

Simplified DES

1 Introduction

In this lab we will work through a simplified version of the DES algorithm. The algorithm is not cryptographically secure, but its operations are similar enough to the DES operation to give a better feeling for how it works.

We will proceed by reading the Simplified DES algorithm description in the Stallings section. We will then work through a full example in class.

2 Full Example

Let the plaintext be the string 0010 1000. Let the 10 bit key be 1100011110.

2.1 Key Generation

The keys k_1 and k_2 are derived using the functions $P10$, Shift, and $P8$.

$P10$ is defined as follows:

P10
3 5 2 7 4 10 1 9 8 6

$P8$ is defined to be as follows:

P8
6 3 7 4 8 5 10 9

The first key k_1 is therefore equal to:

Bit #

K

$P10(K)$

Shift($P10(K)$) $P8$ (Shift

($P10(K)$))

0 0 1 1 0	0 1 1 1 1
0 1 1 0 0	1 1 1 1 0
1 1 1 0 1	0 0 1

1 2 :
1 1 :

The second key k_2 is derived in a similar manner:

Bit #

K

$P_{10}(K)$
 $Shif\ t^3(P_{10}(K))\ P_8(Shif$
 $t^2(P_{10}(K)))$

1 2
1 1
0 0

1 0 0 0 1	1 1 0 1 1
1 0 1 0 0	1 1 1

So we have the two keys $k_1 = \{1110\ 1001\}$ and $k_2 = \{1010\ 0111\}$

2.2 Initial and Final Permutation

The plaintext undergoes an initial permutation when it enters the encryption function, IP . It undergoes a reverse final permutation at the end IP^{-1} .

The function IP is defined as follows:

IP
2 6 3 1 4 8 5 7

1

The function IP^{-1} is defined as follows:

IP^{-1}
4 1 3 5 7 2 8 6

Applied to the input, we have the following after the initial permutation:

Bit # P	0 0 1 0	0 0 1 0
$IP(P)$	1 2 3 4	0 0 1 0

2.3 Functions f_k , SW , K

- The function f_k is defined as follows. Let $P = (L, R)$, then $f_k(L, R) = (L \oplus F(R, SK), R)$.
- The function SW just switches the two halves of the plaintext, so $SW(L, R) \rightarrow (R, L)$.
- The function $F(p, k)$ takes a four bit string p and eight bit key k and produces a four bit output. It performs the following steps.

1. First it runs an expansion permutation E/P :

E/P

4 1 2 3 2 3 4 1

2. Then it XORs the key with the result of the E/P function
3. Then it substitutes the two halves based on the S-Boxes.
4. Finally, the output from the S-Boxes undergoes the $P4$ permutation:

2 4 3 1

P4

Applying the functions, we must perform the following steps: $IP^{-1} \circ f_{K2} \circ SW \circ f_{K1} \circ IP$ 1. We have already calculated $IP(P) = \{0010\ 0010\}$. Applying the next functions: 2. $f_{K1}(L, R) = f_{\{1110\ 1001\}}(0010\ 0010) = (0010 \oplus F(0010, \{1110\ 1001\}), 0010)$ 3. $F(0010, \{1110\ 1001\}) = P4 \circ SBoxes \circ \{1110\ 1001\} \oplus (E/P(0010))$ 4. The steps are:

Bit #	1 1 1 0	1 0 0 1
R		
E/P(R)	1 1 1 1	1 1 0 1
k_1		
$E/P(R) \oplus k_1$	1 0 0 0	
$SBoxes(E/P(R) \oplus k_1)$		
$P4(Sboxes(E/P(R) \oplus k_1))$	0 0 0 1	

1 2 3 4	5 6 7 8
0 0 1 0	
0 0 0 1	0 1 0 0

5. The result from F is therefore 0001

6. Calculating we then have $f_{K1}(L, R) = (0010 \oplus 0001, 0010) = (0011, 0010)$

7. So far, then $L = 0011$ and $R = 0010$. SW just swaps them so $R = 0011$ and $L = 0010$. 8. We now do the calculation of $f_{K2}(L, R) = f_{\{1010\ 0111\}}(0010\ 0011) = (0010 \oplus F(0011, \{1010\ 0111\}), 0011)$

2

9. The steps for F are as above:

Bit #	0 0 1 1	
R		
E/P(R)	1 0 0 1	0 1 1 0
k_2		
$E/P(R) \oplus k_2$	1 0 1 0	0 1 1 1
$SBoxes(E/P(R) \oplus k_2)$	0 0 1 1	0 0 0 1
$P4(Sboxes(E/P(R) \oplus k_2))$		

1 2 3 4	5 6 7 8
	1 0 1 0

0 0 1 1	
---------	--

10. So now we have the outcome of F as 0011

11. Calculating we then have $f_{k2}(L, R) = (0010 \oplus 0011, 0011) = (0001, 0011)$

12. Last, we perform the IP^{-1} permutation:

Bit #		
R,L	1 0 0 0	1 0 1 0
$IP^{-1}(R,L)$		
	1 2 3	
	0 0 0	

13. So the final result of the encryption is 1000 1010. 3