

## Hill Cipher

The Hill Cipher is a classical polygraphic substitution cipher, a type of encryption technique that uses linear algebra (matrices) to encrypt blocks of letters together rather than one at a time.

Working:

Every letter is assigned a number, A=0, B=1, C=2....Z=25.

Encryption Formula:  $C = K \times P \pmod{26}$

P is plaintext vector, K is the key matrix, and C is the ciphertext vector.

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Example:

Let the word be MIST.

Let the key be  $\begin{bmatrix} 3 & 3 \\ 2 & 5 \end{bmatrix}$

dividing it into pairs (since key is  $2 \times 2$ ): MI and ST

M	12
I	8
S	18
T	19

Pair 1: MI - [12, 8]

$$\begin{bmatrix} 3 & 3 \\ 2 & 5 \end{bmatrix} \begin{bmatrix} 12 \\ 8 \end{bmatrix} = \begin{bmatrix} 60 \\ 76 \end{bmatrix}$$

$60 \bmod 26 = 8$ ,  $76 \bmod 26 = 24$

[8 24] is [I Y]

First ciphertext pair = **IY**

Pair 2: ST - [18, 19]

$$\begin{bmatrix} 3 & 3 \\ 2 & 5 \end{bmatrix} \begin{bmatrix} 18 \\ 19 \end{bmatrix} = \begin{bmatrix} 111 \\ 131 \end{bmatrix}$$

$111 \bmod 26 = 7$ ,  $131 \bmod 26 = 1$

[7 1] is [H B]

Second ciphertext pair = **HB**

Final Ciphertext: **IYHB**

## Rail Fence Cipher

The Rail Fence Cipher is a transposition cipher, which means letters are rearranged and not substituted.

It writes the message in a zigzag pattern across multiple "rails" (rows), and then reads it row by row to form the ciphertext.

For example, to encrypt the message 'WE ARE DISCOVERED' with 3 "rails":

W				E				C				R		
	E		R		D		S		O		E		E	
		A				I				V				D

(Spaces and punctuation are omitted.)

Then the text is read horizontally: WECR ERDSOEE AIVD

Here the no of rails is 3. It is decided by the key given

## Affine Cipher

The Affine Cipher is a monoalphabetic substitution cipher, each letter in the plaintext is mapped to exactly one letter in the ciphertext.

It's based on a simple mathematical formula using modular arithmetic.

Encryption Formula:

For each letter  $x$  (where  $A=0, B=1, \dots, Z=25$ ):

$$E(x) = (ax + b) \bmod 26$$

Where:

- $a$  = multiplicative key (must be coprime with 26)
- $b$  = additive key (any number between 0–25)

Example: MIST

M	12
I	8
S	18
T	19

Taking  $a=5, b=8$ :  $E(x) = (5x + 8) \bmod 26$

$x$	$5x+8$	$(5x+8) \bmod 26$	Cipher Letter
12	68	16	Q
8	48	22	W
18	98	20	U
19	103	25	Z

Ciphertext = **QWUZ**

