

Arrays: Sliding Window

Friday - Content
9:00 PM

10:30 PM - Discussion

Agenda

- Sliding Window Concept
- Minimum swaps
- Spiral Printing

Q1

Given array of N elements, find max ^{window} subarray sum of length=k ($N \geq k$).



arr[10] =

	0	1	2	3	4	5	6	7	8	9
	-3	4	-2	5	3	-2	8	2	-1	4

k=5

s	e	sum
0	4	7
1	5	8
2	6	12
3	7	16
4	8	10
5	9	11

ans = 16

$e \Rightarrow [k-1, N-1]$
 $N-1 - (k-1) + 1$
 $= N - k + 1$
 $= N - k + 1$ iterations

Total Iterations
 $= (N - k + 1) \cdot k$

Idea

For every subarray of size k, iterate & calculate its sum. Overall take the max sum.

```
int maxSubarray(arr, k) {
    s=0, e=k-1
    ans = -inf
    while (e < N) {
        // Compute sum of [s, e]
        sum = 0
        for (i=s; i<=e; i++) {
            sum += arr[i]
        }
        ans = max(ans, sum)
        s = s+1
        e = e+1
    }
    return ans
}
```

k iterations {

}

Worst Case -

$$k=1 \Rightarrow (N-1+1)(1) = N$$

$$k=N \Rightarrow (N-N+1)(N) = N$$

$$k=\frac{N}{2} \Rightarrow (N-\frac{N}{2}+1)(\frac{N}{2}) = (\frac{N}{2}+1)(\frac{N}{2}) \\ = O(N^2)$$

Optimisation

Inner loop $\Rightarrow \frac{\text{sum}[s \dots e]}{\hookrightarrow \text{Prefix sum}}$

1) Construct prefix array - $pf[N]$

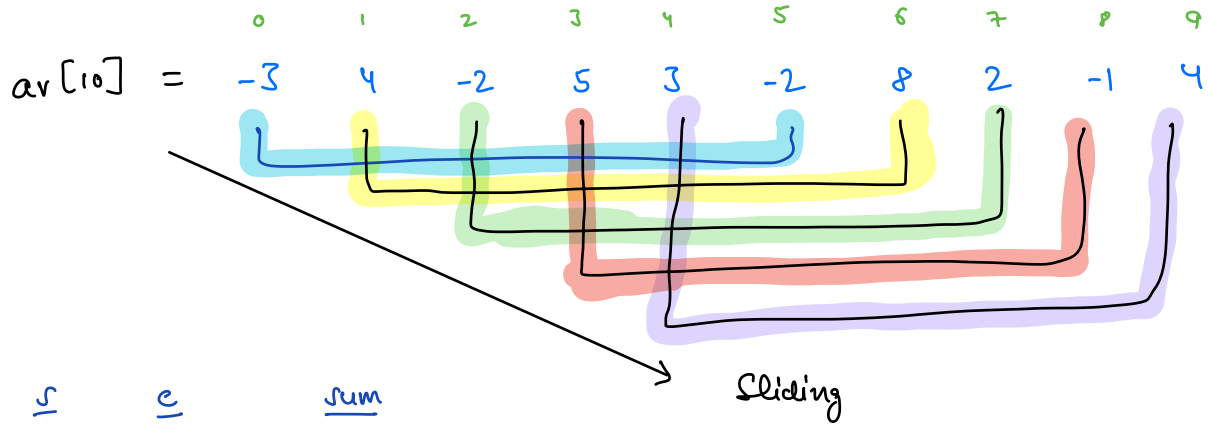
2)

```
while (e < N) {  
    // Compute sum of [s e]  
    sum = 0  
    if s == 0 : sum = pf[e]  
    else : sum = pf[e] - pf[s-1]  
    ans = max(ans, sum)  
    s = s+1  
    e = e+1  
}  
return ans
```

TC : $O(N)$
SC : $O(N)$

Optimisation 2

$k = 6$



<u>s</u>	<u>e</u>	<u>sum</u>
0	5	5
1	6	$sum = sum - A[0] + A[6] = 5 - (-3) + 8 = 16$
2	7	$sum = sum - A[1] + A[7] = 16 - 4 + 2 = 14$
3	8	$sum = sum - A[2] + A[8] = 14 - (-2) + (-1) = 15$
4	9	$sum = sum - A[3] + A[9] = 15 - 5 + 4 = 14$

Ans = 16

$$s \quad e \quad sum = sum - A[s-1] + A[e]$$

Carry forward + All subarrays of same size \Rightarrow Sliding Window

```
int maxWindowSum(int []A, int n, int k) {
```

// Calculate sum of the first window \rightarrow first k elements

```
sum = 0
```

```
for (i=0; i < k; i++) {
    sum += A[i]
}
```

} k iterations

```
s = 1, e = k
```

```
ans = sum
```

```
while (e < N) {
```

// Calculate the sum $[s, e]$

```
sum = sum - A[s-1] + A[e]
```

```
ans = max(ans, sum)
```

```
s = s+1
```

```
e = e+1
```

} $N-k$ iterations

```
}
```

```
return ans
```

```
}
```

Quiz 1

$e \rightarrow [k, N-1]$

$\Rightarrow N-1 - k + 1$

$\Rightarrow N-k$

TC: $O(N)$

SC: $O(1)$

$$\begin{aligned} \text{Total iterations} &= \cancel{k} + N - \cancel{k} \\ &= N \end{aligned}$$

Q2

Given arr[N] and a number B, find minimum no of swaps to bring all numbers $\leq B$

Example

arr = 1 12 10 3 14 10 5
B = 8
↳ ans = 2

Example Quiz 2

arr = 25 30 2 18 7 6 9 50 3
B = 10
↳ ans = 1

Example Quiz 3

arr = 19 11 3 9 7 25 6 20 4
B = 10
↳ ans = 1

→ Count of all elements $\leq B$, say k

→ Size of subarray will be fixed - k

No of swaps

0 - 4
1 - 5
2 - 6
3 - 7
4 - 8

2
2
1
2
2

k=5

All elements $\leq B \Rightarrow$ good

All elements $> B \Rightarrow$ bad

No of swaps in a window = No of bad elements in that window

```
int minSwaps(int []A, int B) {
```

```
    // Calculate k
```

```
    k = 0
```

```
    for (i = 0; i < N; i++) {
```

```
        if (A[i] <= B)
            k++
```

```
    }
```

```
    if (k == 0 || k == 1 || k == N)
```

```
        return 0
```

```
    // Start with sliding window
```

```
    // 1. Get result of first window
```

```
    bad = 0
```

```
    for (i = 0; i < k; i++) {
```

```
        if (A[i] > B) bad++
```

```
    }
```

```
    // 2. Carry forward the count
```

```
    ans = bad
```

```
    s = 1
```

$e = k$

while ($e < N$) {

if ($A[s-1] > B$) $bad--$

if ($A[e] > B$) $bad++$

$s++$

$e++$

$ans = \min(ans, bad)$

}

return ans

}

Quiz 4

TC : $O(N)$

SC : $O(1)$

Break

||

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$A[s-1]$

↓

Check if prev element was bad $\Rightarrow bad--$

↓

arr

=

25

30

2

18

7

6

9

50

3

$B = 10$

count $\rightarrow 3$

↑↑

Check if next

element is bad $\Rightarrow bad++$

↑↑

$A[e]$

Q3

Given a matrix $A[N][N]$, print its boundary in clockwise direction

↓
Square matrix

	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8	9	10
2	11	12	13	14	15
3	16	17	18	19	20
4	21	22	23	24	25

1 2 3 4 5 10 15 20 25
24 23 22 21 16 11 6

	0	1	2
0	1	2	3
1	4	5	6
2	7	8	9

1 2 3 6 9 8 7 4

Idea

1. First row $N-1$ →
2. Last col $N-1$ ↓
3. Last row $N-1$ ←
4. First col $N-1$ ↑

4 loops

```
printBoundaryClockwise(int [][]A, int N, int i=0, int j=0) {
    if(N==1) { print(A[i][j]); return; }
```

1) Print (N-1) elements from first row →

```
for( k=1; k<N; k++) {
    print(A[i][j])
    j++
}
```

→ i=0, j=N-1

2) Print (N-1) elements from last col ↓

```
for( k=1; k<N; k++) {
    print(A[i][j])
    i++
}
```

→ i=N-1, j=N-1

3) Print (N-1) elements from last row ←

```
for( k=1, k<N; k++) {
    print(A[i][j])
    j--
}
```

→ i=N-1, j=0

4) Print (N-1) elements from first col ↑

```
for( k=1, k<N; k++) {
    print(A[i][j])
    i--
}
```

→ i=0, j=0

```
}
```


Quiz 5

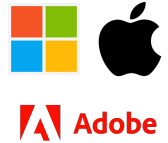
Total iterations - $(N-1) \times 4$
 $= 4N-4$ iterations

TC: $O(N)$

SC: $O(1)$

Q4

Given a matrix $A[N][N]$, print it in spiral form. 
square



	0	1	2	3	4
0	1	2	3	4	5
1	6	7	8	9	10
2	11	12	13	14	15
3	16	17	18	19	20
4	21	22	23	24	25

First cell index

i	j
0	0
1	1
2	2

2^{+1} 2^{+1} 2^{+1}

Size of box

N
5
3
1

2^{-2} 2^{-2} 2^{-2}

\downarrow
1

	0	1	2	3	4	5
0	1	2	3	4	5	6
1	7	8	9	10	11	12
2	13	14	15	16	17	18
3	19	20	21	22	23	24
4	25	26	27	28	29	30
5	31	32	33	34	35	36

First cell index

i	j
0	0
1	1
2	2

2^{+1} 2^{+1} 2^{+1}

$i++$ $j++$

Size of box

N
6
4
2

2^{-2} 2^{-2} 2^{-2}

\downarrow
 $N=0$

$N-=2$

- 1) Keep on printing boundary of box till you can.
- 2) Reduce the size of box after each cycle.

```
printSpiralClockwise(int [][]A, int N) {
```

```
    i=0, j=0
```

```
    while ( N > 0 ) {
```

```
        print Boundary Clockwise (A, N, i, j) ← Q7
```

```
        i++
```

```
        j++
```

```
        N -= 2
```

```
    }
```

```
}
```

Quiz 6

TC: $O(N^2)$

SC: $O(1)$

Traversing over matrix in spiral order

N^2 elements in matrix

↳ N^2 iterations in total

⇓
TC: $O(N^2)$

Doubts

Thank
you

Assignments before HW

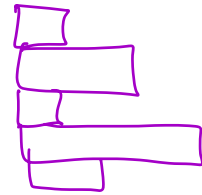
2D Array containing all subarrays

$$\text{No of subarrays} = \frac{N(N+1)}{2}$$

$$\text{ans} = \frac{N(N+1)}{2} \times \underline{\hspace{1cm}}$$

Jagged
Arrays

int [][] ans = new int [$\frac{N(N+1)}{2}$] []



for (i = 0; i < $\frac{N(N+1)}{2}$; i++) {

subarray = ~~_____~~

ans [i] = subarray

}

$$\text{ans} = [0] \times \frac{N(N+1)}{2}$$

Good
Night

Thank
You

9 PM on Friday - Contest
10:50 PM - Contest Discussion