

PSG COLLEGE OF TECHNOLOGY, COIMBATORE - 641 004

Department of Applied Mathematics and Computational Sciences

MSc TCS & Sem 5

CONTINUOUS ASSESSMENT TEST 2 Date: 28.10.2025

23XT52- Computational Number Theory and Cryptography

Time: 1 Hour 30 min.

Maximum Marks: 40

INSTRUCTIONS:

1. Answer ALL questions. Each question carries 20 Marks.
2. Subdivision (a) carries 3 marks each, subdivision (b) carries 7 marks each and subdivision (c) carries 10 marks each.
3. Course Outcome Table :

Qn.1	CO.3	Qn.2	CO.4
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1. a) i) What is the cipher text corresponding to the RSA plain text  $C = 10$ , when RSA values are  $n = 35$ , and  $e = 5$ ? [BTL3]

ii) Justify whether a known-message attack is feasible on the ElGamal cryptosystem. [BTL3]

b) Write any three potential attacks on RSA cryptosystem. [BTL2]

c) Write the Elliptic curve encryption and decryption process. Suppose Bob selects  $p = 67$  and the elliptic curve  $y^2 = x^3 + 2x + 3$  over  $GF(13)$ . He also selects his secret key as  $d = 4$  and  $g = (2, 22)$ . Find out the corresponding public key. (1000) [BTL3]

2. a) i) What is MAC? What is the difference between a MAC and a hash function? [BTL2]

ii) What is dictionary attack on password authentication? [BTL2]

b) Explain merkle damgard hash function. Also, assume we have a very simple message digest. The message digest is just one number between 0 and 25. The digest is initially set to 0. The cryptographic hash function adds the current value of the digest to the value of the current character (between 0 and 25). Addition is in modulo 26. What is the value of the digest if the message is "HELLO"? [BTL3]

c) Compute the private key and sign the message "5" using RSA signature scheme with the given values  $p = 7$ ,  $q = 11$  and  $e = 7$ . Also compute the ElGamal signature for the given values  $e_1 = 10$ ,  $d = 3$ ,  $p = 19$ ,  $M = 17$  and  $r = 5$ . (2000) [BTL3]