Assignment 6

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I. PROB 5.9

Problem: Suppose that two cards are drawn at random from a deck of cards. Let X be the number of aces obtained. Then the value of E(X) is .

(a)
$$\frac{37}{221}$$

(b) $\frac{5}{13}$
(c) $\frac{1}{13}$
(d) $\frac{2}{13}$

(c)
$$\frac{1}{13}$$

Number of ways to get 1 aces

= Number of ways to select 1 ace out of 4 ace cards \times Num

$$=^4 C_1 \times^{48} C_1$$

 $=4\times48$

= 192

Solution:

Let X: be the number of aces obtained we can get 0,1 or 2 aces So the value of x is 0,1 or 2

Total number of ways to draw 2 cards out of 52 is:

Total ways
$$=$$
 $^{52} C_2$ $= 1326$

P(X=0): Probability of getting zero aces Number of ways of getting zero aces

- = Number of ways to select 2 cards out of non ace
- = Number of ways to select 2 cards out of (52-4), 48 cards

$$={}^{48}C_2$$

=1128

$$P(X=0) = \frac{\text{Number of ways to get zero aces}}{\text{Total number of ways}}$$

$$= \frac{1128}{1326}$$

$$P(X = 1)$$
 i..e probability of getting 1 ace

$$P(X = 1) = \frac{\text{Number of ways to get 1 aces}}{\text{Total number of ways}}$$
$$= \frac{192}{1326}$$

$$P(X = 2)$$

i..e probability of getting 2 aces
Number of ways to get 2 aces

= Number of ways to select 2 ace out of 4 ace cards $=^4 C_2$ = 6

$$P(X = 2) = \frac{\text{Number of ways to get 2 aces}}{\text{Total number of ways}}$$
$$= \frac{6}{1326}$$

The probability distribution is:

X	0	1	2
P(X)	$\frac{1128}{1326}$	$\frac{192}{1326}$	$\frac{6}{1326}$

The expected value E(X) is given by

$$\mu = E(X) = \sum_{i=1}^{n} x_i p_i$$

$$= 0 \times \frac{1128}{1326} + 1 \times \frac{192}{1326} + 2 \times \frac{6}{1326}$$

$$= 0 + \frac{192 + 12}{1326}$$

$$= \frac{204}{13260}$$

$$= \frac{2}{13}$$

Thus option D stating the estimation of getting aces when drawing 2 cards from a deck of cards is $\frac{2}{13}$

Code source: https://github.com/harshal9876/ AI5002/blob/main/Assignment_6/Codes/ Assignment_6.py LaTex:https://github.com/harshal9876/ AI5002/blob/main/Assignment_6/ Assignment_6.tex