

Random Variable

(Fix) Algebraic Variable
 \downarrow
 x

$$x + 5 = 10$$

$$x = 10 - 5 \quad \boxed{x = 5}$$

Random Experiment \rightarrow value Random.

ex - Tossing a Coin (x)

$$x = \{H, T\}$$

Event y = Throwing a Dice

Random Variable $\rightarrow y = \{1, 2, 3, 4, 5, 6\}$

\rightarrow event

Sample Space

$$\text{Probability} = \frac{\text{The Event}}{\text{Total outcome.}}$$

$$\text{Probability}(H) = \frac{1}{2}$$

$$T = \frac{1}{2}$$

$$\text{probability of}(1) \text{ in dice} = \frac{1}{6}$$

Type of Random Variable

①

Discrete RV (whole no)
 $= \{1, 2, 3, 4, 5, 6\}$
 $= \{H, T\}$

②

Continuous RV
 $x = \{10, 10\}$
 $= 1.2, 1.75$

Probability Distribution

What are Probability Distributions?

A probability distribution is a list of all of the possible outcomes of a random variable along with their corresponding probability values.

Coin Toss	H	T
Prob. value	$\frac{1}{2}$	$\frac{1}{2}$

← Probability Distribution

Dice	possible outcome	1	2	3	4	5	6
probability		$\frac{1}{6}$	$\frac{2}{6}$	$\frac{3}{6}$	$\frac{4}{6}$	$\frac{5}{6}$	$\frac{6}{6}$

Dice 1		1	2	3	4	5	6
Dice 2	1	2	3	4	5	6	7
	2	3	4	5	6	7	8
	3	4	5	6	7	8	9
	4	5	6	7	8	9	10
	5	6	7	8	9	10	11
	6	7	8	9	10	11	12

36 out come

Possible Outcomes

probability
→ one

2	$\frac{1}{36}$
3	$\frac{2}{36}$
4	$\frac{3}{36}$
5	$\frac{4}{36}$
6	$\frac{5}{36}$
7	$\frac{6}{36}$
8	$\frac{5}{36}$
9	$\frac{4}{36}$
10	$\frac{3}{36}$
11	$\frac{2}{36}$
12	$\frac{1}{36}$

Problem → If the event is limited then we easily calculate.

but what if event is huge in no.

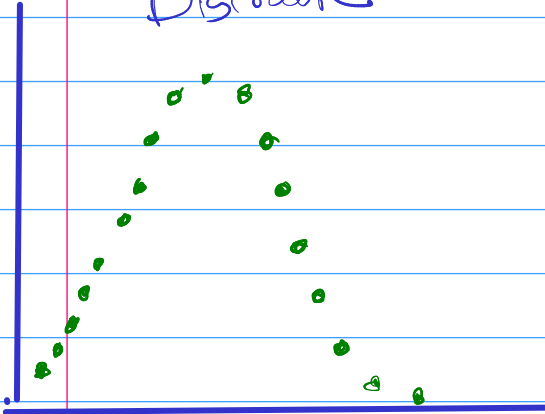
ex - 1 dice thrown 10000 time
2 dice thrown 10,000 time.

Probability Distribution function.

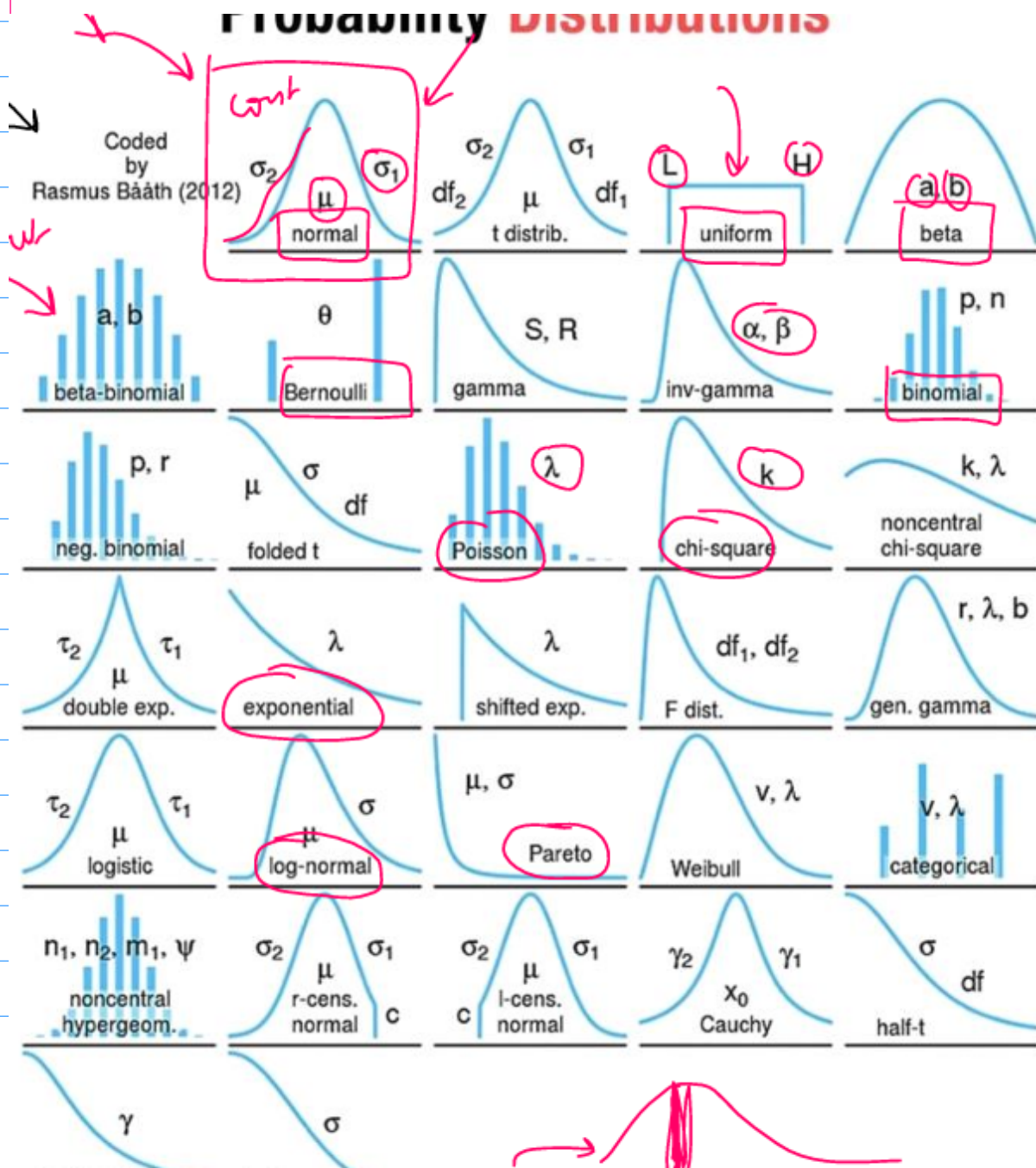
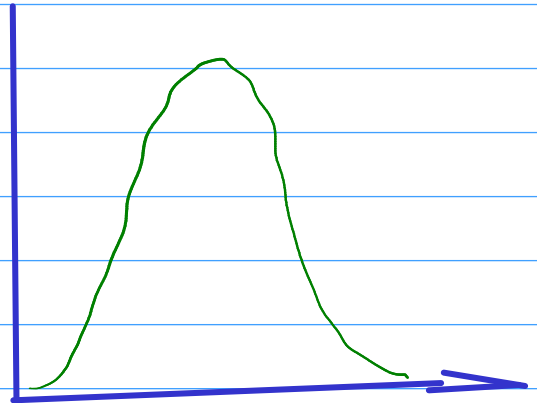
$$y = f(x) =$$

in graphical Representation -

Discrete



Continuous



Probability Distribution Function \Rightarrow PDF

Probability
Mass
Function (Discrete)
(PMF)

Probability
Density
Function (Continuous)
(PDF)

CDF
Cumulative
Distribution
Function.

A probability distribution function (~~PDF~~) is a mathematical function that describes the probability of obtaining different values of a random variable in a particular probability distribution.

PMF

PMF stands for Probability Mass Function. It is a mathematical function that describes the probability distribution of a discrete random variable.

The PMF of a discrete random variable assigns a probability to each possible value of the random variable. The probabilities assigned by the PMF must satisfy two conditions:

- The probability assigned to each value must be non-negative (i.e., greater than or equal to zero).
- The sum of the probabilities assigned to all possible values must equal 1.

Dice - 1 2 3 4 5 6
Prob $\frac{1}{6} + \frac{1}{6} + \frac{1}{6} + \frac{1}{6} + \frac{1}{6} + \frac{1}{6} = \underline{\underline{1}}$

Coin H T
prob $\frac{1}{2} + \frac{1}{2} = 1$

$y = f(x)$

$y = \begin{cases} \frac{1}{6} & \text{if } x \in \{1, 2, 3, 4, 5, 6\} \\ 0 & \text{otherwise} \end{cases}$

Belongs to
↓

2 dice PMF = $y = \begin{cases} \frac{1}{36} & \text{if } x \in \{2, 12\} \\ \frac{2}{36} & \text{if } x \in \{3, 11\} \\ \frac{3}{36} & \text{if } x \in \{4, 10\} \\ \vdots \\ 0 & \text{otherwise} \end{cases}$

CDF - Cumulative Distribution Function.

The cumulative distribution function (CDF) $F(x)$ describes the probability that a random variable X with a given probability distribution will be found at a value less than or equal to x

$F(x) = P(x \leq 4) \xrightarrow{\text{CDF}} = P(x=1) + P(x=2) + P(x=3) + P(x=4)$
 $= \frac{1}{6} + \frac{1}{6} + \frac{1}{6} + \frac{1}{6}$
 $= \frac{4}{6} = \frac{2}{3}$

PDF

	1	2	3	4	5	6
	$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{6}$

CDF

	1	2	3	4	5	6
	$\frac{1}{6}$	$\frac{2}{6}$	$\frac{3}{6}$	$\frac{4}{6}$	$\frac{5}{6}$	$\frac{6}{6} = 1$