

8 Puzzle problem using BFS

In the problem, square will have

$N+1$ tiles, where $N = 8, 15, \dots$

If $N = 8$, square will have 9 tiles

In the problem, initial state will be given & we have to reach goal state/goal config.

Solved by moving the tile one by one empty space & then achieve goal state

Rules:-

→ Empty can only move in 4 directions

Can't move diagonally & only

1 step at a time.

→

0	x	0
x	#	x
0	x	0

Tiles at 0 - no of possible moves

" at x - " " "

" at # - " " "

Complexity → $O(b^d)$ where

b - branching factor

d - depth factor

Worst case - 3^{120}

Branching factor b = all possible moves by empty tile at each position
no of tiles

$$= \frac{24}{9} = 3$$

depth factor - initially 0

As we explore nodes depth factor increases

3 possible moves

1	2	3
4	5	6
7	8	

right

up

down

(2)

(3)

(4)

1	2	3
4	5	6
7	8	

1	2	3
4	5	6
7	8	

1	2	3
4	5	6
7	8	

Similarly continue branching nodes

Worst case complexity as per Panda as per

def bfs (src, target): (BFS code)

queue = []
queue.append(src)
exp = []

while len(queue) > 0:
source = queue.pop(0)
exp.append(source)

print(source)

if source == target:
print("Success")
return

pos_moves to do = []

pos_moves to do = possible_moves(source)

for move in pos_moves to do:

if move not in exp and move not in queue:

queue.append(move)

def possible_moves(state, moves):

b - state index (0)

$d = []$

if b not in $[0, 1, 2]$:

$d.append('u')$

if b not in $[6, 7, 8]$:

$d.append('d')$

if b not in $[0, 3, 6]$:

$d.append('l')$

if b not in $[2, 5, 8]$:

$d.append('r')$

pos_moves = it can = []

for i in d :

pos_moves = it can append gen(state, i)

return [move it can for move it can in pos_moves it can if move it can not in (state)]

def gen(state, m, b):

temp = state.copy()

if $m == 'u'$:

temp[b+3], temp[b] = temp[b], temp[b+3]

temp[b-3]

if $m == 'd'$:

temp[b+3], temp[b] = temp[b], temp[b+3]

temp[b-3]

```
        return temp
initial_state = [1, 2, 3, 4, 5, 6, 7, 8, -1]
target_state = [1, 2, 3, 4, 5, 6, 7, 8, -1]

bfs(initial_state, target_state)
```



```
1 2 3
4 5 6
7 8
```

```
Success
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