Definite Integrals and Applications of Integrals

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Section-B — JEE Main / AIEEE

- 1) $\int_0^{10\pi} |\sin(x)| dx$ is
 - a) 20
 - b) 8
 - c) 10
 - d) 18

(2002)

- 2) $I_n = \int_0^\infty \tan^n(x) dx$ then $\lim_{n \to \infty} n(I_n + I_{n+2})$ equals
 - a) $\frac{1}{2}$
 - b) 1
 - c) ∞
 - d) zero

(2002)

- 3) $\int_{0}^{z} (x^2) dx$ is

 - a) $2 \sqrt{2}$ b) $2 + \sqrt{2}$ c) $\sqrt{2} 1$ d) $-\sqrt{2} \sqrt{3} + 5$
 - (2002)
- 4) $\int_{-\pi}^{\pi} \frac{2x(1+\sin(x))}{1+\cos^{2}(x)} dx \text{ is}$ a) $\frac{\pi^{2}}{4}$ b) π^{2}

 - c) zero
 - d) $\frac{\pi}{2}$

(2002)

- 5) If y = f(x) makes +ve intercept of 2 and 0 unit on x and y axes and encloses an area of $\frac{3}{4}$ square unit with the axes then $\int_{0}^{\pi} x f'(x) dx$ is
 - a) $\frac{3}{2}$
 - b) 1
 - d) $-\frac{3}{4}$

(2002)

6) The area bounded by the curves $y = \ln(x)$, $y = \ln(|x|), y = |\ln(x)| \text{ and } y = |\ln(|x|)|$

- a) 4 sq. units
- b) 6 sq. units
- c) 10 sq. units
- d) none of these

(2002)

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- 7) The area of the region bounded by the curves y = |x - 1| and y = 3 - |x| is
 - a) 6 sq. units
 - b) 2 sq. units
 - c) 3 sq. units
 - d) 4 sq. units

(2003)

8) If f(a+b-x) = f(x) then $\int_{a}^{b} xf(x) dx$ is equal

a)
$$\frac{a+b}{2} \int_{a}^{b} f(a+b+x) dx$$

b)
$$\frac{a+b}{2} \int_{a}^{b} f(b-x) dx$$

c)
$$\frac{a+b}{2} \int_{a}^{b} f(x) dx$$

d)
$$\frac{b-a}{2} \int_{a}^{b} f(x) dx$$

(2003)

- 9) Let f(x) be a function satisfying f'(x) = f(x)with f(0) = 1 and g(x) be a function that satisfies $f(x) + g(x) = x^2$. Then the value of the integral $\int_{a}^{b} f(x) g(x) dx$, is

10) The value of the integral $I = \int_{0}^{x} (x) (1-x)^{n} dx$

is

a)
$$\frac{1}{n+1} + \frac{1}{n+2}$$

b) $\frac{1}{n+1}$

c)
$$\frac{1}{n+2}$$

d) $\frac{1}{n+1} - \frac{1}{n+2}$

(2003)

11)
$$\lim_{n \to \infty} \sum_{r=1}^{n} \frac{1}{n} e^{\frac{r}{n}}$$
 is a) $e + 1$

- b) e 1
- c) $1 e^{-\frac{1}{2}}$
- d) *e*

(2004)

12) The value of
$$\int_{-2}^{3} |1 - x^2| dx$$
 is

- a) $\frac{1}{3}$ b) $\frac{14}{3}$ c) $\frac{7}{3}$ d) $\frac{28}{3}$

(2004)

13) The value of
$$I = \int_{0}^{\frac{\pi}{2}} \frac{(\sin(x) + \cos(x))^{2}}{\sqrt{1 + \sin(2x)}} dx$$
 is

- a) 3
- b) 1
- c) 2
- d) 0

(2004)

14) If
$$\int_{0}^{\pi} xf(\sin(x)) dx = A \int_{0}^{\frac{\pi}{2}} f(\sin(x)) dx$$
, then A is

- a) 2π
- b) π
- c) $\frac{\pi}{4}$ d) 0

(2004)

15) If
$$f(x) = \frac{e^x}{1+e^x}$$
, $I_1 = \int_{f(-a)}^{f(a)} (x) g(x(1-x)) dx$ and

 $I_2 = \int_{f(-a)}^{f(a)} g(x(1-x)) dx, \text{ then the value of } \frac{I_2}{I_1} \text{ is}$ a) 1

- b) -3
- c) -1
- d) 2

(2004)