

AI - Assignment - 7

19K41A05E4

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Given data:

outlook	Temp	Humidity	windy	Houxtrophy
Rainy	Hot	High	False	25
Rainy	Hot	high	True	30
overcat	Hot	high	False	46
Sunny	Mild	high	False	45
Sunny	cool	Normal	False	52
overcast	cool	Normal	True	43
Rainy	mild	high	False	35
Rainy	cool	normal	False	38
Sunny	mild	Normal	False	46
Rainy	mild	Normal	True	48
over cast	mild	high	True	52
overcast	hot	Normal	False	44
Sunny	mild	high	True	30
Sunny	cool	Normal	True	23

Termination criteria: $cvc = 10\%$ (as)

minimum no. of samples.

calculating mean, Standard deviation (SD),

co-efficient of variation (CV),

$$\text{Mean} = \frac{\sum x}{n} = \frac{557}{14} = 39.78$$

$$SD = \sqrt{\frac{\sum (x - \text{mean})^2}{n}} = 9.67$$

$$CV = \frac{SD}{\text{mean}} \times 100 = \frac{9.67}{39.78} \times 100 = 24.30$$

Now, dataset is split into different attributes.

The SD of each branch is calculated.

$$SD(\text{after}) = \sum w(\text{branch}) \cdot SD(\text{branch})$$

and the result SDR (standard Deviation Reduction) is

$$\text{calculated } SDR = SD - SD(\text{after})$$

$$SD = 9.67$$

outlook:

Outlook	Mean	SD	CV	n	w(v)
Raining	35.2	8.7	24.7	5	5/14
Overcast	46.25	4.03	8.72	4	4/14
Sunny	39.2	12.2	31.0	5	5/14

$$\therefore SD(\text{outlook}) = \frac{5}{14} \times 8.7 + \frac{4}{14} \times 4.03 + \frac{5}{14} \times 12.2 = 8.59$$

$$SDR(\text{outlook}) = SD - SD(\text{outlook}) = 9.67 - 8.59 = 1.08$$

Temperature:

Temp	Mean	SD	CV	n	W (v)
Hot	36.25	10.34	30.6	4	4/14
cool	39	12.14	31.1	4	4/14
mild	42.6	8.38	19.65	6	6/14

$$SD(\text{temp}) = \frac{4}{14} * 10.34 + \frac{4}{14} * 12.14 + \frac{6}{14} * 8.38 = 10.01$$

$$SDR(\text{temp}) = SD - SD(\text{temp}) = 9.69 - 10.01 = -0.34$$

Humidity:

Humidity	Mean	SD	CV	n	W (v)
High	37.51	10.11	26.92	7	7/14 = 1/2
Normal	4.2	9.4	22.4	7	7/14 = 1/2

$$SD(\text{humidity}) = \frac{7}{14} * 10.11 + \frac{7}{14} * 9.4 = 9.77$$

$$SDR(\text{humidity}) = SD - SD(\text{humidity})$$

windy:

windy	Mean	SD	CV	n	W (v)
True	37.6	11.6	30.8	6	6/14
False	41.3	8.41	20.3	8	8/14

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$$SD(\text{windy}) = \frac{6}{14} * 11.6 + \frac{8}{14} * 8.41 = 9.77$$

$$SDR(\text{windy}) = SD - SD(\text{windy}) = 9.67 - 9.77 = -0.1$$

SDR	windy	→	-0.1	10.01	9.77
	Outlook	→	1.08	10.01	9.67
	Temp	→	-0.34	10.01	9.67
	Humidity	→	-0.1	10.01	9.67
	windy	→	0.1	10.01	9.67

The value that has highest SDR is considered as root node (i.e., decision node).

considering termination criteria

cv is 10% (or) cv is $(n \leq 4)$

Overcast has cv of 8% which is less than threshold value.

∴, we need not go for further splitting

Outlook



Overcast



Hours played is 46.25

Windy	0	10	10	10
Overcast	0	10	10	10
Clear	0	10	10	10

Outlook	Temp	Humidity	windy	Hours played
Sunny	mild	High	False	45
Sunny	cool	Normal	False	52
Sunny	Cool	Normal	True	23
Sunny	Hot	Normal	True	46
Sunny	mild	High	True	30

mean = 39.2

SD = 12.2

CV = 31.0

Temperature:

Temp	Mean	SD	CV	n	W(CV)
mild	40.3	8.96	22.23	3	3/5
cold	37.5	20.5	54.66	2	2/5

$$SD(\text{humidity}) = \frac{2}{5} * 10.6 + \frac{3}{5} * 15.3 = 13.44$$

$$SDR(\text{humidity}) = SD - SD(\text{humidity}) = 12.2 - 13.44 = -1.22$$

Windy:

Windy	Mean	SD	CV	n	W(CV)
False	47.66	3.78	7.94	3	3/5
True	26.5	4.94	18.63	2	2/5

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$$SD(\text{windy}) = \frac{3}{5} = 3.78 + \frac{2}{5} = 4.94 = 4.23$$

$$SDR(\text{windy}) = SD - SDR(\text{windy}) = 12.2 - 4.23 = 7.97$$

In outlook:

Among, temp, humidity & windy, SDR value is high for

windy: $SDR = 7.97$.

Then, check for cv value.

both true & false satisfy the cv value.

outlook

Sunny

overcast

windy

Hours played
46.25

False

true

Hours played
47.66

Hours played
26.5

Rainy:

outlook	Temp	humidity	windy	hours played.
Rainy	hot	high	False	25
Rainy	hot	high	True	30
Rainy	mild	high	False	35
Rainy	cool	normal	False	38
Rainy	mild	Normal	True	48

$$\text{Mean} = 35.2$$

$$SD = 8.7$$

$$CV = 24.7$$

Temperature :

Temp	Mean	SD	CV	n	w(n)
•Temp					
Hot	27.5	3.53	12.13	2	2/5
mild	41.5	9.19	22.144	2	2/5
cool	38	0	0	1	1/5

$$SD(\text{temp}) = \frac{2}{5} * 3.53 + \frac{2}{5} * 9.19 + \frac{1}{5} * 0 = 5.068$$

$$SDR(\text{temp}) = SD - SD(\text{temp}) = 8.7 - 5.068 = 3.632$$

Humidity :

Humidity	Mean	SD	CV	n	w(n)
high	30	5	16.66	3	3/5
normal	43	7.07	16.44	2	2/5

$$SD(\text{humidity}) = \frac{3}{5} * 5 + \frac{2}{5} * 7.07 = 5.828$$

$$SDR(\text{humidity}) = SD - SD(\text{humidity}) = 8.7 - 5.828 = 2.872$$

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Windy:

Windy	Mean	SD	CV	n	w(c)
False	32.66	8.80	20.85	3	3/5
True	39	12.72	32.5	2	2/5

$$SD(\text{windy}) = \frac{3}{5} \times 6.80 + \frac{2}{5} \times 12.72 = 9.168$$

$$SDR(\text{windy}) = SD - SD(\text{windy}) = 8.7 - 9.168 = -0.468$$

⑤ Among temp, Humidity & windy, The SDR value is high for temperature (i.e. 3.612). Then check for cv value of hot, mild and cold satisfy the cv value.

- Design tree diagram to predict no of hours of play based on weather conditions.

