Assignment 4

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Abstract—This document explains the concept of computing the determinant of a matrix given.

Download all python codes from

https://github.com/harshachinta/EE5609-Matrix-Theory/tree/master/Assignments/Assignment4/ code

and latex-tikz codes from

https://github.com/harshachinta/EE5609-Matrix-Theory/tree/master/Assignments/Assignment4

1 Problem

If a, b and c are real numbers, and $\Delta = \begin{vmatrix} b + c & c + a & a + b \\ c + a & a + b & b + c \\ a + b & b + c & c + a \end{vmatrix} = 0,$

2 EXPLANATION

Given,

$$\Delta = \begin{vmatrix} b+c & c+a & a+b \\ c+a & a+b & b+c \\ a+b & b+c & c+a \end{vmatrix}$$

$$(2.0.1) \quad \Delta = 0 \text{ if } a+b+c = 0 \text{ or } a=b=c.$$
From equation (2.0.6) and (2.0.8)
$$\Delta = 0 \text{ if } a+b+c = 0 \text{ or } a=b=c.$$

$$(2.0.2) \quad \Delta = 0 \text{ if } a+b+c = 0 \text{ or } a=b=c.$$

$$(2.0.2) \quad (2.0.2) \quad (2.0.2) \quad (2.0.2) \quad (2.0.2) \quad (2.0.3)$$

$$= 2(a+b+c) \quad b+c \quad c+a \quad (2.0.3)$$

$$(2.0.3) \quad (2.0.3) \quad (2.0.4)$$

On expanding determinant along first column from equation (2.0.4),

$$\Rightarrow 2(a+b+c)[(c-b)(b-a) - (a-c)^{2}] = 0$$

$$\Rightarrow 2(a+b+c)(a^{2}+b^{2}+c^{2}-ab-bc-ca) = 0$$

$$\Rightarrow (a+b+c)(2a^{2}+2b^{2}+2c^{2}-2ab-2bc-2ca) = 0$$

$$\implies (a+b+c)$$

$$[(a-b)^2 + (b-c)^2 + (c-a)^2] = 0 \quad (2.0.5)$$

From equation (2.0.5) we get 2 equations,

$$\Longrightarrow \boxed{(a+b+c)=0} \tag{2.0.6}$$

or.

$$\implies (a-b)^2 + (b-c)^2 + (c-a)^2 = 0$$
 (2.0.7)

Equation (2.0.7) is possible only when, a = b = c

$$\implies \boxed{a = b = c} \tag{2.0.8}$$

From equation (2.0.6) and (2.0.8) we can say that, $\triangle = 0 \text{ if } a + b + c = 0 \text{ or } a = b = c.$

3 Solution

From equation (2.0.6) and (2.0.8) we can say that,