

GWP 3 Submission

Group No - 846

- Primary Theme - Statistical Related Risk: Volatility & Statistical Related Risk: Correlation
- Secondary Theme - Fallout: Model Failure & Crises

Section - 1 (Theoretical Set up)

1. Statistical Related Risk: Volatility

Volatility, also called Standard Deviation, is a measure of dispersion of data points with respect to its mean. It is square root of Variance.

$$\sigma^2(X) = \frac{\Sigma(X - E(X))^2}{n - 1}$$

$$\sigma(X) = \sqrt{\left(\frac{\Sigma(X - E(X))^2}{n - 1}\right)}$$

Covariance is defined as measure of whether two variables move inline with each other or Anti to each other. It can range from minus infinity to plus infinity.

$$Covar(X, Y) = \frac{\Sigma(X - E(X)) * (Y - E(Y))}{n - 1}$$

1. Statistical Related Risk: Correlation

Correlation is defined as the strength of linear relationship between two variables with an assumption that both variables have a linear relationship. It ranges from +1 to -1. The value of 0 corresponds to no correlation.

$$\rho = \frac{Covar(X, Y)}{\sigma(X) * \sigma(Y)}$$

As an example for both Correlation and Volatility, we will illustrate Fama French 3 Factor model.

Fama French 3 Factor model tries to model returns based on three factors:

- Benchmark excess returns over the risk free rate
- Size premium
- Value premium

7	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN
8	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN
9	Average Value Weighted Returns -- Monthly	NaN	NaN	NaN	NaN	NaN	NaN	NaN	NaN
10	NaN	Agric	Food	Soda	Beer	Smoke	Toys	Fun	Books
11	192607	2.37	0.12	-99.99	-5.19	1.29	8.65	2.5	50.21
12	192608	2.23	2.68	-99.99	27.03	6.5	16.81	-0.76	42.98
13	192609	-0.57	1.58	-99.99	4.02	1.26	8.33	6.42	-4.91
14	192610	-0.46	-3.68	-99.99	-3.31	1.06	-1.4	-5.09	5.37
15	192611	6.75	6.26	-99.99	7.29	4.55	0	1.82	-6.4
16	192612	-3.27	0.18	-99.99	-4.09	2.55	2.48	2.14	-3.29
17	192701	-3.66	-0.16	-99.99	0.57	-0.35	1.73	1.88	1.21
18	192702	7.65	3.66	-99.99	12.83	1.49	-6.12	2.43	10.31
19	192703	-0.6	2.74	-99.99	-13.56	5.51	-8.89	1.93	-7.83

20 rows × 50 columns

```
In [5]: #Extracting the value weighted returns monthly data
value_wted_returns=ind_port.iloc[11:1162,:]
value_wted_returns.columns=['Time', 'Agric', 'Food', 'Soda', 'Beer', 'Smoke', 'Toys', 'Books', 'Hshld', 'Clths', 'Hlth', 'MedEq', 'Drugs', 'Chems', 'Rubbr', 'Txlts', 'BldMt', 'Cnstr', 'Steel', 'FabPr', 'Mach', 'ElcEq', 'Autos', 'Aero', 'Ships', 'Guns', 'Gold', 'Mines', 'Coal', 'Oil', 'Util', 'Telcm', 'PerSv', 'BusSv', 'Hardw', 'Softw', 'Chips', 'LabEq', 'Paper', 'Boxes', 'Trans', 'Whlsl', 'Rtail', 'Meals', 'Banks', 'Insur', 'RlEst', 'Fin', 'Other']
value_wted_returns.reset_index(inplace=True)
value_wted_returns.drop(columns=['index'],inplace=True)
value_wted_returns.head()
```

C:\Users\Admin\AppData\Local\Temp\ipykernel_12824\425753230.py:11: SettingWithCopyWarning:
A value is trying to be set on a copy of a slice from a DataFrame

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy
value_wted_returns.drop(columns=['index'],inplace=True)

```
Out[5]:
```

	Time	Agric	Food	Soda	Beer	Smoke	Toys	Fun	Books	Hshld	...	Boxes	Trans	Whlsl	Rtail	Meals
0	192607	2.37	0.12	-99.99	-5.19	1.29	8.65	2.5	50.21	-0.48	...	7.7	1.92	-23.79	0.07	1.87
1	192608	2.23	2.68	-99.99	27.03	6.5	16.81	-0.76	42.98	-3.58	...	-2.38	4.85	5.39	-0.75	-0.13
2	192609	-0.57	1.58	-99.99	4.02	1.26	8.33	6.42	-4.91	0.73	...	-5.54	0.08	-7.87	0.25	-0.56
3	192610	-0.46	-3.68	-99.99	-3.31	1.06	-1.4	-5.09	5.37	-4.68	...	-5.08	-2.62	-15.38	-2.2	-4.11
4	192611	6.75	6.26	-99.99	7.29	4.55	0	1.82	-6.4	-0.54	...	3.84	1.61	4.67	6.52	4.33

5 rows × 50 columns

```
In [6]: value_wted_returns.shape
```

#This shape corresponds to similar data in the csv file

Out[6]: (1151, 50)

```
In [7]: #Importing and Extracting the required Fama-French Data
ff_data=pd.read_csv('./F-F_Research_Data_5_Factors_2x3.csv')
ff_data.head(20)
```

Out[7]:

This file was created by CMPT_ME_BEME_OP_INV_RETS using the 202205 CRSP database.		Unnamed: 1	Unnamed: 2	Unnamed: 3	Unnamed: 4	Unnamed: 5	Unnamed: 6
0	The 1-month TBill return is from Ibbotson and ...	NaN	NaN	NaN	NaN	NaN	NaN
1	NaN	NaN	NaN	NaN	NaN	NaN	NaN
2	NaN	Mkt-RF	SMB	HML	RMW	CMA	RF
3	196307	-0.39	-0.44	-0.89	0.68	-1.23	0.27
4	196308	5.07	-0.75	1.68	0.36	-0.34	0.25
5	196309	-1.57	-0.55	0.08	-0.71	0.29	0.27
6	196310	2.53	-1.37	-0.14	2.8	-2.02	0.29
7	196311	-0.85	-0.89	1.81	-0.51	2.31	0.27
8	196312	1.83	-2.07	-0.08	0.03	-0.04	0.29
9	196401	2.24	0.11	1.47	0.17	1.51	0.3
10	196402	1.54	0.3	2.74	-0.05	0.9	0.26
11	196403	1.41	1.36	3.36	-2.21	3.19	0.31
12	196404	0.1	-1.59	-0.58	-1.27	-1.04	0.29
13	196405	1.42	-0.64	1.82	-0.16	0.14	0.26
14	196406	1.27	0.31	0.63	-0.28	-0.15	0.3
15	196407	1.74	0.47	0.75	0.04	1.94	0.3
16	196408	-1.44	0.42	0.08	0.15	0.33	0.28
17	196409	2.69	-0.33	1.7	-0.54	0.61	0.28
18	196410	0.59	0.91	1.17	-0.38	0.43	0.29
19	196411	0	-0.15	-1.96	0.62	-0.26	0.29

```
In [8]: ff_monthly_data=ff_data.iloc[3:710,:]
ff_monthly_data.columns=['Time', 'Mkt-RF', 'SMB', 'HML', 'RMW', 'CMA', 'RF']
ff_monthly_data.head()
ff_monthly_data.reset_index(inplace=True)
ff_monthly_data.drop(columns=['index'],inplace=True)
ff_monthly_data.head()
```

C:\Users\Admin\AppData\Local\Temp\ipykernel_12824\3190668661.py:5: SettingWithCopyWarning:
A value is trying to be set on a copy of a slice from a DataFrame

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy
ff_monthly_data.drop(columns=['index'],inplace=True)

Out[8]:

Time	Mkt-RF	SMB	HML	RMW	CMA	RF
------	--------	-----	-----	-----	-----	----

0	196307	-0.39	-0.44	-0.89	0.68	-1.23	0.27
1	196308	5.07	-0.75	1.68	0.36	-0.34	0.25
2	196309	-1.57	-0.55	0.08	-0.71	0.29	0.27
3	196310	2.53	-1.37	-0.14	2.8	-2.02	0.29
4	196311	-0.85	-0.89	1.81	-0.51	2.31	0.27

In [9]: `ff_monthly_data.shape`

Out[9]: (707, 7)

1. Preprocessing of data

For returns dataset

- For industry portfolio data, it is explicitly given that the value of -99.99 or -999 correspond to missing data. So, in order to improve data quality we impute values(mean) these columns(industries).

In [11]: `#proportion of missing data`
`mask=(value_wted_returns== '-99.99') | (value_wted_returns== '-999')`
`mask.mean()`

Out[11]:

Time	0.000000
Agric	0.000000
Food	0.000000
Soda	0.385752
Beer	0.000000
Smoke	0.000000
Toys	0.000000
Fun	0.000000
Books	0.000000
Hshld	0.000000
Clths	0.000000
Hlth	0.448306
MedEq	0.000000
Drugs	0.000000
Chems	0.000000
Rubbr	0.052129
Txtls	0.000000
BldMt	0.000000
Cnstr	0.000000
Steel	0.000000
FabPr	0.385752
Mach	0.000000
ElcEq	0.000000
Autos	0.000000
Aero	0.000000
Ships	0.000000
Guns	0.385752
Gold	0.385752
Mines	0.000000
Coal	0.000000
Oil	0.000000
Util	0.000000
Telcm	0.000000
PerSv	0.010426
BusSv	0.000000
Hardw	0.000000
Softw	0.406603
Chips	0.000000

```

LabEq      0.000000
Paper      0.031277
Boxes      0.000000
Trans      0.000000
Whlsl      0.000000
Rtail      0.000000
Meals      0.000000
Banks      0.000000
Insur      0.000000
RlEst      0.000000
Fin        0.000000
Other      0.000000
dtype: float64

```

```

In [12]: impute_col=['Rubbr','PerSv','Paper','Soda ', 'Hlth ', 'FabPr', 'Guns ', 'Gold ', 'Softw']

value_wted_returns[value_wted_returns.columns[1:]] = value_wted_returns[value_wted_returns
value_wted_returns.info()

```

```

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 1151 entries, 0 to 1150
Data columns (total 50 columns):
#   Column      Non-Null Count  Dtype
---  -
0   Time        1151 non-null   object
1   Agric       1151 non-null   float64
2   Food        1151 non-null   float64
3   Soda        1151 non-null   float64
4   Beer        1151 non-null   float64
5   Smoke       1151 non-null   float64
6   Toys        1151 non-null   float64
7   Fun         1151 non-null   float64
8   Books       1151 non-null   float64
9   Hshld       1151 non-null   float64
10  Clths       1151 non-null   float64
11  Hlth        1151 non-null   float64
12  MedEq       1151 non-null   float64
13  Drugs       1151 non-null   float64
14  Chems       1151 non-null   float64
15  Rubbr       1151 non-null   float64
16  Txtls       1151 non-null   float64
17  BldMt       1151 non-null   float64
18  Cnstr       1151 non-null   float64
19  Steel       1151 non-null   float64
20  FabPr       1151 non-null   float64
21  Mach        1151 non-null   float64
22  ElcEq       1151 non-null   float64
23  Autos       1151 non-null   float64
24  Aero        1151 non-null   float64
25  Ships       1151 non-null   float64
26  Guns        1151 non-null   float64
27  Gold        1151 non-null   float64
28  Mines       1151 non-null   float64
29  Coal        1151 non-null   float64
30  Oil         1151 non-null   float64
31  Util        1151 non-null   float64
32  Telcm       1151 non-null   float64
33  PerSv       1151 non-null   float64
34  BusSv       1151 non-null   float64
35  Hardw       1151 non-null   float64
36  Softw       1151 non-null   float64
37  Chips       1151 non-null   float64
38  LabEq       1151 non-null   float64
39  Paper       1151 non-null   float64
40  Boxes       1151 non-null   float64
41  Trans       1151 non-null   float64

```

```

42  Whlsl      1151 non-null    float64
43  Rtail      1151 non-null    float64
44  Meals      1151 non-null    float64
45  Banks      1151 non-null    float64
46  Insur      1151 non-null    float64
47  RlEst      1151 non-null    float64
48  Fin        1151 non-null    float64
49  Other      1151 non-null    float64

```

dtypes: float64(49), object(1)

memory usage: 449.7+ KB

C:\Users\Admin\AppData\Local\Temp\ipykernel_12824\1382093669.py:3: SettingWithCopyWarning:

A value is trying to be set on a copy of a slice from a DataFrame.

Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy

```

value_wted_returns[value_wted_returns.columns[1:]] = value_wted_returns[value_wted_returns.columns[1:]].astype(float)

```

```

In [13]: #impute with mean values
mask=(value_wted_returns!=-99.99)&(value_wted_returns!=-999)
impute_values=value_wted_returns[impute_col][mask].dropna().mean()
impute_values

```

```

Out[13]: Rubbr      1.043937
PerSv     0.621921
Paper     0.904520
Soda      1.124394
Hlth      1.010283
FabPr     0.830693
Guns      1.284961
Gold      0.925449
Softw     1.041669
dtype: float64

```

```

In [14]: #impute values
for i in impute_col:
    value_wted_returns[i]=np.where(((value_wted_returns[i]==-99.99)|(value_wted_returns[impute_values[i],value_wted_returns[i])

```

C:\Users\Admin\AppData\Local\Temp\ipykernel_12824\2214042178.py:3: SettingWithCopyWarning:

A value is trying to be set on a copy of a slice from a DataFrame.

Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy

```

value_wted_returns[i]=np.where(((value_wted_returns[i]==-99.99)|(value_wted_returns['Rubbr']==-999)),

```

- For F-F dataset, we don't need any particular preprocessing except converting the data type to float(except the 'Time' column).
- Furthermore, we do not disturb the 'Time' column format as they are same across all dataframes.

1. Analysis

```

In [16]: #Industry wise average returns
ri_bar=value_wted_returns.drop(columns=['Time']).mean().sort_values()
ri_bar

```

```

Out[16]: Other      0.727437

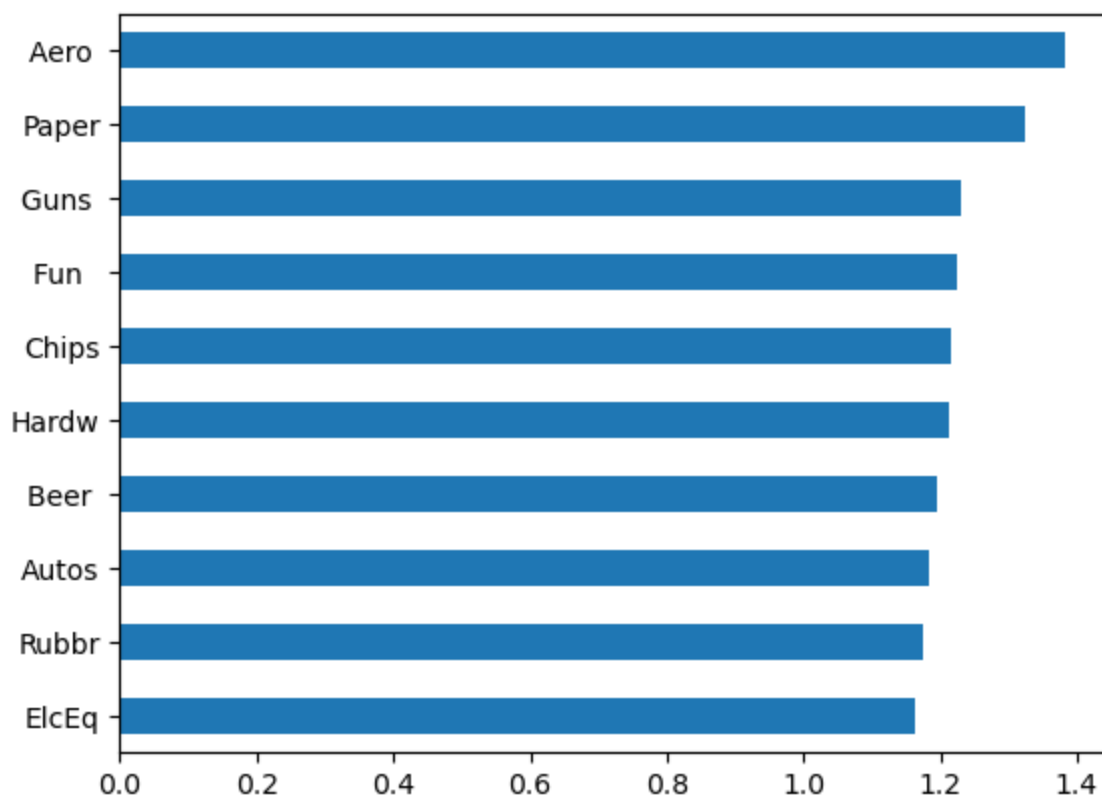
```

FabPr	0.824516
RlEst	0.832068
Whlsl	0.842667
Telcm	0.843649
Util	0.887124
PerSv	0.912913
Trans	0.923162
Hshld	0.928323
Clths	0.938375
Steel	0.947637
Txtls	0.959652
Food	0.970565
Gold	0.976316
Agric	0.977194
Books	0.985343
Toys	0.988471
BusSv	0.994057
BldMt	1.003545
Ships	1.004353
Hlth	1.010283
Softw	1.021270
Mines	1.034205
Rtail	1.043675
Cnstr	1.043840
Oil	1.045048
Chems	1.054466
Boxes	1.064761
Meals	1.068593
Insur	1.075699
Mach	1.079201
Fin	1.089470
Coal	1.091390
Drugs	1.103110
MedEq	1.134683
Soda	1.142685
Smoke	1.145447
Banks	1.152632
LabEq	1.161633
ElcEq	1.162580
Rubbr	1.173846
Autos	1.183840
Beer	1.195864
Hardw	1.211955
Chips	1.216994
Fun	1.224196
Guns	1.230628
Paper	1.323356
Aero	1.382276

dtype: float64

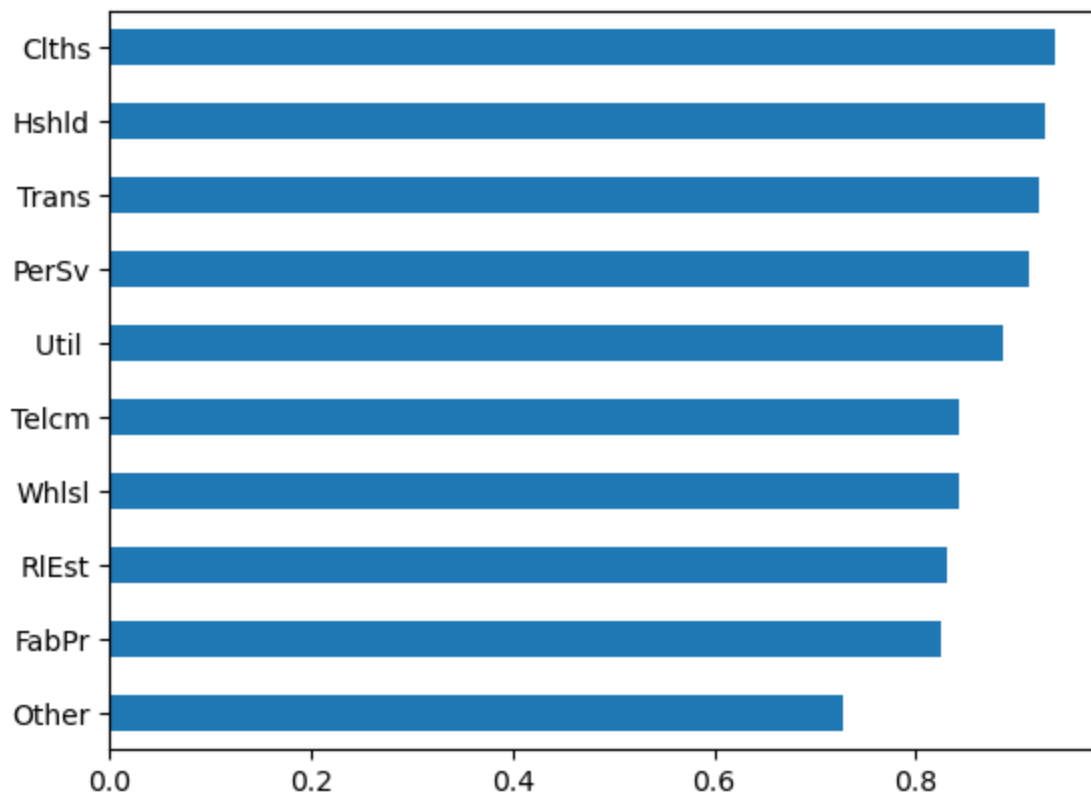
```
In [17]: #Plot top 10 histogram  
ri_bar.tail(10).plot(kind='barh')
```

```
Out[17]: <AxesSubplot:>
```

```
In [18]: #Plot bottom 10 histogram
ri_bar.head(10).plot(kind='barh')
```

```
Out[18]: <AxesSubplot:>
```



```
In [19]: summary_return=value_wted_returns.describe().T
summary_return
```

```
Out[19]:
```

	count	mean	std	min	25%	50%	75%	max
Agric	1151.0	0.977194	7.460563	-36.45	-3.065	0.760000	4.760	91.34

	Food	1151.0	0.970565	4.753352	-27.87	-1.320	1.070000	3.405	32.63
	Soda	1151.0	1.142685	4.861558	-26.26	0.050	1.124394	2.540	38.27
	Beer	1151.0	1.195864	7.112490	-29.19	-2.100	1.000000	4.405	87.61
	Smoke	1151.0	1.145447	5.814748	-24.93	-2.290	1.300000	4.585	33.04
	Toys	1151.0	0.988471	9.902224	-43.34	-4.345	0.830000	5.825	140.45
	Fun	1151.0	1.224196	9.264223	-44.28	-3.175	1.260000	5.930	69.57
	Books	1151.0	0.985343	7.843385	-34.81	-2.935	0.700000	4.585	54.75
	Hshld	1151.0	0.928323	5.761753	-34.97	-1.865	1.050000	4.110	58.33
	Clths	1151.0	0.938375	6.143087	-30.85	-2.215	0.960000	4.055	41.40
	Hlth	1151.0	1.010283	5.999815	-39.11	0.360	1.010283	1.890	36.47
	MedEq	1151.0	1.134683	6.195813	-25.97	-2.285	1.270000	4.720	30.28
	Drugs	1151.0	1.103110	5.677732	-35.47	-1.940	1.100000	4.120	39.50
	Chems	1151.0	1.054466	6.304059	-33.30	-2.395	1.070000	4.510	46.60
	Rubbr	1151.0	1.173846	7.786581	-32.39	-2.175	1.043937	4.575	98.43
	Txtls	1151.0	0.959652	7.786859	-35.96	-3.085	1.050000	5.105	58.93
	BldMt	1151.0	1.003545	6.915460	-31.81	-2.435	1.240000	4.550	42.41
	Cnstr	1151.0	1.043840	9.348882	-38.04	-3.800	0.820000	5.460	67.40
	Steel	1151.0	0.947637	8.536370	-32.91	-3.735	1.140000	5.315	80.84
	FabPr	1151.0	0.824516	5.839429	-32.50	-0.790	0.830693	2.475	30.38
	Mach	1151.0	1.079201	7.215400	-33.35	-2.685	1.490000	4.805	52.08
	ElcEq	1151.0	1.162580	7.598979	-34.53	-2.725	1.060000	5.265	59.58
	Autos	1151.0	1.183840	8.285257	-36.42	-2.985	0.960000	5.125	81.88
	Aero	1151.0	1.382276	9.232740	-40.40	-3.335	1.280000	5.515	72.37
	Ships	1151.0	1.004353	8.044326	-34.42	-3.030	1.030000	4.965	63.37
	Guns	1151.0	1.230628	5.086981	-30.08	0.055	1.284961	2.630	32.64
	Gold	1151.0	0.976316	8.153909	-33.53	-1.410	0.925449	2.690	80.09
	Mines	1151.0	1.034205	7.291411	-34.75	-2.955	0.780000	4.970	46.10
	Coal	1151.0	1.091390	11.003785	-40.72	-4.500	0.670000	5.915	125.43
	Oil	1151.0	1.045048	6.381901	-34.68	-2.430	0.940000	4.560	39.08
	Util	1151.0	0.887124	5.473849	-33.05	-1.675	1.060000	3.620	43.46
	Telcm	1151.0	0.843649	4.612309	-21.56	-1.510	0.910000	3.255	28.17
	PerSv	1151.0	0.912913	9.081922	-39.29	-3.220	0.621921	4.975	84.67
	BusSv	1151.0	0.994057	6.911879	-40.28	-2.205	1.220000	4.235	56.83
	Hardw	1151.0	1.211955	7.312472	-34.75	-2.785	1.300000	5.250	54.04
	Softw	1151.0	1.021270	8.506101	-35.94	-0.735	1.041669	2.665	73.65
	Chips	1151.0	1.216994	8.553929	-42.15	-3.370	1.550000	6.040	62.78
	LabEq	1151.0	1.161633	6.722871	-33.22	-2.720	1.300000	5.105	25.42
	Paper	1151.0	1.323356	15.042804	-62.08	-3.075	0.904520	4.520	300.00

Boxes	1151.0	1.064761	6.077639	-29.24	-2.305	1.180000	4.585	43.19
Trans	1151.0	0.923162	7.073449	-34.61	-2.760	1.020000	4.400	65.40
Whlsl	1151.0	0.842667	7.272389	-43.85	-2.460	1.140000	4.295	57.64
Rtail	1151.0	1.043675	5.956936	-30.41	-2.095	1.010000	4.290	43.51
Meals	1151.0	1.068593	6.477742	-31.61	-2.295	1.250000	4.610	30.65
Banks	1151.0	1.152632	7.020402	-34.00	-2.090	1.200000	4.595	41.79
Insur	1151.0	1.075699	7.375539	-45.76	-2.300	1.010000	4.480	75.11
REst	1151.0	0.832068	9.575857	-52.54	-3.590	0.730000	5.025	66.02
Fin	1151.0	1.089470	7.644688	-39.47	-2.730	1.380000	5.025	66.79
Other	1151.0	0.727437	7.290271	-33.56	-2.970	0.790000	4.645	45.30

```
In [20]: #Inter-quartile Range
iqr=summary_return['75%']-summary_return['25%']
iqr.sort_values()
```

```
Out[20]: Hlth      1.530
Soda      2.490
Guns      2.575
FabPr     3.265
Softw     3.400
Gold      4.100
Food      4.725
Telcm     4.765
Util      5.295
Hshld     5.975
Drugs     6.060
Clths     6.270
Rtail     6.385
BusSv     6.440
Beer      6.505
Banks     6.685
Rubbr     6.750
Whlsl     6.755
Insur     6.780
Smoke     6.875
Boxes     6.890
Meals     6.905
Chems     6.905
BldMt     6.985
Oil       6.990
MedEq     7.005
Trans     7.160
Mach      7.490
Books     7.520
Paper     7.595
Other     7.615
Fin       7.755
Agric     7.825
LabEq     7.825
Mines     7.925
ElcEq     7.990
Ships     7.995
Hardw     8.035
Autos     8.110
Txtls     8.190
PerSv     8.195
REst      8.615
```

Aero 8.850
Steel 9.050
Fun 9.105
Cnstr 9.260
Chips 9.410
Toys 10.170
Coal 10.415
dtype: float64

```
In [199]: #Correlation analysis
value_wted_returns.iloc[:,1:].corr()
```

Out[199]:		Agric	Food	Soda	Beer	Smoke	Toys	Fun	Books	Hshld	Clths	...	
	Agric	1.000000	0.574797	0.216367	0.453961	0.420412	0.459495	0.555590	0.536256	0.534848	0.434004	...	0.5
	Food	0.574797	1.000000	0.412846	0.686322	0.655354	0.542316	0.668993	0.647818	0.774869	0.626494	...	0.7
	Soda	0.216367	0.412846	1.000000	0.343991	0.333403	0.254821	0.327058	0.313627	0.395066	0.421101	...	0.3
	Beer	0.453961	0.686322	0.343991	1.000000	0.454063	0.607033	0.617797	0.547501	0.661448	0.509862	...	0.5
	Smoke	0.420412	0.655354	0.333403	0.454063	1.000000	0.384018	0.473776	0.441969	0.547059	0.429566	...	0.5
	Toys	0.459495	0.542316	0.254821	0.607033	0.384018	1.000000	0.615032	0.581242	0.559627	0.538045	...	0.5
	Fun	0.555590	0.668993	0.327058	0.617797	0.473776	0.615032	1.000000	0.649313	0.687210	0.620490	...	0.6
	Books	0.536256	0.647818	0.313627	0.547501	0.441969	0.581242	0.649313	1.000000	0.644374	0.637933	...	0.6
	Hshld	0.534848	0.774869	0.395066	0.661448	0.547059	0.559627	0.687210	0.644374	1.000000	0.596720	...	0.7
	Clths	0.434004	0.626494	0.421101	0.509862	0.429566	0.538045	0.620490	0.637933	0.596720	1.000000	...	0.6
	Hlth	0.311403	0.376940	0.427470	0.287621	0.281326	0.325558	0.370281	0.374437	0.338893	0.492179	...	0.3
	MedEq	0.483310	0.644559	0.340335	0.557070	0.468249	0.527743	0.624478	0.576266	0.648280	0.555829	...	0.6
	Drugs	0.557769	0.729804	0.335449	0.622163	0.542798	0.510534	0.635772	0.570664	0.721105	0.515025	...	0.6
	Chems	0.601359	0.706716	0.350943	0.614611	0.498769	0.577666	0.701785	0.656437	0.730359	0.660119	...	0.7
	Rubbr	0.543954	0.640757	0.322992	0.587193	0.458486	0.565404	0.713794	0.652791	0.657455	0.639424	...	0.6
	Txtls	0.512388	0.647941	0.368965	0.601647	0.442467	0.592024	0.714447	0.694056	0.656363	0.726815	...	0.6
	BldMt	0.613849	0.747288	0.388123	0.683832	0.527976	0.672076	0.764784	0.737251	0.768605	0.724231	...	0.7
	Cnstr	0.497449	0.594044	0.273748	0.551092	0.429212	0.579698	0.646919	0.655441	0.598475	0.621958	...	0.6
	Steel	0.566235	0.610976	0.261761	0.533822	0.447807	0.541462	0.696041	0.655096	0.640878	0.603669	...	0.7
	FabPr	0.325719	0.288063	0.374589	0.217098	0.222265	0.323909	0.364488	0.354790	0.287127	0.455999	...	0.3
	Mach	0.622234	0.685913	0.331612	0.619602	0.485354	0.621873	0.757407	0.721212	0.733254	0.680373	...	0.7
	ElcEq	0.614002	0.714241	0.318703	0.612709	0.496086	0.596970	0.746607	0.688423	0.755871	0.635555	...	0.7
	Autos	0.506149	0.619449	0.309640	0.542330	0.433205	0.558241	0.696402	0.681622	0.679934	0.649807	...	0.7
	Aero	0.475548	0.616188	0.276926	0.563731	0.414795	0.533782	0.639799	0.571091	0.640783	0.576795	...	0.6
	Ships	0.529525	0.633231	0.314516	0.544830	0.463441	0.529376	0.630938	0.645323	0.613479	0.589426	...	0.6
	Guns	0.261626	0.334804	0.376740	0.237136	0.261440	0.321699	0.314244	0.295100	0.312955	0.424984	...	0.3
	Gold	0.112317	0.100500	0.072158	0.070565	0.106177	0.111712	0.094787	0.094781	0.083741	0.119375	...	0.1
	Mines	0.548550	0.527516	0.266543	0.484576	0.405681	0.524987	0.618832	0.548160	0.549279	0.544625	...	0.6
	Coal	0.443719	0.466590	0.221038	0.420124	0.349853	0.394057	0.515128	0.508152	0.445192	0.448222	...	0.5
	Oil	0.514581	0.569146	0.215153	0.484355	0.416206	0.438407	0.551047	0.541989	0.540012	0.475797	...	0.5

Util	0.466754	0.701691	0.238727	0.577151	0.502493	0.451631	0.594581	0.563985	0.639760	0.464850	...	0.5
Telcm	0.439418	0.637033	0.363550	0.507954	0.461676	0.491604	0.622700	0.565786	0.595820	0.534858	...	0.6
PerSv	0.413795	0.539806	0.251959	0.491585	0.378445	0.536659	0.574575	0.524635	0.544717	0.562932	...	0.5
BusSv	0.461705	0.567940	0.339542	0.492871	0.395872	0.517974	0.569147	0.603481	0.564189	0.582024	...	0.5
Hardw	0.485539	0.582723	0.277396	0.512892	0.417691	0.511891	0.664718	0.584905	0.671900	0.573867	...	0.6
Softw	0.298369	0.266009	0.302769	0.230878	0.198115	0.305704	0.386750	0.320591	0.294947	0.455608	...	0.3
Chips	0.531229	0.582269	0.276039	0.558633	0.402276	0.579142	0.705500	0.615986	0.642725	0.604936	...	0.6
LabEq	0.542851	0.587456	0.368578	0.506314	0.440240	0.552202	0.672481	0.560893	0.630328	0.602017	...	0.6
Paper	0.339226	0.445443	0.145153	0.549906	0.310774	0.522802	0.524649	0.437698	0.464765	0.418200	...	0.4
Boxes	0.552172	0.701029	0.363503	0.576661	0.500939	0.532622	0.657333	0.645901	0.712487	0.645266	...	1.0
Trans	0.603829	0.687611	0.318683	0.608854	0.480009	0.621066	0.722917	0.708477	0.683291	0.663292	...	0.7
Whlsl	0.547372	0.676131	0.318357	0.664149	0.482531	0.630704	0.734288	0.664899	0.686742	0.654877	...	0.6
Rtail	0.559494	0.779244	0.377232	0.646874	0.513657	0.603888	0.744741	0.687990	0.763569	0.739077	...	0.7
Meals	0.533303	0.705775	0.416439	0.635849	0.484112	0.639390	0.727745	0.646935	0.692310	0.680269	...	0.6
Banks	0.527050	0.697784	0.359733	0.598558	0.508700	0.548438	0.675223	0.629945	0.677266	0.607806	...	0.6
Insur	0.568157	0.733186	0.314577	0.596377	0.513990	0.488532	0.701952	0.600113	0.695197	0.571042	...	0.6
RIEst	0.490012	0.595841	0.304714	0.548577	0.407512	0.547971	0.663460	0.641775	0.586625	0.618484	...	0.5
Fin	0.592978	0.700761	0.314659	0.617949	0.478121	0.578668	0.763490	0.691074	0.702283	0.644126	...	0.7
Other	0.521455	0.647417	0.328630	0.572498	0.490388	0.578241	0.679032	0.612758	0.671501	0.622855	...	0.6

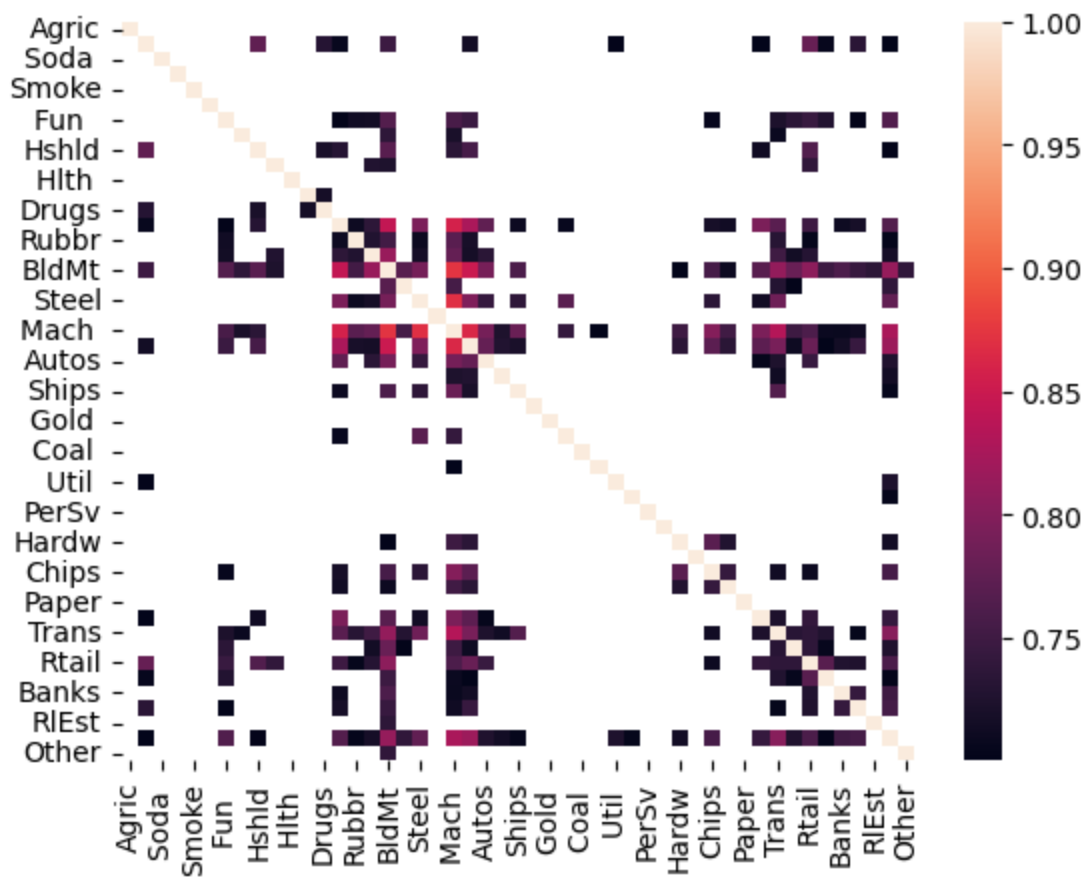
49 rows × 49 columns

In [194...

```
#Only cases with absolute correlation greater than or equal to 0.7
sns.heatmap(value_wted_returns.iloc[:,1:].corr()[(value_wted_returns.iloc[:,1:].corr())>=
```

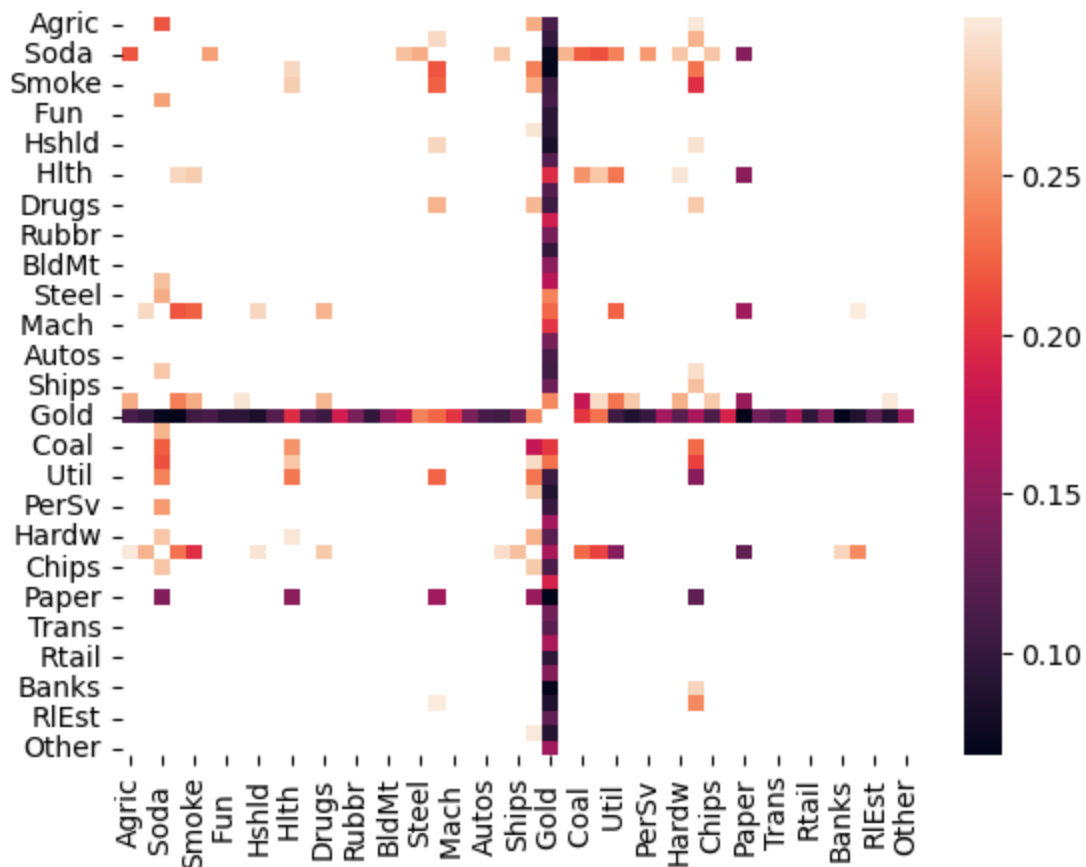
Out[194]:

<AxesSubplot:>



```
In [38]: #Only cases with absolute correlation less than or equals to 0.3
sns.heatmap(value_wted_returns.iloc[:,1:].corr()[(value_wted_returns.iloc[:,1:].corr())>=
```

```
Out[38]: <AxesSubplot:>
```



```
In [39]: #Conversion to time-series data
l=[]
```

```

for i in value_wted_returns.columns[1:]:
    df_temp=pd.DataFrame()
    df_temp['Time']=value_wted_returns['Time']
    df_temp['Industry']=i
    df_temp['Industry_Returns']=value_wted_returns[i]
    l.append(df_temp)
df_ts=pd.concat(l,axis=0)
df_ts.info()

```

```

<class 'pandas.core.frame.DataFrame'>
Int64Index: 56399 entries, 0 to 1150
Data columns (total 3 columns):
#   Column                Non-Null Count  Dtype
---  -
0   Time                  56399 non-null object
1   Industry              56399 non-null object
2   Industry_Returns      56399 non-null float64
dtypes: float64(1), object(2)
memory usage: 1.7+ MB

```

In [40]: *#Our data gets further reduced in size due to missing data for certain dates in either o*

```

df_fin=pd.merge(df_ts,ff_monthly_data,how='inner',on='Time')
df_fin.info()

```

```

<class 'pandas.core.frame.DataFrame'>
Int64Index: 34643 entries, 0 to 34642
Data columns (total 9 columns):
#   Column                Non-Null Count  Dtype
---  -
0   Time                  34643 non-null object
1   Industry              34643 non-null object
2   Industry_Returns      34643 non-null float64
3   Mkt-RF                34643 non-null object
4   SMB                   34643 non-null object
5   HML                   34643 non-null object
6   RMW                   34643 non-null object
7   CMA                   34643 non-null object
8   RF                    34643 non-null object
dtypes: float64(1), object(8)
memory usage: 2.6+ MB

```

In [41]: *#Excess return calculations*

```

df_fin[df_fin.columns[3:]] = df_fin[df_fin.columns[3:]].astype(float)
df_fin['re_bar'] = df_fin['Industry_Returns'] - df_fin['RF']
df_fin.head(10)

```

Out[41]:

	Time	Industry	Industry_Returns	Mkt-RF	SMB	HML	RMW	CMA	RF	re_bar
0	196307	Agric	3.04	-0.39	-0.44	-0.89	0.68	-1.23	0.27	2.77
1	196307	Food	-0.46	-0.39	-0.44	-0.89	0.68	-1.23	0.27	-0.73
2	196307	Soda	2.57	-0.39	-0.44	-0.89	0.68	-1.23	0.27	2.30
3	196307	Beer	-2.19	-0.39	-0.44	-0.89	0.68	-1.23	0.27	-2.46
4	196307	Smoke	-2.54	-0.39	-0.44	-0.89	0.68	-1.23	0.27	-2.81
5	196307	Toys	-5.07	-0.39	-0.44	-0.89	0.68	-1.23	0.27	-5.34
6	196307	Fun	-0.70	-0.39	-0.44	-0.89	0.68	-1.23	0.27	-0.97
7	196307	Books	-0.07	-0.39	-0.44	-0.89	0.68	-1.23	0.27	-0.34
8	196307	Hshld	-0.15	-0.39	-0.44	-0.89	0.68	-1.23	0.27	-0.42
9	196307	Clths	-0.67	-0.39	-0.44	-0.89	0.68	-1.23	0.27	-0.94

```
In [44]: #Industry wise calculation
risk_return_df=df_fin.groupby('Industry').agg({'Industry_Returns':['mean','std']})
risk_return_df.head(10)
```

Out[44]:

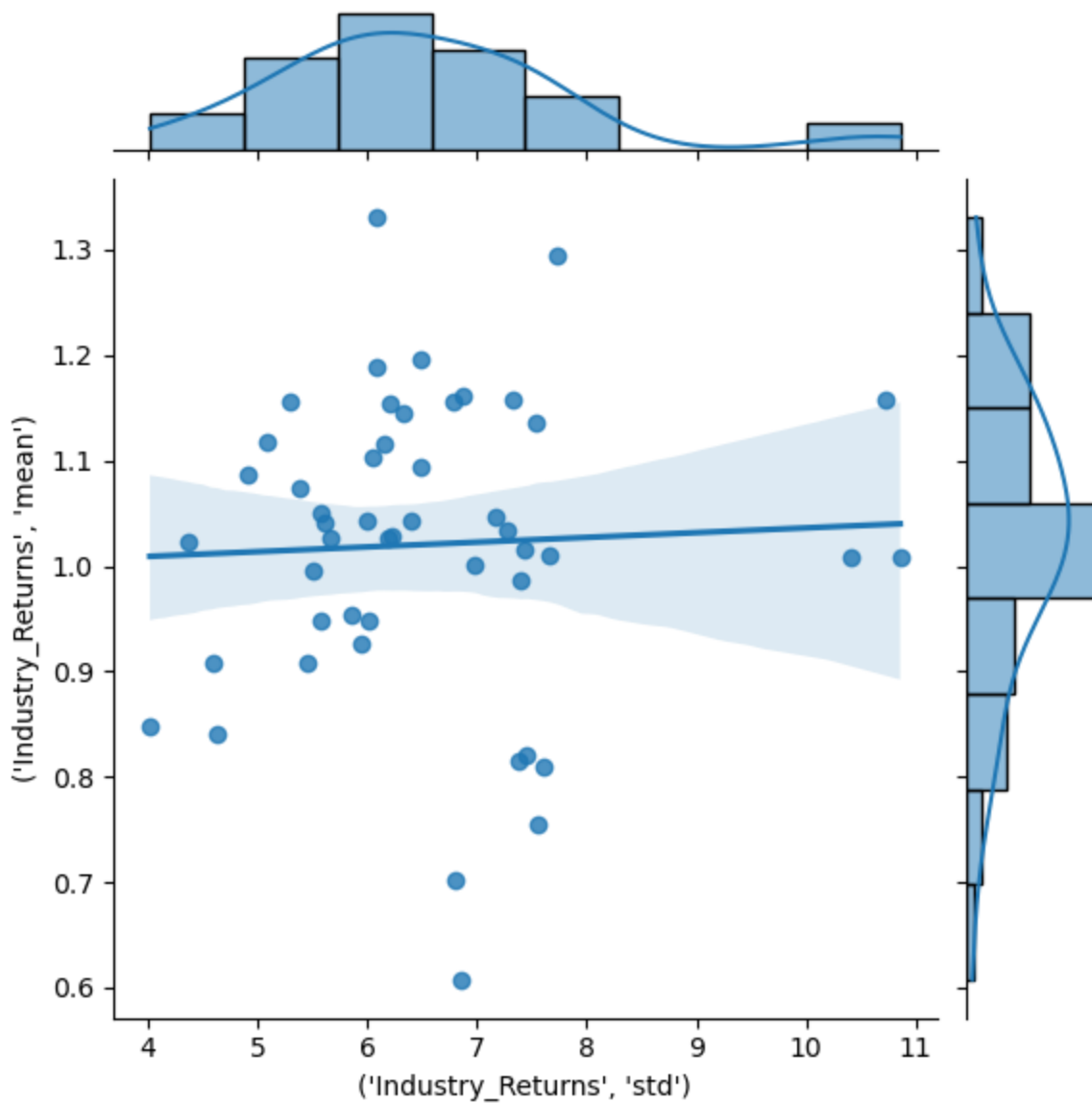
	Industry_Returns	
	mean	std
Industry		
Aero	1.160594	6.873825
Agric	1.042801	6.401401
Autos	1.015502	7.435402
Banks	0.947836	6.012328
Beer	1.117949	5.086936
BldMt	1.026040	6.191058
Books	0.925502	5.939802
Boxes	0.995615	5.511701
BusSv	1.026294	5.669321
Chems	0.948741	5.580444

```
In [45]: risk_return_df.shape
```

Out[45]: (49, 2)

```
In [46]: sns.jointplot(y=risk_return_df['Industry_Returns', 'mean'],x=risk_return_df['Industry_Returns', 'std'])
```

Out[46]: <seaborn.axisgrid.JointGrid at 0x29a897ea3a0>



Traditional Risk-Return paradigm states that risk and the corresponding return go hand in hand, that is, higher the risk corresponds to higher reward. We can clearly observe quite a lot of deviation from the ideal case. This deviation can be attributed to the long time horizon and the different natures of all the different industries and their corresponding market circumstances. All in all, we observe a positive slope which is in agreement with the ideal case despite having such a diverse data sample.

1. FF 3 factor model's industry wise application

a) Industry wise

```
In [47]: l=[]
for i in df_fin['Industry'].unique():
    df_temp=df_fin[df_fin['Industry']==i]
    X=df_fin[df_fin['Industry']==i][['Mkt-RF','HML','SMB']]
    y=df_fin[df_fin['Industry']==i]['re_bar']
    model=LinearRegression()
    model.fit(X,y)
    l.append([i,model.intercept_,model.coef_[0],model.coef_[1],model.coef_[2]])
```

```
In [48]: output_parameters=pd.DataFrame(l,columns=['Industry','alpha','beta_mke-rf','beta_hml','b
output_parameters.set_index('Industry',inplace=True)
output_parameters.head(10)
```

Out[48]:

	alpha	beta_mke-rf	beta_hml	beta_smb
Industry				
Agric	0.123052	0.792252	0.054621	0.419211
Food	0.224902	0.728281	0.190194	-0.158193
Soda	0.274125	0.866519	0.205056	-0.161487
Beer	0.319567	0.777741	0.081535	-0.130624
Smoke	0.532657	0.731028	0.249511	-0.249968
Toys	-0.295823	1.093581	0.035539	0.543507
Fun	0.106524	1.273701	0.003684	0.473940
Books	-0.178282	1.063937	0.243308	0.293418
Hshld	0.123085	0.818153	-0.017683	-0.151367
Clths	-0.027471	1.069713	0.221113	0.388554

We test for which all industries do we have a significant α value.

Statistical test for positive alpha values:

$$H_o : \alpha \leq 0$$

$$H_a : \alpha > 0$$

We do a t-test for above hypothesis. It will be a right tailed test at 95% confidence interval.

```
In [50]: df_t_test=output_parameters['alpha'].to_frame()
df_t_test['t_score']=(df_t_test['alpha']-df_t_test['alpha'].mean())/(df_t_test['alpha'].
df_t_test
```

Out[50]:

	alpha	t_score
Industry		
Agric	0.123052	0.576462
Food	0.224902	0.997931
Soda	0.274125	1.201621
Beer	0.319567	1.389671
Smoke	0.532657	2.271469
Toys	-0.295823	-1.156911
Fun	0.106524	0.508066
Books	-0.178282	-0.670509
Hshld	0.123085	0.576595
Clths	-0.027471	-0.046428
Hlth	-0.007516	0.036148
MedEq	0.377056	1.627569
Drugs	0.409976	1.763794
Chems	-0.135012	-0.491449

Rubbr	0.004920	0.087609
Txtls	-0.350674	-1.383892
BldMt	-0.198565	-0.754443
Cnstr	-0.203660	-0.775524
Steel	-0.483452	-1.933346
FabPr	-0.315638	-1.238907
Mach	-0.093855	-0.321133
ElcEq	0.068233	0.349609
Autos	-0.233029	-0.897060
Aero	-0.009518	0.027863
Ships	-0.141694	-0.519102
Guns	0.208567	0.930332
Gold	0.292011	1.275638
Mines	-0.028855	-0.052154
Coal	-0.034739	-0.076504
Oil	0.017448	0.139456
Util	0.082224	0.407506
Telcm	0.001827	0.074811
PerSv	-0.374036	-1.480567
BusSv	0.015098	0.129729
Hardw	0.140494	0.648637
Softw	-0.035897	-0.081298
Chips	0.165183	0.750804
LabEq	0.206508	0.921815
Paper	-0.127222	-0.459211
Boxes	0.064744	0.335170
Trans	-0.154208	-0.570883
Whlsl	-0.006968	0.038419
Rtail	0.160553	0.731646
Meals	0.172796	0.782308
Banks	-0.269482	-1.047906
Insur	-0.001626	0.060521
RIEst	-0.623108	-2.511268
Fin	-0.050892	-0.143348
Other	-0.506653	-2.029359

```
In [51]: t_stat_critical_value=s.t.ppf(q=0.95,df=48)
t_stat_critical_value
```

Out[51]: 1.6772241953450393

```
In [200]: df_t_test['Reject_Ho']=np.where((df_t_test['t_score']>t_stat_critical_value)|(df_t_test[
df_t_test[df_t_test['Reject_Ho']==1]
```

Out[200]:

	alpha	t_score	Reject_Ho
--	-------	---------	-----------

Industry

Smoke	0.532657	2.271469	1
Drugs	0.409976	1.763794	1
Steel	-0.483452	-1.933346	1
RIEst	-0.623108	-2.511268	1
Other	-0.506653	-2.029359	1

b) Overall market

```
In [53]: # R regression approach for overall market

df_2nd_pass=df_fin.groupby('Industry').mean()['re_bar']
df_2nd_pass=df_2nd_pass.sort_index()

df_final=output_parameters.sort_index()
df_final['re_bar']=df_2nd_pass
df_final.drop(columns=['alpha'],inplace=True)
df_final
```

Out[53]:

	beta_mke-rf	beta_hml	beta_smb	re_bar
--	-------------	----------	----------	--------

Industry

Aero	1.154123	0.326350	0.246603	0.796973
Agric	0.792252	0.054621	0.419211	0.679180
Autos	1.265263	0.454733	0.137214	0.651881
Banks	1.194491	0.665083	-0.119846	0.584215
Beer	0.777741	0.081535	-0.130624	0.754328
BldMt	1.199291	0.401560	0.272023	0.662419
Books	1.063937	0.243308	0.293418	0.561881
Boxes	0.977340	0.098625	-0.064160	0.631994
BusSv	1.064510	-0.129574	0.398365	0.662673
Chems	1.106349	0.334070	-0.033097	0.585120
Chips	1.244688	-0.471083	0.333086	0.793508
Clths	1.069713	0.221113	0.388554	0.730071
Cnstr	1.235851	0.216194	0.498143	0.670198
Coal	1.104526	0.340065	0.453170	0.793748
Drugs	0.811561	-0.265418	-0.281450	0.722405
ElcEq	1.211425	0.022051	0.106481	0.781273
FabPr	1.021359	0.167546	0.655578	0.457016

Fin	1.249810	0.247246	0.102387	0.752999
Food	0.728281	0.190194	-0.158193	0.659533
Fun	1.273701	0.003684	0.473940	0.930184
Gold	0.508354	-0.043782	0.360953	0.644639
Guns	0.836448	0.350894	0.197723	0.832885
Hardw	1.098486	-0.490863	0.140310	0.637652
HLth	0.965435	-0.025345	0.533935	0.646663
Hshld	0.818153	-0.017683	-0.151367	0.545134
Insur	1.039844	0.419258	-0.130485	0.686025
LabEq	1.113354	-0.450969	0.450837	0.793126
Mach	1.174607	0.086558	0.311329	0.663819
Meals	1.012593	0.077212	0.262841	0.825545
MedEq	0.857152	-0.281932	0.086301	0.791344
Mines	1.106386	0.318476	0.357801	0.772871
Oil	0.944245	0.491733	-0.104552	0.679533
Other	1.138192	0.154611	0.276869	0.244074
Paper	1.014149	0.332004	-0.012956	0.544767
PerSv	1.035001	0.061052	0.499222	0.338571
RIEst	1.154797	0.547170	0.872141	0.390835
Rtail	0.977786	-0.046554	0.061144	0.710552
Rubbr	0.991946	0.145007	0.588126	0.739066
Ships	1.139721	0.442853	0.204747	0.683706
Smoke	0.731028	0.249511	-0.249968	0.967016
Soda	0.866519	0.205056	-0.161487	0.790552
Softw	1.282164	-0.753334	0.872137	0.644837
Steel	1.283837	0.369072	0.409657	0.445488
Telcm	0.837358	0.146211	-0.191829	0.476789
Toys	1.093581	0.035539	0.543507	0.451641
Trans	1.083384	0.284701	0.205318	0.590325
Txtls	1.118299	0.633929	0.661026	0.623041
Util	0.606420	0.336512	-0.200872	0.484314
Whlsl	0.988903	0.060981	0.485809	0.676676

```
In [54]: X=sm.add_constant(df_fin[['Mkt-RF', 'HML', 'SMB']])
y=df_fin['re_bar']

model=sm.OLS(y,X).fit()
print(model.summary())
```

OLS Regression Results

=====

```

Dep. Variable:          re_bar    R-squared:          0.504
Model:                  OLS      Adj. R-squared:        0.504
Method:                 Least Squares    F-statistic:          1.172e+04
Date:                   Tue, 07 Feb 2023    Prob (F-statistic):      0.00
Time:                   21:45:54    Log-Likelihood:        -1.0285e+05
No. Observations:      34643    AIC:                  2.057e+05
Df Residuals:          34639    BIC:                  2.057e+05
Df Model:              3
Covariance Type:        nonrobust

```

	coef	std err	t	P> t	[0.025	0.975]
const	-0.0163	0.026	-0.631	0.528	-0.067	0.034
Mkt-RF	1.0278	0.006	169.123	0.000	1.016	1.040
HML	0.1396	0.009	15.861	0.000	0.122	0.157
SMB	0.2279	0.009	26.130	0.000	0.211	0.245
Omnibus:	7824.968		Durbin-Watson:	1.576		
Prob(Omnibus):	0.000		Jarque-Bera (JB):	142739.118		
Skew:	0.612		Prob(JB):	0.00		
Kurtosis:	12.869		Cond. No.	4.78		

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

Based on above, we can say that when the whole market is considered at once, then we find that all three coefficients are significant and Market risk premium dominates the other two factors in dependent variable's sensitivity to it.

2. Correlation between Automobile stocks

```

In [235... import yfinance as yf
from pandas.plotting import scatter_matrix
from datetime import datetime

```

```

In [222... datetime.now().year

```

Out[222]: 2023

```

In [228... symbol = 'TSLA'
ticker = yf.Ticker(symbol)
tesla = ticker.history(period='1y',
interval='1d',
actions=True,
auto_adjust=True)
tesla.info()

```

```

<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 252 entries, 2022-02-07 00:00:00-05:00 to 2023-02-07 00:00:00-05:00
Data columns (total 7 columns):
#   Column      Non-Null Count  Dtype
---  -
0   Open        252 non-null   float64
1   High        252 non-null   float64
2   Low         252 non-null   float64
3   Close       252 non-null   float64
4   Volume      252 non-null   int64
5   Dividends   252 non-null   float64
6   Stock Splits 252 non-null   float64
dtypes: float64(6), int64(1)
memory usage: 15.8 KB

```

```
In [229... symbol = 'F'
ticker = yf.Ticker(symbol)
ford = ticker.history(period='1y',
interval='1d',
actions=True,
auto_adjust=True)
ford.info()
```

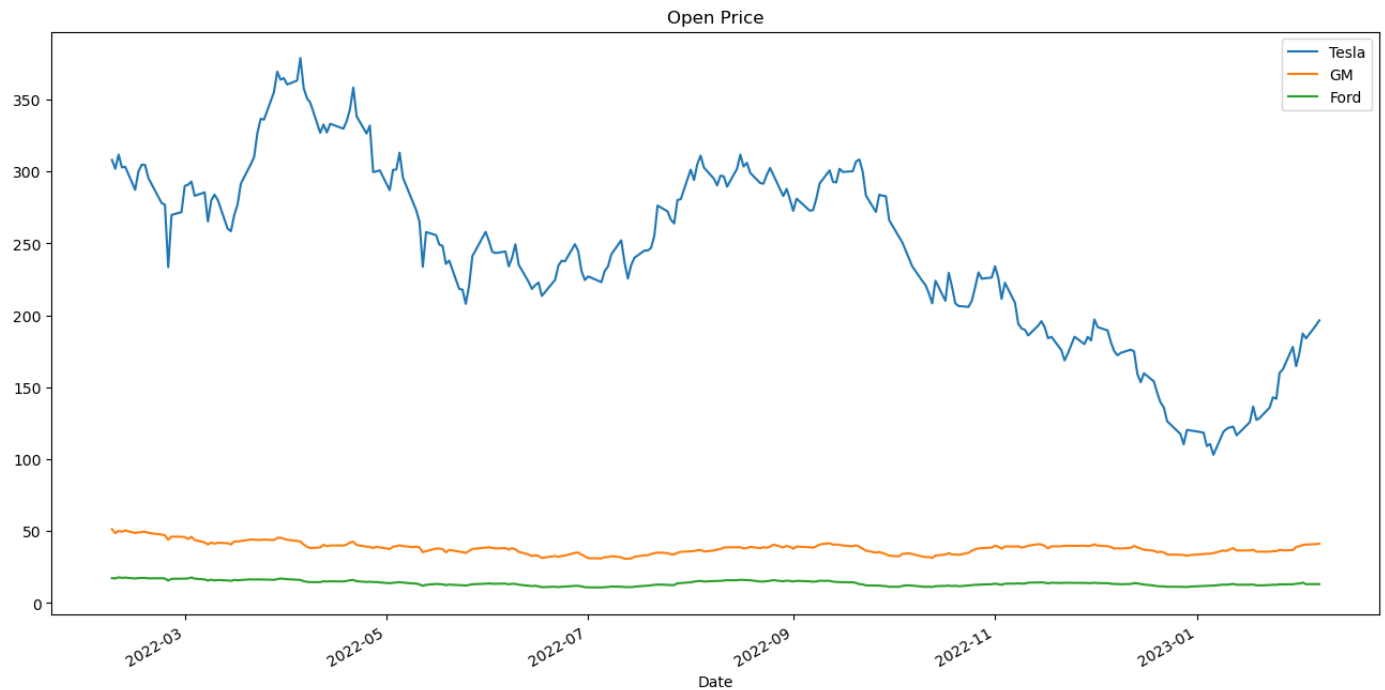
```
<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 252 entries, 2022-02-07 00:00:00-05:00 to 2023-02-07 00:00:00-05:00
Data columns (total 7 columns):
#   Column          Non-Null Count  Dtype
---  -
0   Open            252 non-null   float64
1   High            252 non-null   float64
2   Low             252 non-null   float64
3   Close           252 non-null   float64
4   Volume          252 non-null   int64
5   Dividends       252 non-null   float64
6   Stock Splits    252 non-null   float64
dtypes: float64(6), int64(1)
memory usage: 15.8 KB
```

```
In [230... symbol = 'GM'
ticker = yf.Ticker(symbol)
gm = ticker.history(period='1y',
interval='1d',
actions=True,
auto_adjust=True)
gm.info()
```

```
<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 252 entries, 2022-02-07 00:00:00-05:00 to 2023-02-07 00:00:00-05:00
Data columns (total 7 columns):
#   Column          Non-Null Count  Dtype
---  -
0   Open            252 non-null   float64
1   High            252 non-null   float64
2   Low             252 non-null   float64
3   Close           252 non-null   float64
4   Volume          252 non-null   int64
5   Dividends       252 non-null   float64
6   Stock Splits    252 non-null   float64
dtypes: float64(6), int64(1)
memory usage: 15.8 KB
```

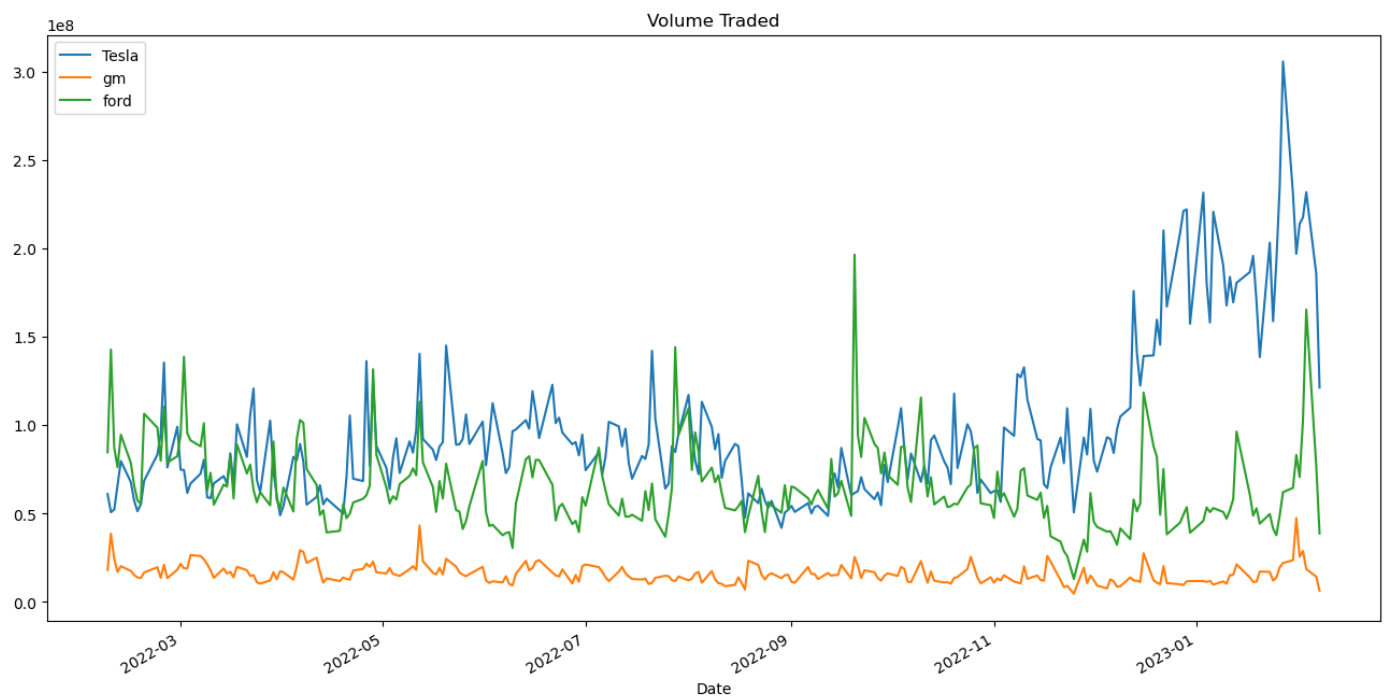
```
In [231... tesla['Open'].plot(label='Tesla',figsize=(16,8),title='Open Price')
gm['Open'].plot(label='GM')
ford['Open'].plot(label='Ford')
plt.legend()
```

```
Out[231]: <matplotlib.legend.Legend at 0x29a8f6bde50>
```



```
In [232]: tesla['Volume'].plot(label='Tesla',figsize=(16,8),title='Volume Traded')
gm['Volume'].plot(label='gm')
ford['Volume'].plot(label='ford')
plt.legend()
```

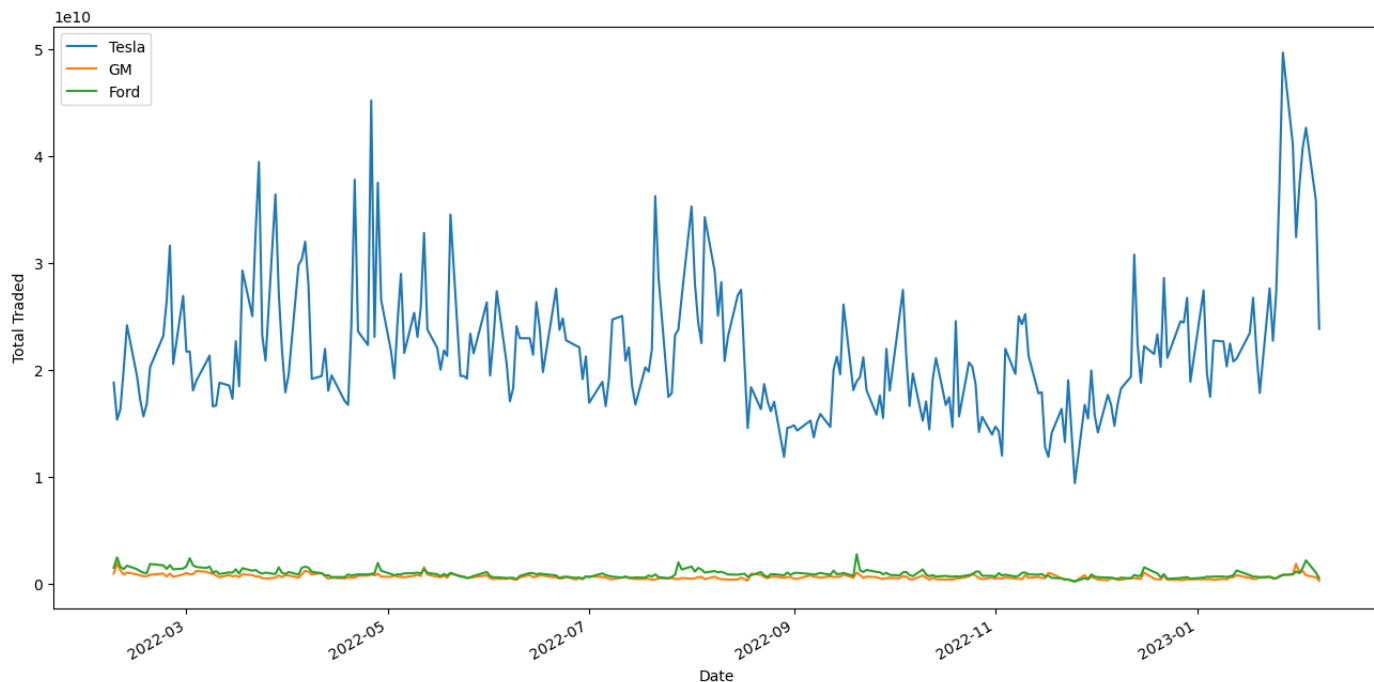
Out[232]: <matplotlib.legend.Legend at 0x29a91164e80>



```
In [233]: tesla['Total Traded'] = tesla['Open']*tesla['Volume']
ford['Total Traded'] = ford['Open']*ford['Volume']
gm['Total Traded'] = gm['Open']*gm['Volume']
```

```
In [241]: tesla['Total Traded'].plot(label='Tesla',figsize=(16,8))
gm['Total Traded'].plot(label='GM')
ford['Total Traded'].plot(label='Ford')
plt.legend()
plt.ylabel('Total Traded')
```

Out[241]: Text(0, 0.5, 'Total Traded')



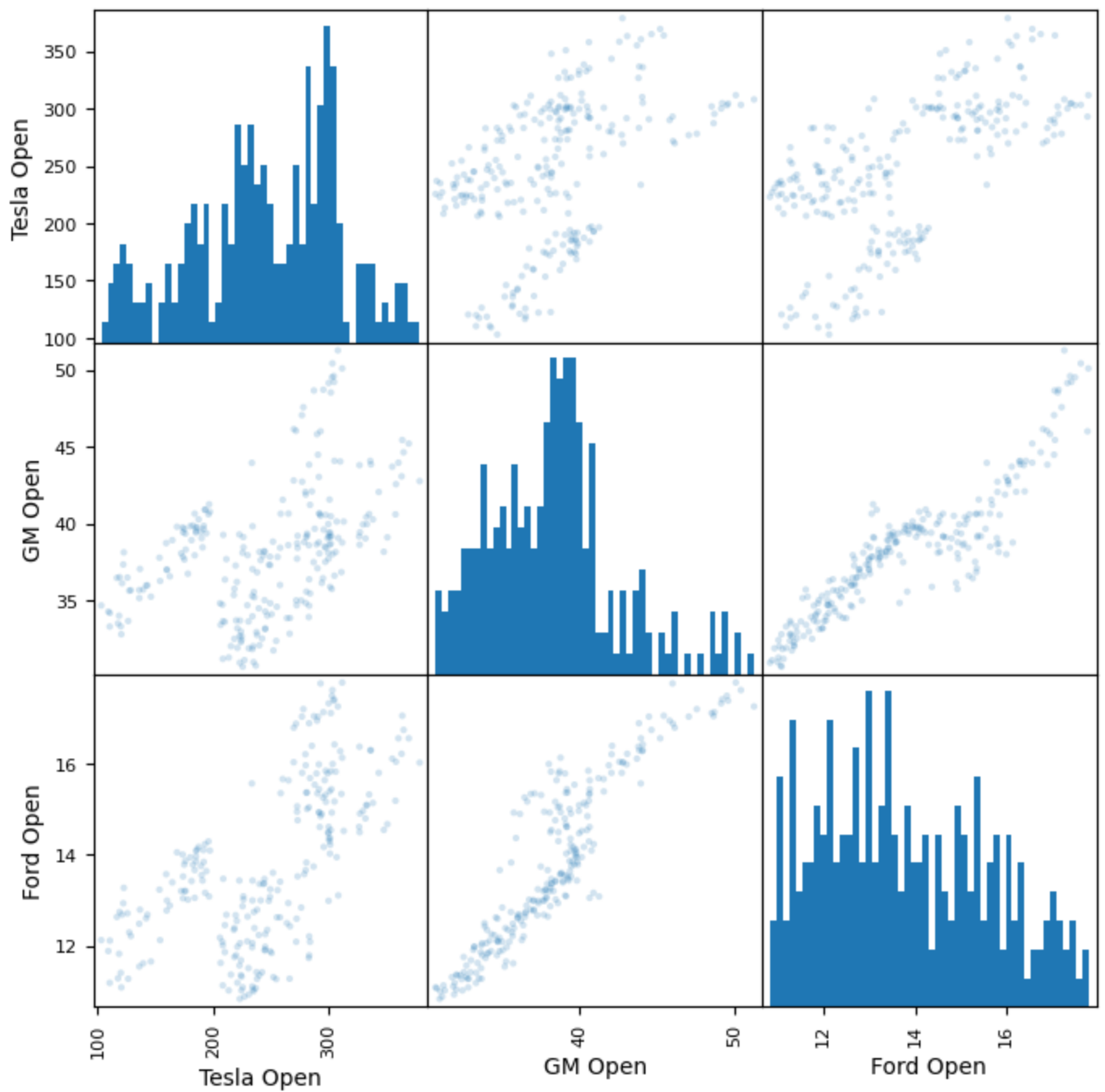
In [236...

```
comparison = pd.concat([tesla['Open'], gm['Open'], ford['Open']], axis=1)
comparison.columns = ['Tesla Open', 'GM Open', 'Ford Open']

scatter_matrix(comparison, figsize=(8,8), alpha=0.2, hist_kwds={'bins':50})
```

Out[236]:

```
array([[<AxesSubplot:xlabel='Tesla Open', ylabel='Tesla Open'>,
        <AxesSubplot:xlabel='GM Open', ylabel='Tesla Open'>,
        <AxesSubplot:xlabel='Ford Open', ylabel='Tesla Open'>],
       [<AxesSubplot:xlabel='Tesla Open', ylabel='GM Open'>,
        <AxesSubplot:xlabel='GM Open', ylabel='GM Open'>,
        <AxesSubplot:xlabel='Ford Open', ylabel='GM Open'>],
       [<AxesSubplot:xlabel='Tesla Open', ylabel='Ford Open'>,
        <AxesSubplot:xlabel='GM Open', ylabel='Ford Open'>,
        <AxesSubplot:xlabel='Ford Open', ylabel='Ford Open'>]],
      dtype=object)
```



```
In [251...] comparison.describe().loc['mean',:]/comparison.describe().loc['std',:]
```

```
Out[251]: Tesla Open    3.900512
          GM Open     9.155948
          Ford Open    7.624141
          dtype: float64
```

```
In [237...] tesla['Open'].corr(ford['Open'])
```

```
Out[237]: 0.6315345206188344
```

```
In [238...] tesla['Open'].corr(gm['Open'])
```

```
Out[238]: 0.4539597606104765
```

```
In [239...] gm['Open'].corr(ford['Open'])
```

```
Out[239]: 0.9065758928982761
```

```
In [255...] comparison_2 = pd.concat([tesla['Close'],gm['Close'],ford['Close']],axis=1)
```

```
comparison_2.columns = ['Tesla Close', 'GM Close', 'Ford Close']
```

```
ret=comparison_2.pct_change().dropna()  
ret.describe()
```

Out[255]:

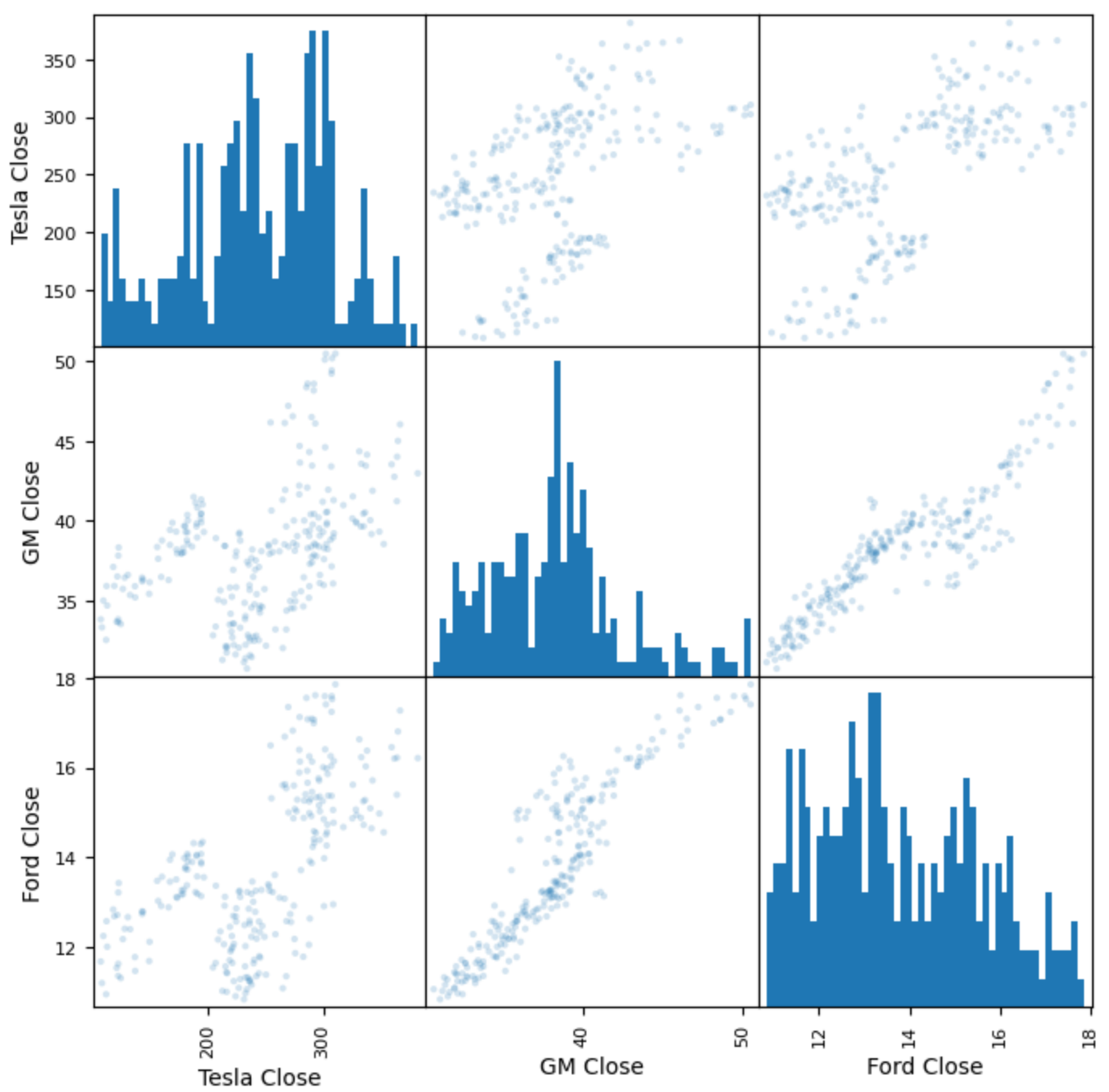
	Tesla Close	GM Close	Ford Close
count	251.000000	251.000000	251.000000
mean	-0.000914	-0.000459	-0.000671
std	0.042503	0.027837	0.029467
min	-0.122422	-0.080749	-0.123242
25%	-0.025651	-0.019388	-0.020458
50%	0.000974	0.000985	0.001460
75%	0.023823	0.017643	0.018458
max	0.110002	0.089139	0.085209

In [256...

```
scatter_matrix(comparison_2,figsize=(8,8),alpha=0.2,hist_kwds={'bins':50})
```

Out[256]:

```
array([[<AxesSubplot:xlabel='Tesla Close', ylabel='Tesla Close'>,  
       <AxesSubplot:xlabel='GM Close', ylabel='Tesla Close'>,  
       <AxesSubplot:xlabel='Ford Close', ylabel='Tesla Close'>],  
       [<AxesSubplot:xlabel='Tesla Close', ylabel='GM Close'>,  
       <AxesSubplot:xlabel='GM Close', ylabel='GM Close'>,  
       <AxesSubplot:xlabel='Ford Close', ylabel='GM Close'>],  
       [<AxesSubplot:xlabel='Tesla Close', ylabel='Ford Close'>,  
       <AxesSubplot:xlabel='GM Close', ylabel='Ford Close'>,  
       <AxesSubplot:xlabel='Ford Close', ylabel='Ford Close'>]],  
      dtype=object)
```



In []: