

$$y_i = \underbrace{f(x_i)}_{\substack{\downarrow \\ E(y/x_i)}} + \epsilon_i$$

$$y_i / x_i \sim N(\underbrace{\omega^T \phi(x_i)}_{y/x_i}, \sigma)$$

$$\underbrace{E(y_i/x)}_{\downarrow \omega^T \phi(x)} \quad T = \{ (x_1, y_1), (x_2, y_2), \dots, (x_n, y_n) \}$$

$$y_i / x_i \sim N(\omega^T \phi(x_i), \sigma)$$

$$\underline{P(\theta/D) = P(D/\theta)P(\theta)}$$

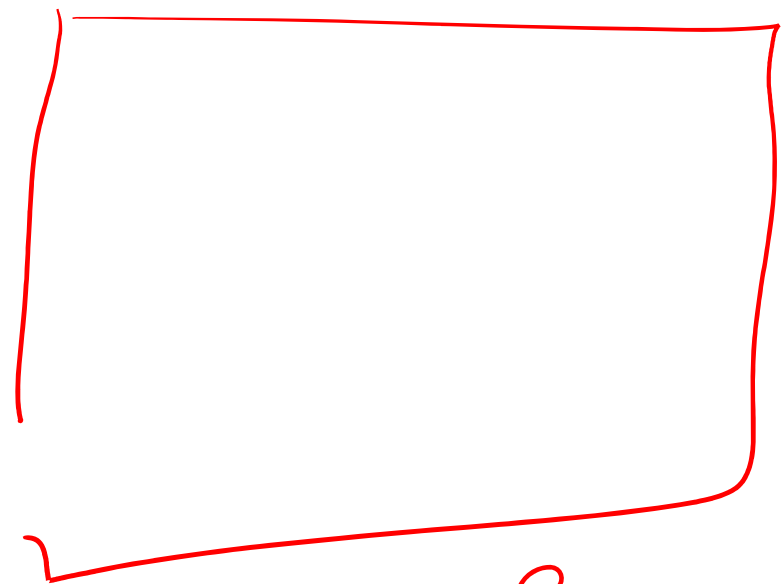
DCL

$$D = \{x_1, x_2, \dots, x_n\}$$

Find θ from sample D ,

$$\arg \max_{\theta} P(\theta/D)$$

$$= \max_{\theta} P(D/\theta)P(\theta)$$



$D(\theta)$ Population

$$\max_{\theta} P(D/\theta)$$

$$\max_{\theta} \mathcal{L}(D/\theta)$$

$$\max_{\theta} \mathcal{L}((x_1, x_2, \dots, x_N) / \theta)$$

$$\max_{\theta} \prod_{i=1}^N \mathcal{L}(x_i / \theta)$$

$$\max_{\theta} \log \prod_{i=1}^N \mathcal{L}(x_i / \theta)$$

$$\max_{\theta} \sum_{i=1}^N \log \mathcal{L}(x_i / \theta)$$

$$S = \mathcal{N}(\mu, \sigma)$$

$$x_i \sim \mathcal{N}(\mu, \sigma)$$

$$\max_{\mu} \sum_{i=1}^N \log \mathcal{L}(x_i / \mu)$$

$$\max_u \sum_{i=1}^N \log \left(\frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{1}{2} \left(\frac{x_i - u}{\sigma} \right)^2} \right)$$

$$= \max_u \left(\sum_{i=1}^N \log \left(\frac{1}{\sqrt{2\pi}\sigma} \right) - \sum_{i=1}^N \frac{1}{2} \left(\frac{x_i - u}{\sigma} \right)^2 \right)$$

$$\sigma = \frac{1}{N} \sum_{i=1}^N (x_i - u)^2$$

$$\Rightarrow \sum_{i=1}^N \frac{1}{\sigma} (x_i - u) = 0$$

$$\Rightarrow \sum_{i=1}^N (x_i - u) = 0$$

$$u = \frac{1}{N} \sum_{i=1}^N x_i$$

max T

$$\max_w P((y_1, y_2, \dots, y_N) / (x_1, x_2, \dots, x_N))$$

$$\max_w \prod_{i=1}^N P(y_i / x_i)$$

$$\max_w \prod_{i=1}^N \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{1}{2} \left(\frac{y_i - w^T \phi(x_i)}{\sigma} \right)^2}$$

$$\max_w \sum_{i=1}^N \log \left(\frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{1}{2} \left(\frac{y_i - w^T \phi(x_i)}{\sigma} \right)^2} \right)$$

$$\max_w \left(\underbrace{\sum_{i=1}^N \log \left(\frac{1}{\sqrt{2\pi}\sigma} \right)}_{\text{constant}} = \underbrace{\frac{1}{2\sigma^2} \sum_{i=1}^N (y_i - w^T \phi(x_i))^2}_{\text{loss}} \right)$$

$$\max_w \sum_{i=1}^N (y_i - w^T \phi(x_i))^2$$

$$\Rightarrow \min_w \sum_{i=1}^N (y_i - w^T \phi(x_i))^2$$