

Example of diagonal dominance.

Q. 1 Convert following into diagonal dominance.

$$\begin{bmatrix} 8 & -3 & 2 \\ 6 & 3 & 12 \\ 4 & 11 & -1 \end{bmatrix} \begin{matrix} R_1 \\ R_2 \\ R_3 \end{matrix}$$

Solⁿ - Interchanging $R_2 \sim R_3$

$$\begin{bmatrix} 8 & -3 & 2 \\ 4 & 11 & -1 \\ 6 & 3 & 12 \end{bmatrix} \text{ is diagonal dominance}$$

Q. 2 Consider the system of equation. Convert the system so that the matrix is diagonal dominance.

$$\begin{array}{lcl} x_1 + 7x_2 - x_3 = 3 & \text{Diagonal} & 5x_1 + x_2 + x_3 = 9 \\ 5x_1 + x_2 + x_3 = 9 & \text{Dominant} & x_1 + 7x_2 - x_3 = 3 \\ -3x_1 + 2x_2 + 7x_3 = 17 & & -3x_1 + 2x_2 + 7x_3 = 17 \end{array}$$

Solⁿ - OR Rearrange equations as follows also.

$$\begin{cases} 7x_2 + x_1 - x_3 = 3 \\ x_2 + 5x_1 + x_3 = 9 \\ 2x_2 - 3x_1 + 7x_3 = 17 \end{cases} \left\{ \begin{array}{l} \text{Now Matrix will} \\ \text{be diagonal dominant} \\ \text{The solution appear} \\ \text{in order } \underline{x_2}, \underline{x_1} \text{ and } \underline{x_3} \end{array} \right.$$