

Assignment 1

Harsha Vardhan - EE18BTECH11018

Download all latex-tikz codes from

https://github.com/harshagv9/C_DataStructures/blob/main/assignment1.tex

1 PROBLEM

(Q 49) Consider the following ANSI C program.

```
#include <stdio.h>
int foo(int x,int y, int q)
{
    if ((x<=0) && (y <= 0))
        return q;
    if (x <=0)
        return foo(x, y-q, q);
    if (y <= 0)
        return foo(x-q, y, q);
    return foo(x, y-q, q) + foo(x-q, y, q);
}
int main()
{
    int r = foo(15,15,10);
    printf("%d", r);
    return 0;
}
```

The output of the program upon execution is

2 SOLUTION

Answer : 60

Explanation

This is a problem involving recursion. The function foo gets executed recursively until the values of x and y are negative in the foo function and finally returns the value of q. Hence final value of output depends on the number of recursive foo functions at the end.

Initially at $x = 15$, $y = 15$, the inside block gets neglected and again foo functions gets executed.

Now two foo functions each with x,y are (5, 15), (15, 5) are executed. $\text{foo}(15,15,10) = \text{foo}(5,15,10) + \text{foo}(15,5,10)$

$\text{foo}(5,15,10) = \text{foo}(-5,15,10) + \text{foo}(5,-5,10)$

$\text{foo}(15,5,10) = \text{foo}(15,-5,10) + \text{foo}(5,5,10)$

$\text{foo}(5,5,10) = \text{foo}(5,-5,10) + \text{foo}(-5,5,10)$

$\text{foo}(-5,15,10) = \text{foo}(-5,5,10) = \text{foo}(-5,-5,10) = 10$

$\text{foo}(5,-5,10) = \text{foo}(-5,-5,10) = 10$

$\text{foo}(-5,15,10) = \text{foo}(-5,5,10) = \text{foo}(-5,-5,10) = 10$

$\text{foo}(15,-5,10) = \text{foo}(5,-5,10) = \text{foo}(-5,-5,10) = 10$

Hence adding the return values of all foo functions result = 60

Mathematical Analysis

This problem can be viewed as no of unique paths down the tree one has to travel so to get basic unit pair of numbers. i.e, the no of combinations for each pair taken a single number and obtaining the remainder each time until we get basic pair of least negative numbers.

For any two random integers x, y the answer will always be some multiple of q given by following equation $\text{foo}(x, y, q)$

$$\text{foo}(x, y, q) = \left(\frac{\left(\left\lceil \frac{x}{q} \right\rceil + \left\lceil \frac{y}{q} \right\rceil\right)!}{\left(\left\lceil \frac{x}{q} \right\rceil!\right)\left(\left\lceil \frac{y}{q} \right\rceil!\right)} \right) * q$$

