

CHAPTER 10

Simple Harmonic Motion (Oscillations)

Section-A

JEE Advanced/ IIT-JEE

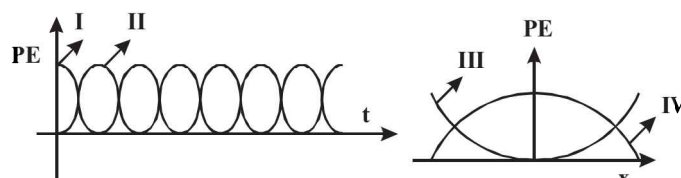
A Fill in the Blanks

1. An object of mass 0.2 kg executes simple harmonic oscillation along the x -axis with a frequency of $(25/\pi)$ Hz. At the position $x = 0.04$, the object has Kinetic energy of 0.5 J and potential energy 0.4 J. The amplitude of oscillations ism.
(1994 - 2marks)

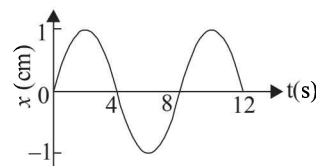
C MCQs with One Correct Answer

1. Two bodies M and N of equal masses are suspended from two separate massless springs of spring constants k_1 and k_2 respectively. If the two bodies oscillate vertically such that their maximum velocities are equal, the ratio of the amplitude of vibration of M to that of N is (1988 - 1mark)
 - (a) $\frac{k_1}{k_2}$
 - (b) $\sqrt{k_1/k_2}$
 - (c) $\frac{k_2}{k_1}$
 - (d) $\sqrt{k_2/k_1}$
2. A particle free to move along the x -axis has potential energy given by $U(x) = k[1 - \exp(-x^2)]$ for $-\infty \leq x \leq +\infty$, where k is a positive constant of appropriate dimensions. Then (1999S - 2marks)
 - (a) at points away from the origin, the particle is in unstable equilibrium
 - (b) for any finite nonzero value of x , there is a force directed away from the origin
 - (c) if its total mechanical energy is $k/2$, it has its minimum kinetic energy at the origin.
 - (d) for small displacements from $x = 0$, the motion is simple harmonic
3. The period of oscillation of a simple pendulum of length L suspended from the roof of a vehicle which moves without friction down an inclined plane of inclination α , is given by
 - (a) $2\pi\sqrt{\frac{L}{g \cos \alpha}}$
 - (b) $2\pi\sqrt{\frac{L}{g \sin \alpha}}$
 - (c) $2\pi\sqrt{\frac{L}{g}}$
 - (d) $2\pi\sqrt{\frac{L}{g \tan \alpha}}$
4. A particle executes simple harmonic motion between $x = -A$ and $x = +A$. The time taken for it to go from 0 to $A/2$ is T_1 and to go from $A/2$ to A is T_2 . Then (2001S)
 - (a) $T_1 < T_2$
 - (b) $T_1 > T_2$
 - (c) $T_1 = T_2$
 - (d) $T_1 = 2T_2$

5. For a particle executing SHM the displacement x is given by $x = A \cos \omega t$. Identify the graph which represents the variation of potential energy (PE) as a function of time t and displacement x (2003S)

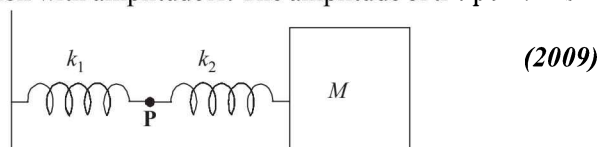


- (a) I, III
 - (b) II, IV
 - (c) II, III
 - (d) I, IV
6. A simple pendulum has time period T_1 . The point of suspension is now moved upward according to the relation $y = Kt^2$, ($K = 1 \text{ m/s}^2$) where y is the vertical displacement. The time period now becomes T_2 . The ratio of $\frac{T_1^2}{T_2^2}$ is ($g = 10 \text{ m/s}^2$) (2005S)
 - (a) 5/6
 - (b) 6/5
 - (c) 1
 - (d) 4/5
 7. The x - t graph of a particle undergoing simple harmonic motion is shown below. The acceleration of the particle at $t = 4/3 \text{ s}$ is (2009)



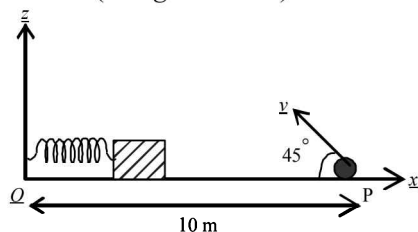
- (a) $\frac{\sqrt{3}}{32} \pi^2 \text{ cm/s}^2$
 - (b) $-\frac{\pi^2}{32} \text{ cm/s}^2$
 - (c) $\frac{\pi^2}{32} \text{ cm/s}^2$
 - (d) $-\frac{\sqrt{3}}{32} \pi^2 \text{ cm/s}^2$
8. A uniform rod of length L and mass M is pivoted at the centre. Its two ends are attached to two springs of equal spring constants k . The springs are fixed to rigid supports as shown in the figure, and the rod is free to oscillate in the horizontal plane. The rod is gently pushed through a small angle θ in one direction and released. The frequency of oscillation is (2009)
 - (a) $\frac{1}{2\pi} \sqrt{\frac{2k}{M}}$
 - (b) $\frac{1}{2\pi} \sqrt{\frac{k}{M}}$
 - (c) $\frac{1}{2\pi} \sqrt{\frac{6k}{M}}$
 - (d) $\frac{1}{2\pi} \sqrt{\frac{24k}{M}}$

9. The mass M shown in the figure oscillates in simple harmonic motion with amplitude A . The amplitude of the point P is



(2009)

- (a) $\frac{k_1 A}{k_2}$ (b) $\frac{k_2 A}{k_1}$ (c) $\frac{k_1 A}{k_1 + k_2}$ (d) $\frac{k_2 A}{k_1 + k_2}$
10. A point mass is subjected to two simultaneous sinusoidal displacements in x -direction, $x_1(t) = A \sin \omega t$ and $x_2(t) = A \sin\left(\omega t + \frac{2\pi}{3}\right)$. Adding a third sinusoidal displacement $x_3(t) = B \sin(\omega t + \phi)$ brings the mass to a complete rest. The values of B and ϕ are (2011)
- (a) $\sqrt{2}A, \frac{3\pi}{4}$ (b) $A, \frac{4\pi}{3}$ (c) $\sqrt{3}A, \frac{5\pi}{6}$ (d) $A, \frac{\pi}{3}$
11. A small block is connected to one end of a massless spring of un-stretched length 4.9 m. The other end of the spring (see the figure) is fixed. The system lies on a horizontal frictionless surface. The block is stretched by 0.2 m and released from rest at $t = 0$. It then executes simple harmonic motion with angular frequency $\omega = \pi/3$ rad/s. Simultaneously at $t = 0$, a small pebble is projected with speed v from point P at an angle of 45° as shown in the figure. Point P is at a horizontal distance of 10 m from O . If the pebble hits the block at $t = 1$ s, the value of v is (take $g = 10 \text{ m/s}^2$) (2012)

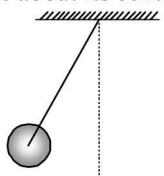


- (a) $\sqrt{50} \text{ m/s}$ (b) $\sqrt{51} \text{ m/s}$
(c) $\sqrt{52} \text{ m/s}$ (d) $\sqrt{53} \text{ m/s}$

D MCQs with One or More than One Correct

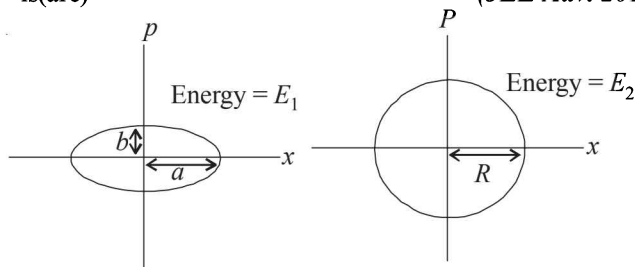
1. A particle executes simple harmonic motion with a frequency f . The frequency with which its kinetic energy oscillates is (1987 - 2marks)
- (a) $f/2$ (b) f
(c) $2f$ (d) $4f$
2. A linear harmonic oscillator of force constant $2 \times 10^6 \text{ N/m}$ and amplitude 0.01 m has a total mechanical energy of 160 J. Its (1989 - 2 Mark)
- (a) maximum potential energy is 100 J
(b) maximum kinetic energy is 100 J
(c) maximum potential energy is 160 J
(d) maximum potential energy is zero
3. A uniform cylinder of length L and mass M having cross sectional area A is suspended, with its length vertical, from a fixed point by a massless spring, such that it is half-submerged in a liquid of density ρ at equilibrium position. When the cylinder is given a small downward push and released it starts oscillating vertically with small amplitude. If the force constant of the spring is k , the frequency of oscillation of the cylinder is (1990 - 2mark)
- (a) $\frac{1}{2\pi} \left(\frac{k - A\rho g}{M} \right)^{1/2}$ (b) $\frac{1}{2\pi} \left(\frac{k + A\rho g}{M} \right)^{1/2}$
(c) $\frac{1}{2\pi} \left(\frac{k + \rho g L}{M} \right)^{1/2}$ (d) $\frac{1}{2\pi} \left(\frac{k + A\rho g}{A\rho g} \right)^{1/2}$
4. A highly rigid cubical block A of small mass M and side L is fixed rigidly on to another cubical block B of the same dimensions and of low modulus of rigidity η such that the lower face of A completely covers the upper face of B . The lower face of B is rigidly held on a horizontal surface. A small force F is applied perpendicular to one of the sides faces of A . After the force is withdrawn, block A executes small oscillations the time period of which is given by (1992 - 2mark)
- (a) $2\pi\sqrt{M\eta L}$ (b) $2\pi\sqrt{\frac{M\eta}{L}}$ (c) $2\pi\sqrt{\frac{ML}{\eta}}$ (d) $2\pi\sqrt{\frac{M}{\eta L}}$
5. One end of a long metallic wire of length L is tied to the ceiling. The other end is tied to a massless spring of spring constant K . A mass m hangs freely from the free end of the spring. The area of cross-section and the Young's modulus of the wire are A and Y respectively. If the mass is slightly pulled down and released, it will oscillate with a time period T equal to: (1993-2marks)
- (a) $2\pi(m/K)^{1/2}$ (b) $2\pi\sqrt{\frac{m(YA + KL)}{YAK}}$
(c) $2\pi[(mYA/KL)^{1/2}]$ (d) $2\pi[(mL/YA)^{1/2}]$
6. A particle of mass m is executing oscillations about the origin on the x axis. Its potential energy is $V(x) = k|x|^3$ where k is a positive constant. If the amplitude of oscillation is a , then its time period T is (1998S - 2marks)
- (a) proportional to $1/\sqrt{a}$ (b) independent of a
(c) proportional to \sqrt{a} (d) proportional to $a^{3/2}$
7. Three simple harmonic motions in the same direction having the same amplitude a and same period are superposed. If each differs in phase from the next by 45° , then. (1999S - 3marks)
- (a) the resultant amplitude is $(1 + \sqrt{2})a$
(b) the phase of the resultant motion relative to the first is 90°
(c) the energy associated with the resulting motion is $(3 + 2\sqrt{2})$ times the energy associated with any single motion
(d) the resulting motion is not simple harmonic.
8. The function $x = A \sin^2 \omega t + B \cos^2 \omega t + C \sin \omega t \cos \omega t$ represent SHM for which of the option(s) (2006 - 5M, -1)
- (a) for all value of A, B and C ($C \neq 0$)
(b) $A = B, C = 2B$
(c) $A = -B, C = 2B$
(d) $A = B, C = 0$

9. A metal rod of length 'L' and mass 'm' is pivoted at one end. A thin disc of mass 'M' and radius 'R' (<L) is attached at its center to the free end of the rod. Consider two ways the disc is attached: (case A). The disc is not free to rotate about its centre and (case B) the disc is free to rotate about its centre. The rod disc system performs SHM in vertical plane after being released from the same displaced position. Which of the following statement(s) is (are) true? (2011)



- (a) Restoring torque in case A = Restoring torque in case B
 (b) restoring torque in case A < Restoring torque in case B
 (c) Angular frequency for case A > angular frequency for case B.
 (d) Angular frequency for case A < Angular frequency for case B.

10. Two independent harmonic oscillators of equal mass are oscillating about the origin with angular frequencies ω_1 and ω_2 and have total energies E_1 and E_2 , respectively. The variations of their momenta p with positions x are shown in the figures. If $\frac{a}{b} = n^2$ and $\frac{a}{R} = n$, then the correct equation(s) is(are) (JEE Adv. 2015)

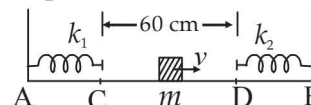
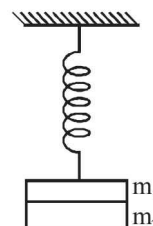


- (a) $E_1 \omega_1 = E_2 \omega_2$ (b) $\frac{\omega_2}{\omega_1} = n^2$
 (c) $\omega_1 \omega_2 = n^2$ (d) $\frac{E_1}{\omega_1} = \frac{E_2}{\omega_2}$
11. A block with mass M is connected by a massless spring with stiffness constant k to a rigid wall and moves without friction on a horizontal surface. The block oscillates with small amplitude A about an equilibrium position x_0 . Consider two cases: (i) when the block is at x_0 ; and (ii) when the block is at $x = x_0 + A$. In both the cases, a particle with mass m (<M) is softly placed on the block after which they stick to each other. Which of the following statement(s) is (are) true about the motion after the mass m is placed on the mass M? (JEE Adv. 2016)

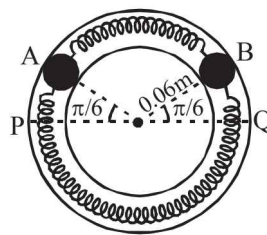
- (a) The amplitude of oscillation in the first case changes by a factor of $\sqrt{\frac{M}{m+M}}$, whereas in the second case it remains unchanged.
 (b) The final time period of oscillation in both the cases is same.
 (c) The total energy decreases in both the cases.
 (d) The instantaneous speed at x_0 of the combined masses decreases in both the cases

E Subjective Problems

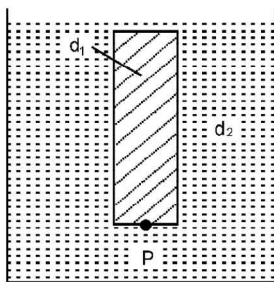
1. A mass M attached to a spring, oscillates with a period of 2sec. If the mass is increased by 2 kg the period increases by one sec. Find the initial mass M assuming that Hook's Law is obeyed. (1979)
2. Two masses m_1 and m_2 are suspended together by a massless spring of spring constant k. When the masses are in equilibrium, m_1 is removed without disturbing the system. Find the angular frequency and amplitude of oscillation of m_2 . (1981 - 3 marks)
3. Two light springs of force constants k_1 and k_2 and a block of mass m are in one line AB on a smooth horizontal table such that one end of each spring is fixed on rigid supports and the other end is free as shown in the figure. The distance CD between the free ends of the springs is 60 cms. If the block moves along AB with a velocity 120 cm/sec in between the springs, calculate the period of oscillation of the block ($k_1 = 1.8$ N/m, $k_2 = 3.2$ N/m, $m = 200$ gm) (1985 - 6 Marks)



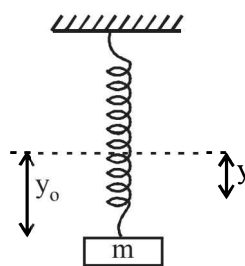
4. Two non-viscous, incompressible and immiscible liquids of densities ρ and 1.5ρ are poured into the two limbs of a circular tube of radius R and small cross section kept fixed in a vertical plane as shown in fig. Each liquid occupies one fourth the circumference of the tube. (1991 - 4 + 4 marks)
- (a) Find the angle θ that the radius to the interface makes with the vertical in equilibrium position.
 (b) If the whole is given a small displacement from its equilibrium position, show that the resulting oscillations are simple harmonic. Find the time period of these oscillations.
5. Two identical balls A and B each of mass 0.1 kg, are attached to two identical massless springs. The spring-mass system is constrained to move inside a rigid smooth pipe bent in the form of a circle as shown in Fig. The pipe is fixed in a horizontal plane.
- The centres of the balls can move in a circle of radius 0.06π meter. Each spring has a natural length of 0.06π meter and spring constant 0.1 N/m. Initially, both the balls are displaced by an angle $\theta = \pi/6$ radian with respect to the diameter PQ of the circle (as shown in Fig.) and released from rest. (1993 - 6 marks)
- (i) Calculate the frequency of oscillation of ball B.
 (ii) Find the speed of ball A when A and B are at the two ends of the diameter PQ.
 (iii) What is the total energy of the system



6. A thin rod of length L and area of cross-section S is pivoted at its lowest point P inside a stationary, homogeneous and non-viscous liquid. The rod is free to rotate in a vertical plane about a horizontal axis passing through P . The density d_1 of the material of the rod is smaller than the density d_2 of the liquid. The rod is displaced by a small angle θ from its equilibrium position and then released. Show that the motion of the rod is simple harmonic and determine its angular frequency in terms of the given parameters. (1996 - 5 Marks)



7. A small body attached to one end of a vertically hanging spring is performing SHM about its mean position with angular frequency ω and amplitude a . If at a height y^* from the mean position, the body gets detached from the spring, calculate the value of y^* so that the height H attained by the mass is maximum. The body does not interact with the spring during its subsequent motion after detachment. ($a\omega^2 > g$) (2005 - 4 Marks)



F Match the Following

DIRECTIONS (Q. No. 1-2) : Each question contains statements given in two columns, which have to be matched. The statements in Column-I are labelled A, B, C and D, while the statements in Column-II are labelled p, q, r and s. Any given statement in Column-I can have correct matching with ONE OR MORE statement(s) in Column-II. The appropriate bubbles corresponding to the answers to these questions have to be darkened as illustrated in the following example :

If the correct matches are A-p, s and t; B-q and r; C-p and q; and D-s then the correct darkening of bubbles will look like the given.

	p	q	r	s	t
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B	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>
C	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
D	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>

1. **Column I** describes some situations in which a small object moves. **Column II** describes some characteristics of these motions. Match the situations in **Column I** with the characteristics in **Column II** and indicate your answer by darkening appropriate bubbles in 4×4 matrix given in the ORS. (2007)

Column I

- (A) The object moves on the x -axis under a conservative force in such a way that its "speed" and position satisfy $v = c_1 \sqrt{c_2 - x^2}$ where c_1 and c_2 are positive constants.
- (B) The object moves on the x -axis in such a way that its velocity and its displacement from the origin satisfy $v = -kx$, where k is a positive constant.
- (C) The object is attached to one end of a mass-less spring of a given spring constant. The other end of the spring is attached to the ceiling of an elevator. Initially everything is at rest. The elevator starts going upwards with a constant acceleration a . The motion of the object is observed from the elevator during the period it maintains this acceleration.
- (D) The object is projected from the earth's surface vertically upwards with a speed $2\sqrt{GM_e/R_e}$, where, M_e is the mass of the earth and R_e is the radius of the earth, Neglect forces from objects other than the earth.

Column II

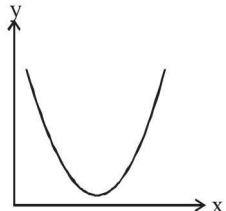
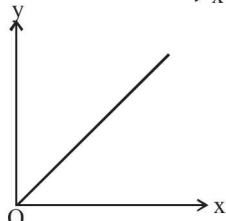
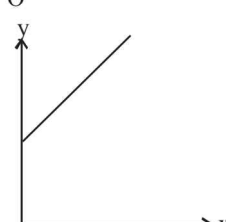
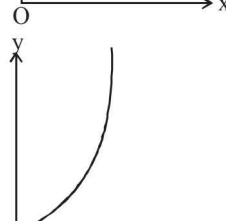
- (p) The object executes a simple harmonic motion.
- (q) The object does not change its direction.
- (r) The kinetic energy of the object keeps on decreasing.
- (s) The object can change its direction only once.

2. Column I gives a list of possible set of parameters measured in some experiments. The variations of the parameters in the form of graphs are shown in Column II. Match the set of parameters given in Column I with the graph given in Column II. Indicate your answer by darkening the appropriate bubbles of the 4×4 matrix given in the ORS. (2008)

Column I

- (A) Potential energy of a simple pendulum (y axis) as a function of displacement (x axis)
- (B) Displacement (y axis) as a function of time (x axis) for a one dimensional motion at zero or constant acceleration when the body is moving along the positive x-direction.
- (C) Range of a projectile (y axis) as a function of its velocity (x axis) when projected at a fixed angle.
- (D) The square of the time period (y axis) of a simple pendulum as a function of its length (x axis)

Column II

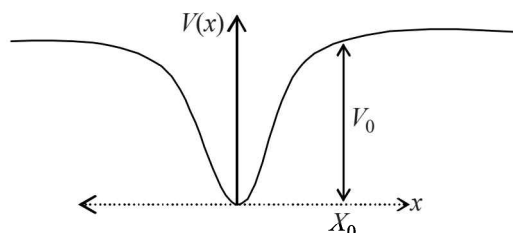
- (p) 
- (q) 
- (r) 
- (s) 

G Comprehension Based Questions

PASSAGE - 1

When a particle of mass m moves on the x -axis in a potential of the form $V(x) = kx^2$ it performs simple harmonic motion. The corresponding time period is proportional to $\sqrt{\frac{m}{k}}$, as can be seen easily using dimensional analysis. However, the motion of a particle can be periodic even when its potential energy increases on both sides of $x = 0$ in a way different from kx^2 and its total energy is such that the particle does not escape to infinity. Consider a particle of mass m moving on the x -axis. Its potential energy is $V(x) = \alpha x^4$ ($\alpha > 0$) for $|x|$ near the origin and becomes a constant equal to V_0 for $|x| \geq X_0$ (see figure).

(2010)



1. If the total energy of the particle is E , it will perform periodic motion only if
- (a) $E < 0$ (b) $E > 0$
 (c) $V_0 > E > 0$ (d) $E > V_0$

2. For periodic motion of small amplitude A , the time period T of this particle is proportional to

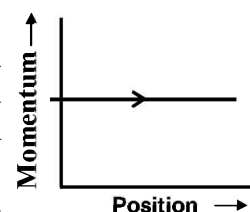
(a) $A\sqrt{\frac{m}{\alpha}}$ (b) $\frac{1}{A}\sqrt{\frac{m}{\alpha}}$ (c) $A\sqrt{\frac{\alpha}{m}}$ (d) $\frac{1}{A}\sqrt{\frac{\alpha}{m}}$

3. The acceleration of this particle for $|x| > X_0$ is

(a) proportional to V_0 (b) proportional to $\frac{V_0}{mX_0}$
 (c) proportional to $\sqrt{\frac{V_0}{mX_0}}$ (d) zero

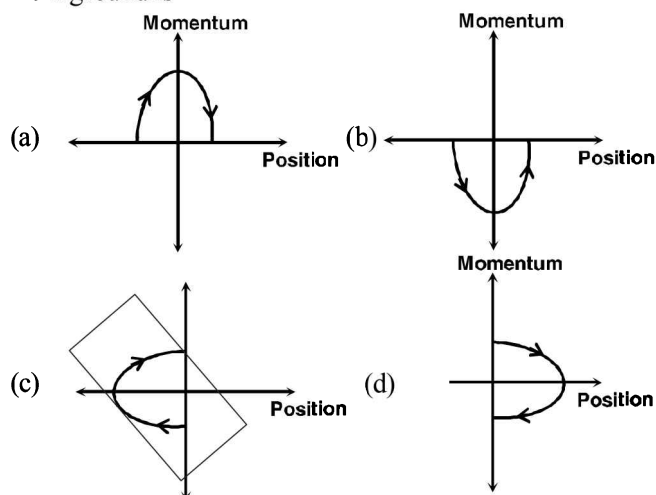
PASSAGE - 2

Phase space diagrams are useful tools in analyzing all kinds of dynamical problems. They are especially useful in studying the changes in motion as initial position and momentum are changed. Here we consider some simple dynamical



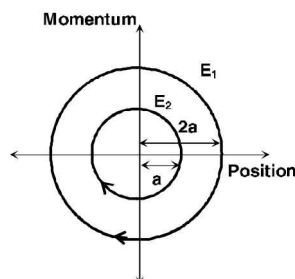
systems in one dimension. For such systems, phase space is a plane in which position is plotted along horizontal axis and momentum is plotted along vertical axis. The phase space diagram is $x(t)$ vs. $p(t)$ curve in this plane. The arrow on the curve indicates the time flow. For example, the phase space diagram for a particle moving with constant velocity is a straight line as shown in the figure. We use the sign convention in which position or momentum upwards (or to right) is positive and downwards (or to left) is negative. (2011)

4. The phase space diagram for a ball thrown vertically up from ground is

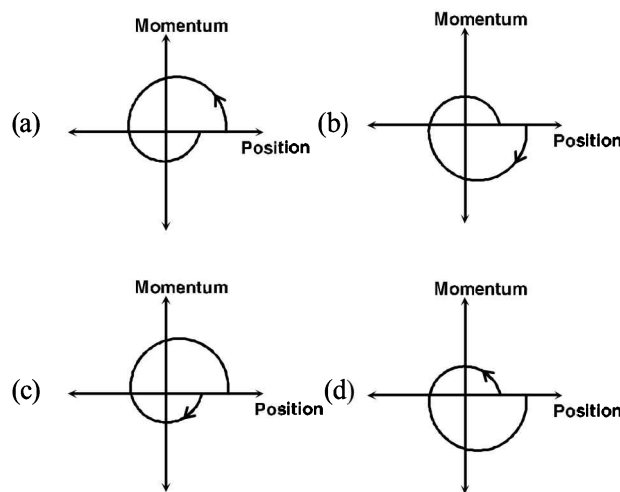
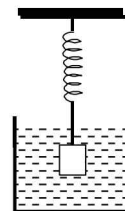


5. The phase space diagram for simple harmonic motion is a circle centered at the origin. In the figure, the two circles represent the same oscillator but for different initial conditions, and E_1 and E_2 are the total mechanical energies respectively. Then

- (a) $E_1 = \sqrt{2}E_2$
 (b) $E_1 = 2E_2$
 (c) $E_1 = 4E_2$
 (d) $E_1 = 16E_2$

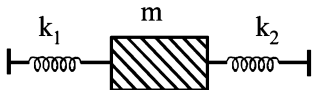


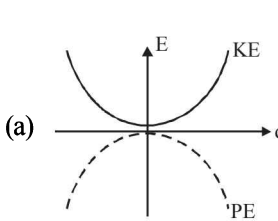
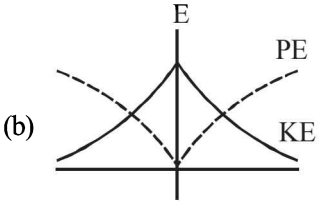
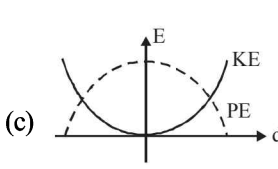
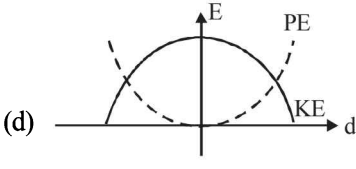
6. Consider the spring-mass system, with the mass submerged in water, as shown in the figure. The phase space diagram for one cycle of this system is



Section-B JEE Main / AIEEE

1. In a simple harmonic oscillator, at the mean position [2002]
 (a) kinetic energy is minimum, potential energy is maximum
 (b) both kinetic and potential energies are maximum
 (c) kinetic energy is maximum, potential energy is minimum
 (d) both kinetic and potential energies are minimum.
2. If a spring has time period T , and is cut into n equal parts, then the time period of each part will be [2002]
 (a) $T\sqrt{n}$ (b) T/\sqrt{n}
 (c) nT (d) T
3. A child swinging on a swing in sitting position, stands up, then the time period of the swing will [2002]
 (a) increase
 (b) decrease
 (c) remains same
 (d) increases if the child is long and decreases if the child is short
4. A mass M is suspended from a spring of negligible mass. The spring is pulled a little and then released so that the mass executes SHM of time period T . If the mass is increased by m , the time period becomes $\frac{5T}{3}$. Then the ratio of $\frac{m}{M}$ is [2003]
 (a) $\frac{3}{5}$ (b) $\frac{25}{9}$ (c) $\frac{16}{9}$ (d) $\frac{5}{3}$
5. Two particles A and B of equal masses are suspended from two massless springs of spring constant k_1 and k_2 , respectively. If the maximum velocities, during oscillation, are equal, the ratio of amplitude of A and B is [2003]
 (a) $\sqrt{\frac{k_1}{k_2}}$ (b) $\frac{k_2}{k_1}$ (c) $\sqrt{\frac{k_2}{k_1}}$ (d) $\frac{k_1}{k_2}$
6. The length of a simple pendulum executing simple harmonic motion is increased by 21%. The percentage increase in the time period of the pendulum of increased length is [2003]
 (a) 11% (b) 21% (c) 42% (d) 10%
7. The displacement of a particle varies according to the relation $x = 4(\cos \pi t + \sin \pi t)$. The amplitude of the particle is [2003]
 (a) -4 (b) 4 (c) $4\sqrt{2}$ (d) 8
8. A body executes simple harmonic motion. The potential energy (P.E), the kinetic energy (K.E) and total energy (T.E) are measured as a function of displacement x . Which of the following statements is true? [2003]
 (a) K.E. is maximum when $x = 0$
 (b) T.E is zero when $x = 0$
 (c) K.E is maximum when x is maximum
 (d) P.E is maximum when $x = 0$

9. The bob of a simple pendulum executes simple harmonic motion in water with a period t , while the period of oscillation of the bob is t_0 in air. Neglecting frictional force of water and given that the density of the bob is $(4/3) \times 1000 \text{ kg/m}^3$. What relationship between t and t_0 is true [2004]
- (a) $t = 2t_0$ (b) $t = t_0/2$
(c) $t = t_0$ (d) $t = 4t_0$
10. A particle at the end of a spring executes S.H.M with a period t_1 , while the corresponding period for another spring is t_2 . If the period of oscillation with the two springs in series is T then [2004]
- (a) $T^{-1} = t_1^{-1} + t_2^{-1}$ (b) $T^2 = t_1^2 + t_2^2$
(c) $T = t_1 + t_2$ (d) $T^{-2} = t_1^{-2} + t_2^{-2}$
11. The total energy of a particle, executing simple harmonic motion is [2004]
- (a) independent of x (b) $\propto x^2$
(c) $\propto x$ (d) $\propto x^{1/2}$
where x is the displacement from the mean position, hence total energy is independent of x .
12. A particle of mass m is attached to a spring (of spring constant k) and has a natural angular frequency ω_0 . An external force $F(t)$ proportional to $\cos \omega t$ ($\omega \neq \omega_0$) is applied to the oscillator. The time displacement of the oscillator will be proportional to [2004]
- (a) $\frac{1}{m(\omega_0^2 + \omega^2)}$ (b) $\frac{1}{m(\omega_0^2 - \omega^2)}$
(c) $\frac{m}{\omega_0^2 - \omega^2}$ (d) $\frac{m}{(\omega_0^2 + \omega^2)}$
13. In forced oscillation of a particle the amplitude is maximum for a frequency ω_1 of the force while the energy is maximum for a frequency ω_2 of the force; then [2004]
- (a) $\omega_1 < \omega_2$ when damping is small and $\omega_1 > \omega_2$ when damping is large
(b) $\omega_1 > \omega_2$
(c) $\omega_1 = \omega_2$
(d) $\omega_1 < \omega_2$
14. Two simple harmonic motions are represented by the equations $y_1 = 0.1 \sin \left(100\pi t + \frac{\pi}{3} \right)$ and $y_2 = 0.1 \cos \pi t$. The phase difference of the velocity of particle 1 with respect to the velocity of particle 2 is [2005]
- (a) $\frac{\pi}{3}$ (b) $\frac{-\pi}{6}$ (c) $\frac{\pi}{6}$ (d) $\frac{-\pi}{3}$
15. The function $\sin^2(\omega t)$ represents [2005]
- (a) a periodic, but not SHM with a period $\frac{\pi}{\omega}$
(b) a periodic, but not SHM with a period $\frac{2\pi}{\omega}$
(c) a SHM with a period $\frac{\pi}{\omega}$
(d) a SHM with a period $\frac{2\pi}{\omega}$
16. The bob of a simple pendulum is a spherical hollow ball filled with water. A plugged hole near the bottom of the oscillating bob gets suddenly unplugged. During observation, till water is coming out, the time period of oscillation would [2005]
- (a) first decrease and then increase to the original value
(b) first increase and then decrease to the original value
(c) increase towards a saturation value
(d) remain unchanged
17. If a simple harmonic motion is represented by $\frac{d^2x}{dt^2} + \alpha x = 0$, its time period is [2005]
- (a) $\frac{2\pi}{\sqrt{\alpha}}$ (b) $\frac{2\pi}{\alpha}$ (c) $2\pi\sqrt{\alpha}$ (d) $2\pi\alpha$
18. The maximum velocity of a particle, executing simple harmonic motion with an amplitude 7 mm, is 4.4 m/s. The period of oscillation is [2006]
- (a) 0.01 s (b) 10 s (c) 0.1 s (d) 100 s
19. Starting from the origin a body oscillates simple harmonically with a period of 2 s. After what time will its kinetic energy be 75% of the total energy? [2006]
- (a) $\frac{1}{6}$ s (b) $\frac{1}{4}$ s (c) $\frac{1}{3}$ s (d) $\frac{1}{12}$ s
20. Two springs, of force constants k_1 and k_2 are connected to a mass m as shown. The frequency of oscillation of the mass is f . If both k_1 and k_2 are made four times their original values, the frequency of oscillation becomes [2007]
- 
- (a) $2f$ (b) $f/2$ (c) $f/4$ (d) $4f$
21. A particle of mass m executes simple harmonic motion with amplitude a and frequency ν . The average kinetic energy during its motion from the position of equilibrium to the end is [2007]
- (a) $2\pi^2 m a^2 \nu^2$ (b) $\pi^2 m a^2 \nu^2$
(c) $\frac{1}{4} m a^2 \nu^2$ (d) $4\pi^2 m a^2 \nu^2$
22. The displacement of an object attached to a spring and executing simple harmonic motion is given by $x = 2 \times 10^{-2} \cos \pi t$ metre. The time at which the maximum speed first occurs is [2007]
- (a) 0.25 s (b) 0.5 s
(c) 0.75 s (d) 0.125 s
23. A point mass oscillates along the x -axis according to the law $x = x_0 \cos(\omega t - \pi/4)$. If the acceleration of the particle is written as $a = A \cos(\omega t + \delta)$, then [2007]
- (a) $A = x_0 \omega^2$, $\delta = 3\pi/4$ (b) $A = x_0 \omega^2$, $\delta = -\pi/4$
(c) $A = x_0 \omega^2$, $\delta = \pi/4$ (d) $A = x_0 \omega^2$, $\delta = -\pi/4$
24. If x , v and a denote the displacement, the velocity and the acceleration of a particle executing simple harmonic motion of time period T , then, which of the following does not change with time? [2009]
- (a) aT/x (b) $aT + 2\pi v$
(c) aT/v (d) $a^2 T^2 + 4\pi^2 v^2$

25. Two particles are executing simple harmonic motion of the same amplitude A and frequency ω along the x -axis. Their mean position is separated by distance X_0 ($X_0 > A$). If the maximum separation between them is $(X_0 + A)$, the phase difference between their motion is: [2011]
- (a) $\frac{\pi}{3}$ (b) $\frac{\pi}{4}$ (c) $\frac{\pi}{6}$ (d) $\frac{\pi}{2}$
26. A mass M , attached to a horizontal spring, executes S.H.M. with amplitude A_1 . When the mass M passes through its mean position then a smaller mass m is placed over it and both of them move together with amplitude A_2 . The ratio of $\left(\frac{A_1}{A_2}\right)$ is: [2011]
- (a) $\frac{M+m}{M}$ (b) $\left(\frac{M}{M+m}\right)^{\frac{1}{2}}$
- (c) $\left(\frac{M+m}{M}\right)^{\frac{1}{2}}$ (d) $\frac{M}{M+m}$
27. If a simple pendulum has significant amplitude (up to a factor of $1/e$ of original) only in the period between $t = 0$ s to $t = \tau$ s, then τ may be called the average life of the pendulum. When the spherical bob of the pendulum suffers a retardation (due to viscous drag) proportional to its velocity with b as the constant of proportionality, the average life time of the pendulum is (assuming damping is small) in seconds : [2012]
- (a) $\frac{0.693}{b}$ (b) b (c) $\frac{1}{b}$ (d) $\frac{2}{b}$
28. The amplitude of a damped oscillator decreases to 0.9 times its original magnitude in 5s. In another 10s it will decrease to α times its original magnitude, where α equals [JEE Main 2013]
- (a) 0.7 (b) 0.81 (c) 0.729 (d) 0.6
29. An ideal gas enclosed in a vertical cylindrical container supports a freely moving piston of mass M . The piston and the cylinder have equal cross sectional area A . When the piston is in equilibrium, the volume of the gas is V_0 and its pressure is P_0 . The piston is slightly displaced from the equilibrium position and released. Assuming that the system is completely isolated from its surrounding, the piston executes a simple harmonic motion with frequency [JEE Main 2013]
- (a) $\frac{1}{2\pi} \frac{A\gamma P_0}{V_0 M}$ (b) $\frac{1}{2\pi} \frac{V_0 M P_0}{A^2 \gamma}$
- (c) $\frac{1}{2\pi} \sqrt{\frac{A^2 \gamma P_0}{M V_0}}$ (d) $\frac{1}{2\pi} \sqrt{\frac{M V_0}{A \gamma P_0}}$
30. A particle moves with simple harmonic motion in a straight line. In first τ s, after starting from rest it travels a distance a , and in next τ s it travels $2a$, in same direction, then: [JEE Main 2014]
- (a) amplitude of motion is $3a$
 (b) time period of oscillations is 8τ
 (c) amplitude of motion is $4a$
 (d) time period of oscillations is 6τ
31. A pendulum made of a uniform wire of cross sectional area A has time period T . When an additional mass M is added to its bob, the time period changes to T_M . If the Young's modulus of the material of the wire is Y then $\frac{1}{Y}$ is equal to : [JEE Main 2015]
- (g = gravitational acceleration)
- (a) $\left[1 - \left(\frac{T_M}{T}\right)^2\right] \frac{A}{Mg}$ (b) $\left[1 - \left(\frac{T}{T_M}\right)^2\right] \frac{A}{Mg}$
- (c) $\left[\left(\frac{T_M}{T}\right)^2 - 1\right] \frac{A}{Mg}$ (d) $\left[\left(\frac{T_M}{T}\right)^2 - 1\right] \frac{Mg}{A}$
32. For a simple pendulum, a graph is plotted between its kinetic energy (KE) and potential energy (PE) against its displacement d . Which one of the following represents these correctly? (graphs are schematic and not drawn to scale) [JEE Main 2015]
- (a)  (b) 
- (c)  (d) 
33. A particle performs simple harmonic motion with amplitude A . Its speed is trebled at the instant that it is at a distance $\frac{2A}{3}$ from equilibrium position. The new amplitude of the motion is : [JEE Main 2016]
- (a) $A\sqrt{3}$ (b) $\frac{7A}{3}$
- (c) $\frac{A}{3}\sqrt{41}$ (d) $3A$