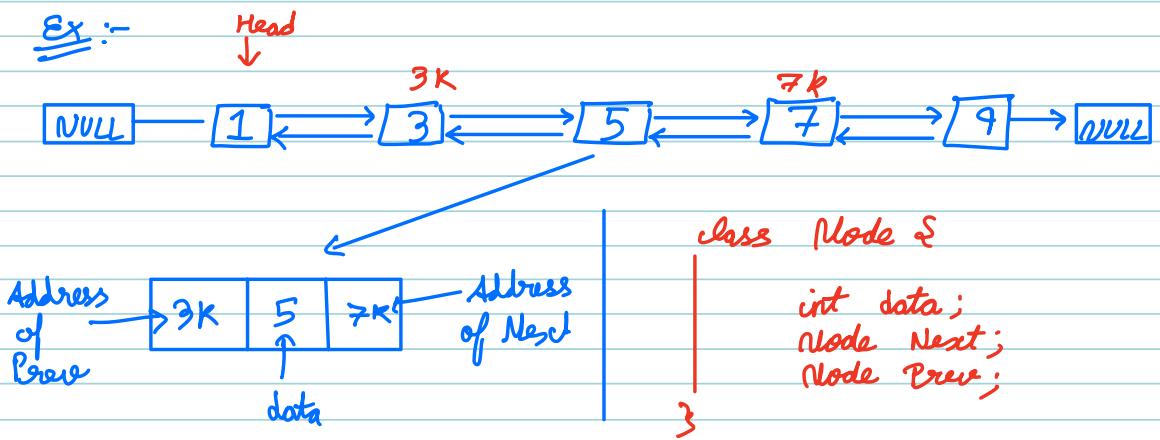
AGENDA

- what is Doubly Linked List ?
- How is Doubly Linked List different from singly linked list ?
- 4 Coding problems related to doubly linked list .

DOUBLY LINKED LIST

↳ A doubly linked list is a type of data structure used in computer science & programming to store & organize a collection of elements, such as nodes. It is similar to a singly linked list but with an additional feature: each node in a doubly linked list contains pointer or references to both the next & the previous nodes in the list.

Ex :-



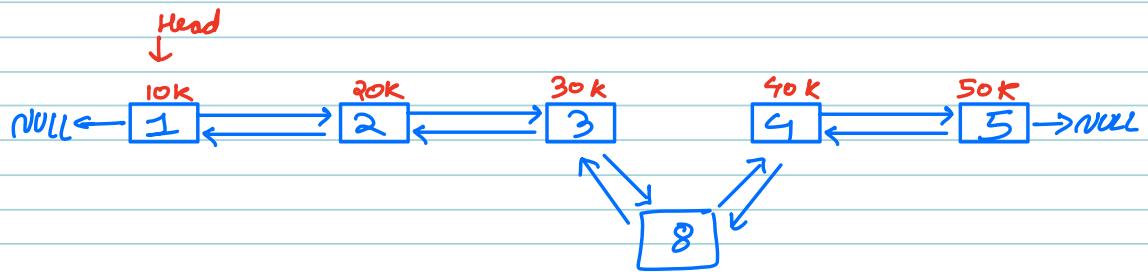
Quiz 1 :- Base Pointer of Head of Doubly Linked List points to:

NULL

Question 1 :- A doubly linked list is given. A node is to be inserted with data x at position K . The range of K is between $0 \leq K \leq N$ where N is length of the doubly linked list.



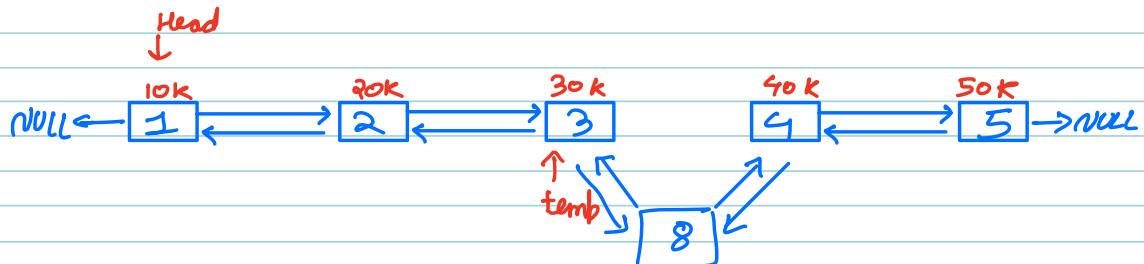
Ex :- $x = 8$, $K = 3$



Quiz 2 :- In a doubly linked list, the no. of pointers affected for an insertion operation b/w two nodes will be?

4

Idea :-



- Steps:-
- ① move temp till prev of insertion
 - ② update Prev & Next of New Node.
 - ③ update Prev of Node ahead of New Node.
 - ④ update Next of Prev of New Node.

nn.next = temp.next

nn.prev = temp;

temp.next.prev = nn;

temp.next = nn;

PSEUDO CODE

nn = new Node(x)

if C head == null) { return nn; }

// Edge Case 1

temp = head;

for(i=1 ; i < K ; i++) {

|
temp = temp.next;
}

nn.next = temp.next

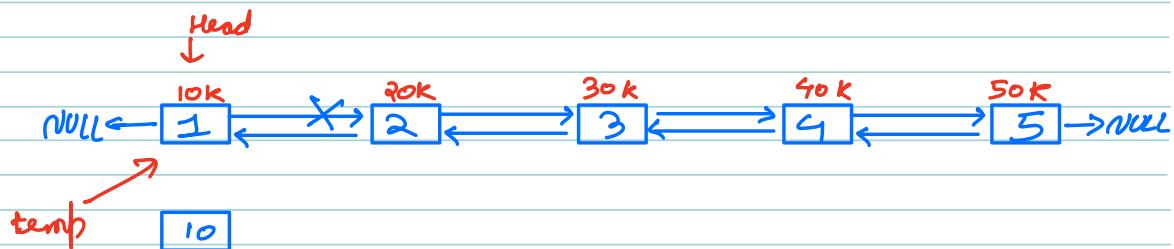
nn.prev = temp;

temp.next.prev = nn;

temp.next = nn;

Edge Case

① $x = 10$, $k = 0$



Correction

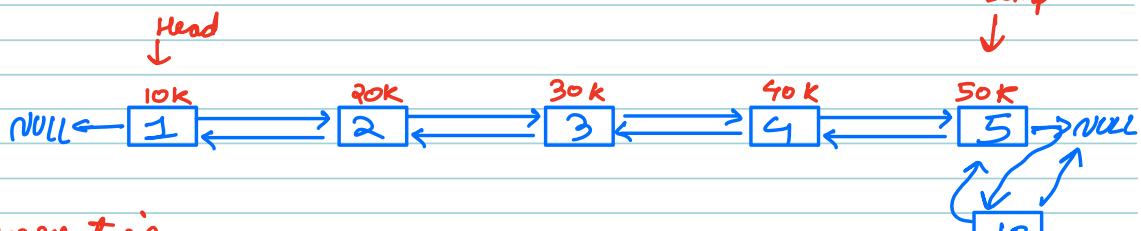
if ($k == 0$) {

 nn.next = head;

 head.prev = nn;

 head = nn;
 return head

② $x = 10$, $k = 5$



correction

 nn.next = temp.next;

 nn.prev = temp;

 if (temp.next != null) {

 temp.next.prev = nn;

 temp.next = nn;

$TC = O(N)$

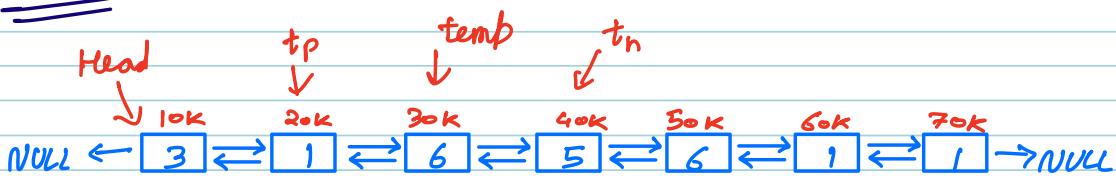
$SC = O(1)$

Question 2 :- We have been given a doubly linked list of length N , we have to delete the first occurrence of data x from the given doubly linked list. If element x is not present, don't do anything.



Ex :- $x = 6$
Head
↓
NULL ← [3] ←→ [1] ←→ [5] ←→ [6] ←→ [6] ←→ [1] ←→ [1] → NULL

Idea



- steps :-
- ① Goto First occurrence.
 - ② Initialize : $\text{temp}.\text{prev} \& \text{temp}.next$
 - ③ Delete

$$tp = \text{temp}.prev;$$

$$tn = \text{temp}.next;$$

$$tp.next = tn;$$

$$tn.prev = tp;$$

PSEUDO CODE

```
temp = head;  
// Searching  
while (temp != null) {  
    if (temp.data == x) {  
        break;  
    }  
    temp = temp.next;  
}  
  
if (temp == null) {  
    return head;  
}  
else if (temp.prev == null && temp.next == null) {  
    head = null;  
    return null;  
}  
else if (temp.prev == null) {  
    temp.next.prev = null  
    temp.next = head;  
    head = temp.next;  
    return head;  
}  
else if (temp.next == null) {  
    temp.prev.next = null  
    temp.prev = head;  
    head = temp.prev;  
    return head;
```

Edge Cases

else S

tp = temp. prev;
tn = temp. next;
tp.next = tn;
tn.prev = tp;

TC \rightarrow OCN)

SC \rightarrow OCD

LRU CACHE

question 3 :- We have been given running stream of integers & the fixed memory of size M , we have to maintain the most recent M elements. In case the current memory is full, we have to delete the last recent elements & insert the current data into the memory (as the most recent item.)

LRU CACHE [Least Recently Used Cache]



Data Stream :- 7 3 2 9 6 10 14 2 15 10 8 11 10 19
Stream ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑ ↑

Max Capacity = 5

Policy:- least Recently used

~~7 3 2 9 6 10 14 15~~

CACHE

↳ Problem:- Need to do something for no. already existing.

Data Stream :- 7 3 2 9 6 10 14 2 15 10 8 11 10 19

 ↑
Correct Way

Max = 5 ele

~~7 3 2 9 6 10 14 15 10 8 11 10 19~~
CACHE

- Steps :-
- ① Insert if capacity < 5
 - ② Delete the element if you got it & existing previously (Basically re-insertion)
 - ③ If got element which is new then Delete LRU & insert new

FLOW CHART

$[x]$ element to insert

Search (x)

x present

x absent

↳ Remove (x)

if (cache.size() == limit) {

↳ Insert-last (x)



↳ Delete-first()

↳ Insert-last (x)

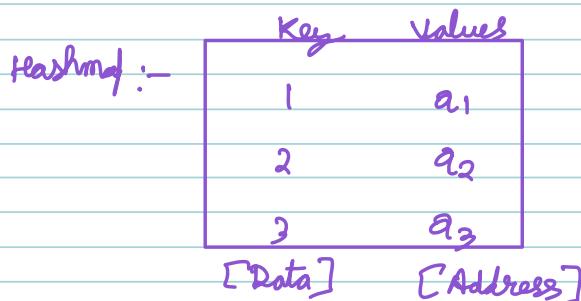
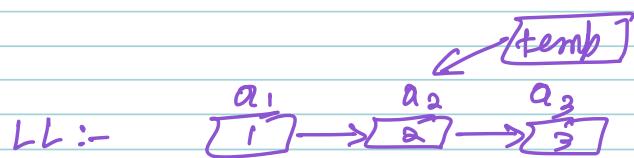
↳ Insert-last (x)

Ques 3 :- what is the behaviour of an LRU cache memory when a new item is inserted & the cache is already full?

↳ New item added & Least recently used will be removed.

⇒ Function which is Required for LRU implementation

<u>operations</u>	Array	Linked-List	Linked List - hashmap
① Search(x)	$O(N)$	$O(N)$	$O(1)$
② Remove(x)	$O(N)$	$O(N)$ tail is maintained	$O(N)$
③ Insert_Last(x)	$O(1)$ arraylist	$O(1)$	$O(1)$
④ Delete_Earst()	$O(N)$	$O(1)$	$O(1)$



* The problem in LL + Hashmap Solution is Removal.
This can be solved using Doubly linked list + Hashmap

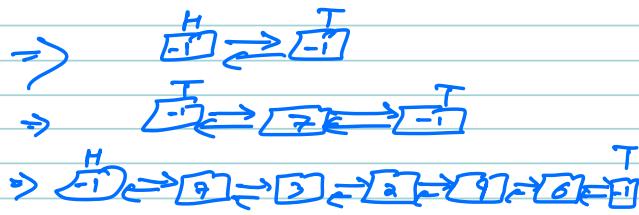
DRY RUN

Data :- \downarrow \downarrow \downarrow \downarrow \downarrow
 7 3 2 9 6 12 14 9 15 19
 Cap=5

7

CACHE

Doubly Linked List



HashMap.

7 → a_1
 3 → a_2
 2 → a_3
 9 → a_4
 6 → a_5

Steps :- ① By default maintain something like this:-



② Check if 7 present [This can be checked using Map]. If not see flow chart & perform operation

③ Run till capacity reaches. If Cap reaches delete from LC & Map. check map for the Node to be deleted [you will get address.]

PSEUDO CODE

Node h = new Node(-1);

Node t = new Node(-1);

h.next = t;
t.prev = H;



HashMap < Int, Node > hm;

Function LRU (int x, int Limit) {

if (hm.contains (x)) {

Node th = hm [x];

Delete Node (th);

Node nn = new Node (x);

Insert-Last (nn, T);

hm [x] = nn;

} else {

if (hm.size () == Limit) {

Node t = h.next;

hm.remove (t.data);

Delete Node (t);

Node nn = new Node (x);

Insert-Last (nn, T);

hm [x] = nn;

void Delete Node (Node temp) {

tp = temp. prev;

tn = temp. next;

tp. next = tn;

tn. prev = tp;

} void Insert Last (Node nn, Node tail) {

tp = tail. prev;

nn. prev = tp;

nn. next = tail;

tp. next = nn;

tail. prev = nn;

TC \rightarrow Constant

Actual Copy

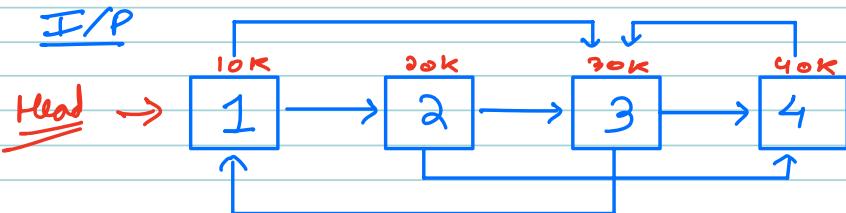
[Deep Copy of linked list]

Question 4 :- We have to create a deep copy of the Doubly Linked List with random pointers. Here there is no certain next & prev pointer, a node can point to some other node.

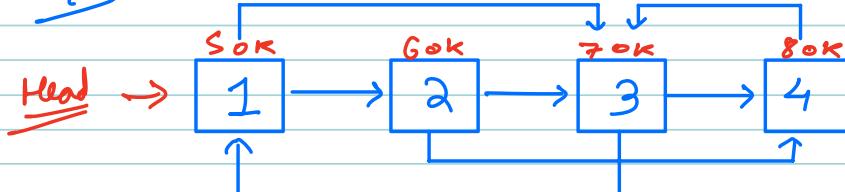
class Node {

```
int data;
Node next;
Node rand;
```

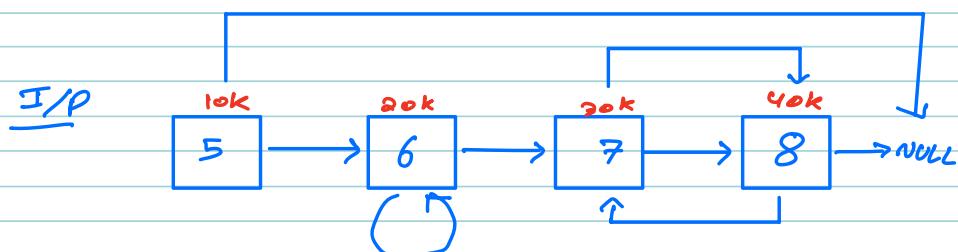
Ex1



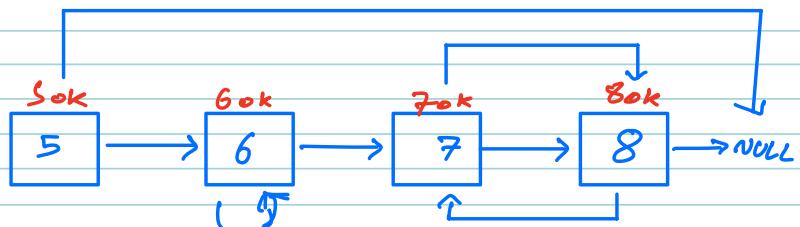
O/P



Ex2 :-



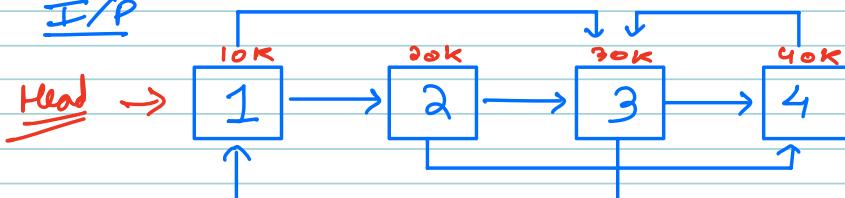
O/P



IDEA

Step 1 :- Create copy of Doubly LL without random pointers.

I/P



Step 2 :- Update Random pointers

Approach 1 :- Use Hashmap

old
↑
Hashmap < Node , Node >
↓
Copy

~~Hash Map~~

10K → 50K
20K → 60K
30K → 70K
40K → 80K

(⇒) Code for using map to update random

temp = old.random;
new.random = hashmap.get(temp);

PSEUDO CODE

```
while( old != null){  
    temp = old.random  
    New.random = map.get(temp);  
    old = old.next;  
    new = new.next;  
}
```

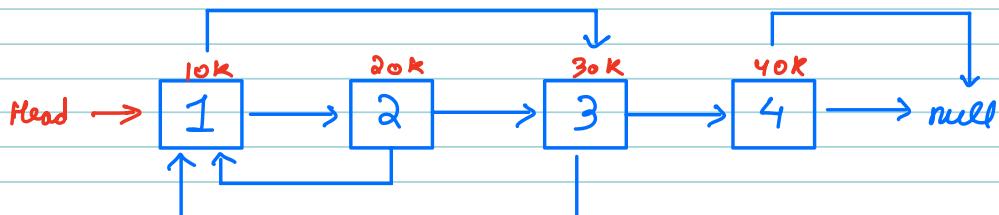
TC $\rightarrow O(N)$

SC $\rightarrow O(N)$

\rightarrow map

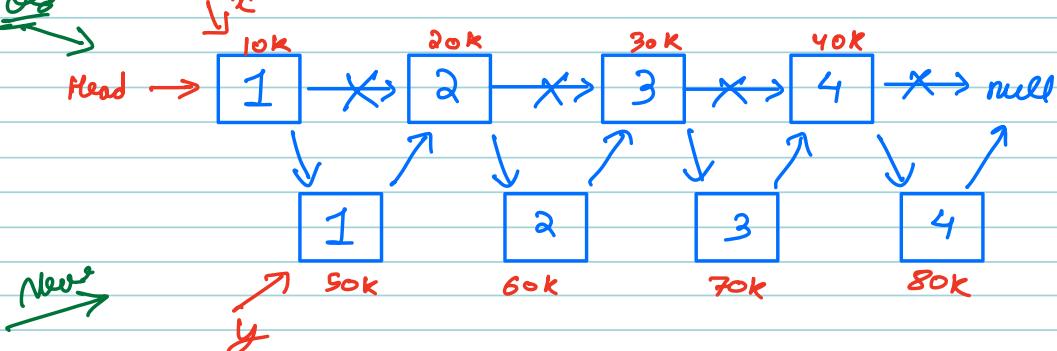
⇒ Constraint :- Do it in a constant space.

Approach 2



Step 1:- Insert new Nodes in b/w odd

old
Insert new Nodes.



Code

while ($x \neq \text{null}$) {

$y = \text{new Node}(x.\text{data});$

$y.\text{next} = x.\text{next};$

$x.\text{next} = y;$

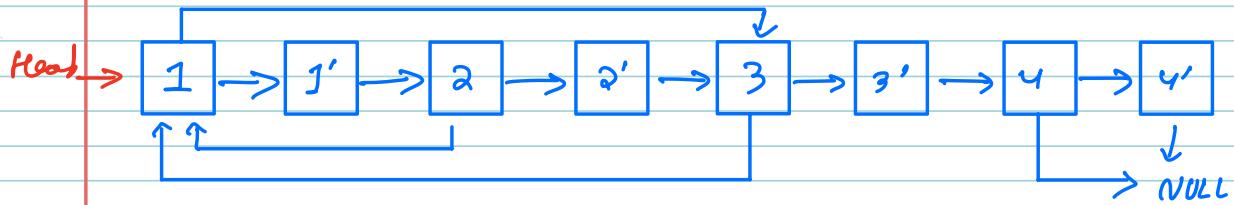
$x = x.\text{next}.\text{next};$

3

old

* All ^{old} Node have random pointers intact.
while New Nodes have not assigned random pointers.

Step 2 :- update Random pointer of newly created nodes.



magical link
temp.next.random = temp.random.next

Pseudo Code

```
temp = head;  
while (temp != null){
```

 else if
 temp.next.random =
 temp.random.next;

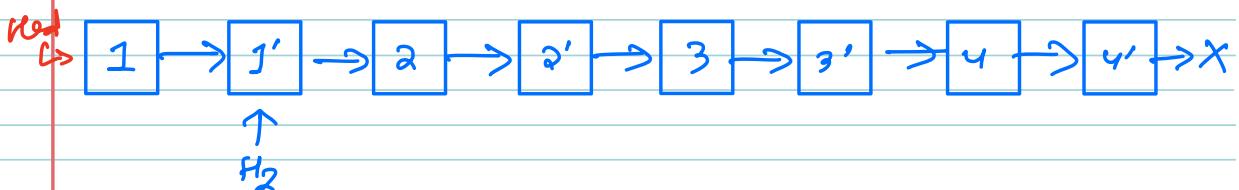
 temp = temp.next.next;

Edge Case

Correction :-

```
if (temp.random == null),  
    temp.next.random = null;
```

Step 3:- Separate old & new LI.



$H_2 = \text{head} \cdot \text{next};$

$x = \text{head};$

$y = H_2;$

while ($x \neq \text{null}$) {

$x \cdot \text{next} = x \cdot \text{next} \cdot \text{next};$

if ($y \cdot \text{next} \neq \text{null}$) {

$y \cdot \text{next} = y \cdot \text{next} \cdot \text{next};$

3

$x = x \cdot \text{next};$

$y = y \cdot \text{next};$

y

return $H_2;$

TC $\rightarrow O(N)$

SC $\rightarrow O(1)$

Ques 4:- what is the time complexity of creating a deep copy of a doubly linked list consists of N nodes with random pointers using extra space?
 $\hookrightarrow O(N)$