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AI24BTECH11015 - Harshvardhan Patidar

Ouestion:

The x-coordinate of a point **P** twice its y-coordinate. If **P** is equidistant from the points $\mathbf{Q}\begin{pmatrix}2 & -5\end{pmatrix}$ and $\mathbf{R}\begin{pmatrix}-3 & 6\end{pmatrix}$, find the coordinates of **P**.

Solution:

Variable	Description
P	$\begin{pmatrix} 2a & a \end{pmatrix}$ point
Q	(2 -5) point
R	$\begin{pmatrix} -3 & 6 \end{pmatrix}$ point
a	y-coordinate of P

TABLE 0: Variables Used

Now, since P is equidistant from Q and R,

$$||P - Q|| = ||P - R|| \tag{0.1}$$

$$\sqrt{(P-Q)^T (P-Q)} = \sqrt{(P-R)^T (P-R)}$$
 (0.2)

$$(P-Q) = {2a-2 \choose a+5}, (P-R) = {2a+3 \choose a-6}$$

Putting values into equation 0.2 and squaring,

$$(2a-2)^2 + (a+5)^2 = (2a+3)^2 + (a-6)^2$$
(0.3)

$$a = 8 \tag{0.4}$$

So.

$$\mathbf{P} = \begin{pmatrix} 16 \\ 8 \end{pmatrix}$$

